ALIGNMENT, VIBRATIONAL, AND STERIC EFFECTS IN
UNIMOLECULAR AND BIMOLECULAR SYSTEMS:
TOWARDS AN UNDERSTANDING OF CHEMICAL REACTIONS IN
QUANTUM-STATE DETAIL

by

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This thesis describes a series of experimental and theoretical projects designed to explore the dynamics of molecules and molecular collision systems in quantum-state resolved detail. First, the unimolecular dynamics of HOD are explored via photoacoustic spectroscopy of the $3\nu_{\text{OH}}$ and $4\nu_{\text{OH}}$ overtone bands. Analysis of the overtone series provides the vibrational dependence of rotational constants as well as evidence that the transition dipole moment vector tilts away from the OH bond with increasing excitation, inconsistent with simple local-mode, bond-dipole model predictions but in excellent agreement with full 3D quantum variational calculations.

Second, the generation of radical clusters from the photolysis of Ar-H$_2$S and Ar$_2$-H$_2$S is investigated via quasiclassical trajectory calculations, providing a comparison with earlier experiments in supersonic jet expansions. The calculations confirm the overall efficiency of radical cluster formation as well as significant intracluster excitation; clusters with excess rotational energy above the dissociation limit are found to be trapped by an angular momentum barrier that prevents dissociation.

Third, quasiclassical trajectory calculations on experimentally determined intermolecular potentials for He-O$_2$, He-CO, and He-CO$_2$ simulate the collisional formation of rotationally aligned molecular distributions in a supersonic expansion. These calculations verify a preference for $\mathbf{j}$ perpendicular to the expansion axis, with
asymptotic alignment increasing monotonically with j. This alignment reflects comparable contributions from elastic and inelastic collisions; in addition, molecules with \( j \) aligned parallel to the expansion axis have faster average velocities than molecules with \( j \) perpendicular. Fourth, the role of intramolecular vibrational redistribution on the timescale of a reactive encounter is explored with a reduced-dimensionality model of \( \text{Cl} + \text{H}_2\text{O} \rightarrow \text{HCl} + \text{OH} \), with isotopic variations. The vibrational eigenstates of \( \text{H}_2\text{O}/\text{HOD}/\text{D}_2\text{O} \) are calculated versus Cl-water separation, generating adiabatic potential energy curves and nonadiabatic coupling terms for time-dependent dynamics calculations. For the vibrational eigenstates, the near-resonance of the \( \text{H}_2\text{O} \) symmetric and asymmetric stretches rotates the symmetric/asymmetric stretch towards/away from the Cl atom as it approaches in the vibrationally adiabatic limit. For Cl+HOD, vibrational excitation in the OH mode enhances HCl + OD reaction probability by more than an order of magnitude more than excitation in OD.
To my parents, Frank and Janet, and my brother, Ken,

and

in memory of my grandparents
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CHAPTER 1
INTRODUCTION

A physical chemist’s ultimate goal might be to understand and manipulate each aspect of a reactive encounter, i.e., the initial rovibrational states of the reactants, relative orientations, direction of approach, and collision velocities, guiding the breaking and formation of bonds at a state-to-state level of detail. While such detailed understanding and control of chemical reaction is not currently feasible experimentally, a number of strides have nevertheless been made in this direction. Two well-developed areas of this study included vibrationally mediated chemistry\(^1\) and stereodynamical control of chemical reactions,\(^2\) with progress in these areas more fully detailed in subsequent chapters.

The crossroads between these two areas can be beautifully illustrated by a series of experiments by the Zare group on the reaction of CH\(_4\) and CD\(_3\)H with Cl atoms.\(^3-5\) In these studies, CH\(_4\), coexpanded with Cl\(_2\), was vibrationally excited to \(v_3=1\) (asymmetric stretch); the Cl\(_2\) was then photolyzed at 355 nm to produce collisions between Cl and CH\(_4\) at a collision energy of 1280 cm\(^{-1}\). The state-to-state differential cross sections for the reaction of Cl with CH\(_4\)(\(v_3=1\)) were measured and
compared with results from ground-state CH\textsubscript{4} and CD\textsubscript{3}H(\nu_1=1, CH stretch). This series of experiments determined sufficient detail about the nature of the reactive encounter to propose a mechanism for the H-atom abstraction, namely, that small, medium, and large impact parameters produce backwards, forwards, and sideways scattering of the HCl, respectively. CH\textsubscript{4} vibrational excitation was shown to increase the cone angle of acceptance for reaction. This mechanism was then confirmed by studies of steric effects in the reaction of Cl with spatially aligned CD\textsubscript{3}H.

This example illustrates three major steps in understanding chemical reaction in quantum-state detail: preparation and interrogation of a specific quantum state of the reactant molecule; control and understanding of the interaction between the reactants; and collection and analysis of the products of the reaction. In a series of four projects, we follow this path toward quantum-state understanding of chemical reactions, beginning with the preparation of a molecule in a single quantum state and concluding with a study of how such a prepared quantum state influences chemical reaction. Over the course of this thesis, the interchange between theory and experiment is emphasized, and in particular, the opportunities for theory to provide insight initially unavailable from experiment alone are stressed.

The first project, described in Chapter 2, involves the experimental investigation of the unimolecular dynamics of HOD via OH vibrational overtone excitation.\textsuperscript{6} From an experimental point of view, vibrational excitation of a particular bond, which can be used to prepare this molecule in a single rovibrational quantum state, provides a path towards selective reaction. Since the probability of absorbing a photon varies as the cosine squared of the angle between the transition dipole moment
of the molecule and the polarization vector of the light, such photoexcitation can prepare an aligned distribution of reactive molecules for stereochemical studies. Importantly, this study provides evidence that for OH overtone transitions, the transition dipole moment vector tilts away from the OH bond with increasing $v_{OH}$ excitation, qualitatively inconsistent with simple local-mode, bond-dipole model predictions of the vibrational transition moments. This observation thus provides the opportunity for exchange between theory and experiment: the relative importance of electrical (i.e., in the dipole surface) versus mechanical (i.e., in the potential surface) anharmonicity effects are investigated by 2D and 3D quantum variational calculations.

The second project, described in Chapter 3, extends the study of unimolecular dynamics to unimolecular collisions via photodissociation of a reactive precursor within a cluster. Specifically, the production of radical clusters from the photolysis of Ar-H$_2$S and Ar$_2$-H$_2$S is investigated via quasiclassical trajectory calculations, providing a comparison with earlier experiments on these clusters in supersonic jet expansions. If the cluster is considered as a single unit, this process is a means of preparing a wide range of cluster quantum states for subsequent dynamical studies. Alternatively, photodissociation within clusters of potentially reactive species provides the possibility of controlling the geometry of the reactive encounter. Thus, this study provides the next step on the path towards understanding reactive bimolecular collisions. Once again, this work allows for interchange between experiment and theory through investigating the details of the experimentally observed photodissociation process. Not only do the photolysis calculations confirm
the overall efficiency of radical cluster formation, but they also provide evidence for
bound clusters with excess rotational energy above the dissociation limit, trapped by
an angular momentum barrier that prevents dissociation. These calculations thus
contribute additional understanding of the cluster dynamics unavailable from the
experiment.

The third project, described in Chapter 4, extends the study of collision
dynamics to bimolecular, nonreactive scattering with a computational study of
collisional alignment in supersonic expansions. Experimentally, collisions between a
light “diluent” gas and heavier “seed” rotor molecules in a seeded supersonic
expansion have been shown to produce a distribution of rotor molecules with a
preference for $j$ perpendicular to the expansion axis. This phenomenon has been
demonstrated for a wide variety of rotor molecules and collision partners, aligning a
more general class of molecules than can be accomplished with AC and DC field
methods. Despite the promising possibility that collisional alignment could be used
to prepare reagents for studies of steric effects in chemical reactions, it has yet to see
practical application in this way. In part, this results from a current lack of agreement
among experimental and theoretical studies about the details of this alignment
process. The goal of this chapter thus is to elucidate the mechanism of alignment via
classical trajectory calculations on experimentally determined intermolecular
potentials. We focus on particular areas of controversy such as the velocity- and $j$-
dependence of alignment, as well as on determining the relative contributions from
both elastic ($m_j$-changing) and inelastic ($j$-changing) collisions.
The final project, described in Chapter 5, concludes the study of collision dynamics with an investigation of vibrational effects in chemical reaction, focusing on the reaction of Cl with water and its isotopes. While vibrationally mediated chemistry has been investigated in great detail both experimentally and theoretically, few studies have directly probed the effect of the reactive atom on the vibrational state of the molecule. Consequently, we explore the role of the reactive atom in intramolecular vibrational redistribution on the timescale of a reactive encounter via time-dependent quantum reactive scattering. In these studies, the vibrational eigenstates of a reduced-dimensionality model of Cl + H₂O → HCl + OH (and isotopic variations) are calculated as a function of Cl-H₂O center of mass separation, generating adiabatic potential energy curves and the nonadiabatic coupling matrix elements between these curves for use in time-dependent dynamics simulations. These calculations allow us to look in detail at the nature of the vibrational eigenfunctions for H₂O/D₂O/HOD with chlorine-atom approach. In this study, we have thus come full circle from our initial work on the overtone spectroscopy of HOD to probe how an initially prepared quantum state is influenced and changed by the reactive encounter.
References for Chapter 1


CHAPTER 2
OH STRETCH OVERTONE SPECTROSCOPY AND TRANSITION DIPOLE ALIGNMENT OF HOD

2.1 Introduction

In recent years, a wealth of experimental studies have been aimed at elucidating photofragmentation and chemical reaction dynamics of vibrationally quantum state selected molecules. As a result of its small size, large vibrational spacings, and relatively convenient access to high overtone absorption bands (i.e., $v_{\text{OH}} = 3, 4, \text{ and } 5$) with near-IR and visible dye lasers, H$_2$O and its isotopomers have been a focus of significant attention. Of particular relevance has been the highly localized versus delocalized nature of the OH stretch vibrational levels in HOD, which has made it an especially attractive candidate for experimental and theoretical studies of vibrationally mode specific reaction dynamics. Indeed, as beautifully demonstrated in the Crim,$^1$-4 Rosenwaks,$^5$-7 and Zare$^8$ groups, vibrational excitation of HOD has been used to control which bond is broken by subsequent UV photolysis$^{1,5-8}$ as well as to manipulate bond specific reaction probabilities.$^{2-4}$
Despite the elegant dynamical studies performed on vibrationally excited HOD, until recently surprisingly little was known about its high-resolution overtone spectroscopy. There have been far-IR and microwave studies of HOD in the ground vibrational state\(^9\) as well as near-IR studies of HOD in the fundamental region that have analyzed single-quantum (i.e., \(\nu_{\text{OH}}, \nu_{\text{OD}}\)) excitation from the ground to first excited OH or OD stretching states.\(^{10}\) However, there have been no rotationally resolved studies on HOD excited beyond \(\nu_{\text{OD}} = 2\), and, until fairly recently, no rotationally analyzed overtone studies whatsoever in the pure OH stretch manifold. The difficulty of such a rotational analysis is easily appreciated, due to the large rotational constants, anomalous centrifugal effects, and widely spaced, irregular level patterns of a highly asymmetric top. These issues are further exacerbated in light hydrides such as HOD by the anomalously large changes in rotational constants with OH vibrational excitation.

This absence of high overtone data on HOD has recently been changed by efforts from several directions. The first is an overtone study by Bykov \textit{et al.} on the \(3\nu_{\text{OH}}\) and \(5\nu_{\text{OH}}\) bands of HOD obtained via intracavity laser spectrometer and optoacoustic dye laser spectrometer, respectively.\(^{11}\) This study determined vibrational origins and rotational constants for both bands, with a frequency precision of 0.03 cm\(^{-1}\) for \(3\nu_{\text{OH}}\). However, as a prerequisite to vibrationally mediated photolysis studies of HOD\(^{12}\) and HOD-containing clusters\(^{13}\) under supersonic jet conditions, we have more recently performed a high-resolution overtone study in our laboratory on the \(3\nu_{\text{OH}}\) band of HOD. This study, obtained by photoacoustic detection in a room-temperature cell with an injection-seeded optical parametric
oscillator, was performed to determine rovibrational frequencies for $3\nu_{\text{OH}}$ transitions out of the ground (i.e., $J_{K_aK_c} = 0_00$) rotational state with greater precision.

In addition to this work, high-resolution OH stretch overtone data on HOD via H + HOD “action” spectra and photoacoustic spectra for $4\nu_{\text{OH}}$ has been obtained by Crim and co-workers, for which a rotational analysis has not previously been attempted. The successful completion of our work in the $3\nu_{\text{OH}}$ region stimulated us to rotationally analyze this unassigned $4\nu_{\text{OH}}$ data. In the meantime, vibrationally mediated photolysis studies on HOD in the $4\nu_{\text{OH}}$ region have been reported by Brouard and Langford\textsuperscript{14} in which the primary aim was toward characterizing the detailed OD photofragment distributions from photolysis of quantum-state-selected HOD. Nevertheless, the work clearly necessitated sufficient understanding of the $4\nu_{\text{OH}}$ rotational structure to label the HOD quantum states, which allowed estimates of the band origin and rotational constants to be obtained. However, as some of these results differ substantially from the present analysis, a more detailed spectroscopic investigation of the HOD $4\nu_{\text{OH}}$ overtone band is still warranted. Thus, the detailed analysis of both our $3\nu_{\text{OH}}$ spectra and the $4\nu_{\text{OH}}$ data of the Crim group forms the initial thrust of this chapter.

The second area addressed in this chapter is the alignment of the vibrational overtone transition dipole moment vector with respect to the HOD molecular framework. This proves to be a surprisingly subtle issue, one whose resolution is quite sensitive to the topology of the potential energy and dipole moment surfaces. For example, if we think in terms of a simple “bond-dipole” model for a purely localized vibration, the transition dipole moment vector would be aligned perfectly
along the axis of the vibrating bond. Conversely, if electrical anharmonicity effects lead to a redistributed charge distribution with nuclear displacement, the transition dipole moment vector can be rotated significantly away from the bond axis by an amount which depends on the degree of overtone excitation. Clever experimental techniques for study of such vibrational-transition-moment anisotropies have been developed for large organic molecules aligned in stretched films. However, this information has proven challenging to obtain for much smaller species such as water, which rotate nearly freely and therefore cannot be effectively aligned by the film. A more traditional alternative is via rotationally resolved spectroscopy of these species in the gas phase. Specifically, this information can be extracted by measuring the fractional a-, b-, and c-type character of each vibrational band, which from a rigid asymmetric top model determines where the transition moment lies relative to the principal inertial axes of the molecule. Consequently, with rotationally resolved data for the OH stretch ($\nu_{OH}$, $3\nu_{OH}$, and $4\nu_{OH}$) series in HOD, one can not only determine the direction of this transition moment vector but also probe how that vector changes as a function of OH vibrational excitation. This is of particular interest for such fundamental species as water, where high quality \textit{ab initio} dipole moment and potential energy surfaces exist which can be used with exact 3D quantum variational calculations for rigorous comparison with experiment.

The remainder of this chapter is organized as follows. Section 2.2 briefly reviews the experimental apparatus for $3\nu_{OH}$ and $4\nu_{OH}$ photoacoustic spectroscopy of HOD. In Sect. 2.3, the results from the $3\nu_{OH}$ analysis are used to facilitate rotational assignment of the $4\nu_{OH}$ overtone spectrum of HOD of Crim and co-workers, and
relative a- and b-type band intensities are determined for the $\nu_{OH}$, $3\nu_{OH}$ and $4\nu_{OH}$ overtone series. These intensity ratios probe the vibrational dependence of the transition dipole moment vector and are used in Sect. 2.4 to test theoretical models of the H$_2$O dipole moment surface. The conclusions of this chapter are summarized in Sect. 2.5.

### 2.2 Experimental

The source of light for the $3\nu_{OH}$ photoacoustic signals is a single-mode optical parametric oscillator (OPO) generating narrow-bandwidth infrared radiation, which is described elsewhere.$^{16}$ Briefly, the tripled output at 355 nm of an injection-seeded, pulsed Nd:YAG laser is used to pump two $\beta$-barium borate (BBO) crystals in a four-mirror ring resonator to generate “signal” and “idler” beams via parametric amplification. The ring resonator configuration is exploited by injection seeding the OPO cavity with a tunable, single-mode cw dye laser prior to the UV pump, which therefore generates near Fourier transform limited, tunable output ($3.5$ ns, $\Delta\nu = 160$ MHz) for both signal and idler pulses. Day-to-day reproducibility and frequency stability at the MHz level$^{17}$ for the single-mode 355 nm pump source is maintained by servo loop locking the injection seed for the Nd:YAG laser fundamental to a stabilized optical transfer cavity,$^{18}$ which is locked to a polarization-stabilized HeNe laser.$^{19}$ Based on the stability of the optical transfer cavity, frequency differences can be routinely measured to a precision of better than a few ten-thousandths of a cm$^{-1}$ over several hundred cm$^{-1}$, which is far narrower than the Doppler broadened line width for HOD at room temperature ($\Delta\nu_{\text{FWHM}} \approx 0.030$ cm$^{-1}$). The spectral precision

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of these measurements is quantitatively verified by comparison with well-known HITRAN $|03\rangle \rightarrow \text{H}_2\text{O}$ overtone transitions$^{20,21}$ simultaneously observed in the photoacoustic cells.

For the $4\nu_{\text{OH}}$ band work, a similar photoacoustic cell arrangement is used in the Crim group but with a conventional pulsed dye laser operating in the $13,750$ cm$^{-1}$ region. The bandwidth of the dye laser is $0.05$ cm$^{-1}$, which is now in excess of room temperature Doppler widths for HOD. This multimode dye laser has the considerable advantage over the single mode OPO light source of being able to scan relatively quickly over the entire photoacoustic spectrum. However, the corresponding disadvantage is a much lower overall accuracy of frequency measurement. Consequently, the dye laser wavelength scan has been calibrated to $56 |04\rangle \rightarrow \text{H}_2\text{O}$ overtone transitions embedded in the photoacoustic spectrum, based on the H$_2$O transition frequencies reported in the HITRAN database.$^{20,21}$ It is worth noting that this calibration plot is quite linear but shifted by nearly $10$ cm$^{-1}$ from values obtained simply from wavelength readings on the tuning mechanism. Left uncorrected, this would lead to errors of comparable magnitude in the least-squares fit band origins, with smaller but also significant effects on the reported rotational constants. This suggests the dye laser calibration to be the predominant reason for the significant discrepancies between the recently reported spectroscopic values of Brouard and Langford$^{14}$ and our current results from the calibrated $4\nu_{\text{OH}}$ photoacoustic data. From the scatter in this calibration, the frequency precision of the dye laser is estimated to be $2\sigma = 0.07$ cm$^{-1}$, dominated by residual nonlinearity in the dye laser wavelength scan.
These light sources (either the pulsed OPO or dye laser output) are then sequentially passed through two photoacoustic cells, the first containing 10 Torr of pure H$_2$O, the second containing 10 Torr of a mixture of H$_2$O/HOD/D$_2$O in a near-stoichiometric 1:2:1 ratio. Photoacoustic signals from each cell are simultaneously digitized via sample and hold circuits and recorded as a function of frequency. Transitions for both pure HOD $3\nu_{\text{OH}}$ and $4\nu_{\text{OH}}$ are readily identified by comparison between spectra recorded for the two cells. Absolute frequencies are obtained by calibration against H$_2$O second and third overtone transitions in this spectral region tabulated in the HITRAN database.$^{20,21}$

2.3 Results

2.3.1 HOD: $3\nu_{\text{OH}}$

The transition frequencies, rotational assignment and asymmetric top spectral fits of the $3\nu_{\text{OH}}$ band of HOD are obtained in the following way. In order to minimize the effects of centrifugal distortion, it is useful to restrict the photoacoustic scans to regions corresponding to low $J_{K_aK_c}$. The initial search is guided by theoretical calculations by Tennyson and co-workers$^{22}$ on the H$_2$O potential surface of Polyansky et al.$^{23}$ which predict a $3\nu_{\text{OH}}$ band origin at 10632.5 cm$^{-1}$. Due to the light H/D masses, one must contend with an anomalously large vibrational dependence of the A, B, and C rotational constants, which can be estimated for $\nu_{\text{OH}} = 3$ by linear extrapolation from the ground and $\nu_{\text{OH}} = 1$ rotational constants. A simulated asymmetric top spectrum for the $3\nu_{\text{OH}}$ band generated from these predictions enables the search to be constrained to maxima in the P and R branch regions at low $J_{K_aK_c}$,
which proves sufficiently reliable to make initial rotational assignments of the overtone spectra. These assignments are then rigorously confirmed by ground-state combination differences with the microwave data of De Lucia et al.,\textsuperscript{9} which also agree to within 100 MHz, i.e., <10% of the Doppler broadened line widths (\(\Delta v_{\text{Doppler}} \approx 1 \, \text{GHz}\)) observed in a room temperature photoacoustic cell. A summary of the low \(J_{\text{KaKc}}\) transitions (\(J<5\)) observed and assigned in the P-branch (10631-10656 cm\(^{-1}\)) and R-branch (10680-10690 cm\(^{-1}\)) regions are reported in Table 2.1.

The \(3\nu_{\text{OH}}\) spectral data for HOD have been analyzed by least squares fitting to a Watson\textsuperscript{24} asymmetric top Hamiltonian (A-type reduction, \(I'\) representation), including up to quartic centrifugal distortion terms; the results are summarized in Table 2.2. The resulting simulation of the HOD spectrum in this region, shown in Fig. 2.1c, agrees essentially quantitatively in position and intensity with the observed transitions in Fig. 2.1.a. As unambiguous confirmation of this rotational assignment, we have performed vibrationally mediated photodissociation studies of HOD in supersonic jets, where by virtue of supersonic cooling the spectrum collapses to a \textit{single} \(3\nu_{\text{OH}}\) \(1_{01} \leftarrow 0_{00}\) transition out of the \(0_{00}\) ground rotational state.\textsuperscript{12} Of special note, Tennyson’s prediction\textsuperscript{22} of the HOD band origin is within 0.8 cm\(^{-1}\) of the experimental result, which provides strong quantitative confirmation of the Polansky potential surface\textsuperscript{23} for \(\text{H}_2\text{O}\). Furthermore, this \(3\nu_{\text{OH}}\) data set allows quite reliable extrapolation to the \(4\nu_{\text{OH}}\) overtone manifold, permitting detailed rotational assignment of the third overtone OH stretch HOD data of Crim and coworkers. To facilitate comparison with fits of other OH stretch transitions of HOD, these fits have
Table 2.1. Observed $3\nu_{\text{OH}}$ transitions out of low-J$_{\text{KaKc}}$ states in HOD via high-resolution photoacoustic spectroscopy.

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<th>$J'$</th>
<th>$K_a'$</th>
<th>$K_c'$</th>
<th>$J''$</th>
<th>$K_a''$</th>
<th>$K_c''$</th>
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</table>

$^a$ Numbers in parentheses are residual differences from predicted transition frequencies from the fit.

$^b$ Blended peak; weight = 0.1 in fit.
Table 2.2. HOD $v_{\text{OH}=3}$ spectroscopic constants from centrifugally distorted asymmetric top least-squares fit (in cm$^{-1}$).

<p>| | | | |</p>
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<td>20.3873(24)$^a$</td>
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<td></td>
</tr>
<tr>
<td>B</td>
<td>9.0739(7)</td>
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</tr>
<tr>
<td>C</td>
<td>6.1667(7)</td>
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<td></td>
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<tr>
<td>$\Delta_J$</td>
<td>4.81(13)$\times$10$^{-4}$</td>
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<td></td>
</tr>
<tr>
<td>$\Delta_{JK}$</td>
<td>0$^b$</td>
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<td></td>
</tr>
<tr>
<td>$\Delta_K$</td>
<td>1024(24)$\times$10$^{-2}$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\delta_J$</td>
<td>1.69(15)$\times$10$^{-4}$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\delta_K$</td>
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<tr>
<td>$\nu_0$</td>
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</tr>
<tr>
<td>$\sigma_{\text{fit}}$</td>
<td>0.0017</td>
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</table>

$^a$ Uncertainties represent two standard deviations from least-squares fit.

$^b$ Zero within uncertainty and thus constrained to be zero.
**Figure 2.1.** Sample high-resolution photoacoustic scan over the $3\nu_{\text{OH}}$ overtone region in (a) H$_2$O and (b) H$_2$O, HOD and D$_2$O (≈1:2:1) photoacoustic cells. Transitions present in only the mixed isotope cell are due exclusively to HOD (and enhanced five-fold for visual clarity). (c) The results of a least squares fit to an asymmetric top Watson Hamiltonian are shown for HOD $3\nu_{\text{OH}}$ in the lowest panel.
been repeated with parameters limited to the lowest order A, B, and C constants and a vibrational origin. The results of such a rigid asymmetric top fit of HOD for $3\nu_{OH}$ are listed in Table 2.3.

For a rigid asymmetric top, the ratio of a-type, b-type, and c-type band intensities is determined by the square modulus of the transition dipole moment component along the corresponding inertial axes of the molecule. For $3\nu_{OH}$-excited HOD, only a-type and b-type transitions are observed, consistent with a transition moment in the plane of the molecule. To specify the intramolecular alignment of the in-plane transition moment, integrated a-type and b-type line strengths are measured and compared with predicted line intensities from the Watson Hamiltonian. Averaged over all line strengths measured, the $3\nu_{OH}$ second overtone band of HOD corresponds to an a-type/b-type ratio of 2.7(10):1, where the uncertainty represents two standard deviations.
Table 2.3. HOD spectroscopic constants\(^a\) (in cm\(^{-1}\) unless otherwise noted) from rigid rotor fits to \(A_v\), \(B_v\), \(C_v\).

<table>
<thead>
<tr>
<th></th>
<th>(v_{OH})</th>
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<tbody>
<tr>
<td></td>
<td>0(^b)</td>
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<tr>
<td>(A_v)</td>
<td>23.256(95)</td>
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<tr>
<td>(B_v)</td>
<td>9.084(36)</td>
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<td>(C_v)</td>
<td>6.398(29)</td>
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<tr>
<td>(v_0) ((v\leftarrow 0))</td>
<td>3707.32(9)</td>
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<tr>
<td>(\Delta_v) ((\text{amu}\cdot\text{Å}^2))</td>
<td>0.054(15)</td>
</tr>
<tr>
<td>(\sigma_{\text{fit}})</td>
<td>0.10</td>
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\(^a\) Uncertainties represent two standard deviations obtained from the least-squares fit.
\(^b\) Fit to \(J \leq 5\) data of De Lucia et al.\(^9\)
\(^c\) Fit to \(J \leq 5\) data of Benedict et al.\(^10\)
\(^d\) From Brouard and Langford.\(^14\)
\(^e\) Predictions by Tennyson and coworkers based on the Polyansky et al. potential surface.\(^23\)
2.3.2 HOD: $4\nu_{\text{OH}}$

Scans over the $4\nu_{\text{OH}}$ band have been obtained by tandem photoacoustic spectroscopy in cells containing i) H$_2$O and ii) isotopically mixed H$_2$O/HOD/D$_2$O. Since pure D$_2$O absorptions in this region correspond to even higher ($\Delta v_{\text{OD}} = 5$) overtone excitation$^{10}$ and can be neglected, comparison of the two spectra readily permits contributions from H$_2$O and HOD to be identified separately. Sample data for H$_2$O and HOD overtone absorptions in the $4\nu_{\text{OH}}$ region from the H$_2$O and the H$_2$O/HOD/D$_2$O photoacoustic cells are shown in Fig. 2.2a, demonstrating relatively clean rotational resolution of the H$_2$O and HOD overtone signals. The region scanned is between 13760 cm$^{-1}$ and 13858 cm$^{-1}$, which from our rotational assignment covers most of the P branch and the Q branch up to and including the H$_2$O vibrational origin.

The analysis of the $4\nu_{\text{OH}}$ spectra for HOD follows an identical strategy to the $3\nu_{\text{OH}}$ band. However, with $\nu_{\text{OH}} = 0, 1$ and 3 manifolds rotationally characterized, considerably less uncertainty exists in the extrapolation procedure. Specifically, linear extrapolations of the principal rotational constants for $\nu_{\text{OH}} = 0, 1$, and 3 produce excellent predictions for $A_4$, $B_4$, and $C_4$. Similarly, a Birge-Sponer extrapolation of the $\nu_{\text{OH}}$ and $3\nu_{\text{OH}}$ band origins yields the necessary information to estimate the $4\nu_{\text{OH}}$ band origin. Unlike the previous analysis of $3\nu_{\text{OH}}$, the much smaller extrapolation up to $4\nu_{\text{OH}}$ is now sufficiently accurate to demonstrate an immediate and unambiguous correspondence between predicted and experimentally determined spectra. Based on this simulation, preliminary rotational assignments for the low-$J_{KaKc}$ transitions are readily made and rigorously confirmed by ground state combination differences.
Figure 2.2. Sample of the photoacoustic spectra in the $4\nu_{OH}$ overtone region of the OH stretch for (a) H$_2$O and (b) H$_2$O/HOD/D$_2$O ($\approx$1:2:1) cells. Transitions present in only the H$_2$O/HOD/D$_2$O cell are exclusively from HOD. (c) Simulation of the HOD spectrum using A, B, and C rotational constants and vibrational origin obtained from a least-squares fit of a Watson asymmetric top Hamiltonian to the transitions in Table 2.4. The constants from the fit are given in Table 2.5.
This procedure quickly leads to a complete rotational assignment of HOD transitions in the spectral region scanned. The measured HOD $4\nu_{\text{OH}}$ overtone absorption frequencies and rotational assignments are provided in Table 2.4.

By analogy to analysis of the $3\nu_{\text{OH}}$ overtone band, these transitions are least-squares fit to a Watson asymmetric top Hamiltonian ($I_\text{r}$ representation) including up to quartic terms. While the frequency precision is lower than for $3\nu_{\text{OH}}$, the transitions are fit by these parameters to within $2\sigma = 0.09 \text{ cm}^{-1}$ (see Table 2.5). The quality of fit is demonstrated in Fig. 2.2b and c, comparing a $9 \text{ cm}^{-1}$ section of the photoacoustic spectrum with the least-squares prediction. As with the $3\nu_{\text{OH}}$ band, the $J \leq 5$ transitions are also fit to a rigid rotor Hamiltonian, with the results given in Table 2.3.

Also reported in Table 2.5 are the $4\nu_{\text{OH}}$ band origin predictions from Tennyson and co-workers, as well as the previous estimates of the $4\nu_{\text{OH}}$ band origin and rotational constants from Brouard and Langford. Note that the agreement between theoretical and experimental band origins is extremely good, to within $0.1 \text{ cm}^{-1}$. Conversely, there is $8.7-\text{cm}^{-1}$ discrepancy between our results and the previously reported values of Brouard and Langford. As anticipated, the agreement between current and previous values is far better for the rotational constants, though there still are appreciable discrepancies outside our experimental uncertainties for A and B. Again, given the significant differences in our own work between uncorrected dye laser readings and the HITRAN database for the $4\nu_{\text{OH}} \text{H}_2\text{O}$ lines, it is apparent that independent calibration of the dye laser scan is absolutely essential in obtaining accurate transition frequencies.
Table 2.4. Observed $4\nu_{OH}$ transitions in HOD.

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<tr>
<th>$J'$ $K_{a}'$ $K_{c}'$</th>
<th>$J''$ $K_{a}''$ $K_{c}''$</th>
<th>$\nu$ (cm$^{-1}$)</th>
<th>$J'$ $K_{a}'$ $K_{c}'$</th>
<th>$J''$ $K_{a}''$ $K_{c}''$</th>
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Table 2.4. Observed $4\nu_{\text{OH}}$ transitions in HOD. (continued)

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<th>$K_{c}''$</th>
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<td>1</td>
<td>2</td>
<td>13810.63(-2)</td>
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<td>1</td>
<td>2</td>
<td>1</td>
<td>2</td>
<td>13857.27(4)</td>
</tr>
</tbody>
</table>

\(^a\) Numbers in parentheses are residual differences from predicted transition frequencies from the fit.
Table 2.5. HOD $4\nu_{\text{OH}}$ spectroscopic constants\textsuperscript{a} (in cm\textsuperscript{-1}).

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
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</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>19.443(9)</td>
</tr>
<tr>
<td>B</td>
<td>9.054(8)</td>
</tr>
<tr>
<td>C</td>
<td>6.094(4)</td>
</tr>
<tr>
<td>$\Delta_J$</td>
<td>$3.5(18)\times10^{-2}$</td>
</tr>
<tr>
<td>$\Delta_{JK}$</td>
<td>$5(8)\times10^{-2}$</td>
</tr>
<tr>
<td>$\Delta_K$</td>
<td>$8.7(9)\times10^{-1}$</td>
</tr>
<tr>
<td>$d_J$</td>
<td>$1.9(14)\times10^{-2}$</td>
</tr>
<tr>
<td>$d_K$</td>
<td>$2(17)\times10^{-2}$</td>
</tr>
<tr>
<td>$\nu_0$</td>
<td>13853.636(28)</td>
</tr>
</tbody>
</table>

\textsuperscript{a} Uncertainties represent two standard deviations obtained from the least-squares fit.
Of special relevance to the direction of the overtone transition dipole moment in HOD, the ratio of a-type to b-type intensities is determined from the photoacoustic scans to be 6.7(5):1. It is worth noting that this ratio is more than twice as large as the 2.7(10):1 value observed for $3\nu_{OH}$, thus indicating significant changes in the alignment of the transition dipole moment vector with OH stretch excitation. We will return to this point later in the discussion section.

2.4 Discussion

2.4.1 OH stretch dependence of HOD rovibrational constants

The vibrational dependence of the rotational constants can be most simply characterized by a low-order Dunham expansion in the OH stretch quantum, i.e.,

\[
\begin{align*}
A_v &= A_e + \alpha_e^A (v_{OH} + \frac{1}{2}) \\
B_v &= B_e + \alpha_e^B (v_{OH} + \frac{1}{2}) \\
C_v &= C_e + \alpha_e^C (v_{OH} + \frac{1}{2})
\end{align*}
\]

(2.1a)

(2.1b)

(2.1c)

As shown in Fig. 2.3a, the data quantitatively corroborate a linear dependence on $v_{OH}$. These Dunham expressions can be extrapolated to the OH vibrational minimum at $v_{OH} = -\frac{1}{2}$; the corresponding “equilibrium” HOD rotational constants (corrected for zero-point motion in the OH stretch coordinate only) and values for $\alpha_e^A$, $\alpha_e^B$, and $\alpha_e^C$ are listed in Table 2.6. Note the anomalously large sensitivity of $A_v$ to $v_{OH}$, decreasing by nearly 20% from $v_{OH} = 0$ to $v_{OH} = 4$. The results of these rotational
Figure 2.3. Rotational constants and vibrational origins obtained from least-squares fits of a rigid-rotor Watson asymmetric top Hamiltonian to ground-state data and $v_{OH}$, $3v_{OH}$, and $4v_{OH}$ transitions in HOD (see Table 2.3).  (a) Least-squares fits of a low-order Dunham expansion (Eqns. 2.1a-c) to $A_v$, $B_v$, and $C_v$ reveal the strong linear dependence of these rotational constants on OH vibrational quantum.  Note in particular the $\approx 20\%$ change in $A_v$ from $v_{OH} = 0$ to 4.  (b) The $v_{OH}$, $3v_{OH}$, and $4v_{OH}$ vibrational origins are fit to a Birge-Sponer expression $(v_0 / v_{OH}) = -(\omega_e x_e)v_{OH} + (\omega_e - \omega_e x_e)$.  The linearity of this plot indicates near Morse oscillator behavior in the OH stretch of HOD.  The “equilibrium” rotational constants (corrected for zero-point motion of OH only), $\alpha_e$‘s, harmonic frequency $\omega_e$, and vibrational anharmonicity $\omega_e x_e$ obtained from these fits are given in Table 2.6.
Table 2.6. HOD Dunham coefficients\textsuperscript{a} (in cm\textsuperscript{-1}) for OH stretch excitation.

<p>| | |</p>
<table>
<thead>
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<tr>
<td>$A_e$</td>
<td>23.749(12)</td>
</tr>
<tr>
<td>$B_e$</td>
<td>9.092(3)</td>
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<tr>
<td>$C_e$</td>
<td>6.435(3)</td>
</tr>
<tr>
<td>$\alpha^A_e$</td>
<td>0.9751(41)</td>
</tr>
<tr>
<td>$\alpha^B_e$</td>
<td>0.0141(10)</td>
</tr>
<tr>
<td>$\alpha^C_e$</td>
<td>0.0772(11)</td>
</tr>
<tr>
<td>$\omega_e$</td>
<td>3869.9(19)</td>
</tr>
<tr>
<td>$\omega_e x_e$</td>
<td>81.4(6)</td>
</tr>
</tbody>
</table>

\textsuperscript{a} Uncertainties represent two standard deviations obtained from the least-squares fit.
analyses can also be stated in terms of inertial defect \( \Delta = I_C - I_B - I_A \), which for a rigid planar molecule should essentially vanish. As listed in Table 2.3 for \( \nu_{OH}=0 \) to 4, the inertial defects for HOD are consistently \( \approx 0.05 \) amu\( \cdot \)\( \text{Å}^2 \) and yet all slightly positive due to large amplitude in-plane zero-point vibrational motion\(^{25,26} \).

The series of HOD band origins for \( \nu_{OH} \) can be fit to the standard Birge-Sponer expression

\[
E_v = \omega_e (\nu_{OH} + \frac{1}{2}) - \omega_e \chi_e (\nu_{OH} + \frac{1}{2})^2
\]  (2.2)

to obtain harmonic frequencies and vibrational anharmonicities. A corresponding Birge-Sponer plot of the \( \nu_{OH} \), \( 3\nu_{OH} \), and \( 4\nu_{OH} \) band origins given in Table 2.3 and shown in Fig. 2.3b yields \( \omega_e = 3869.9(19) \) cm\(^{-1} \) and \( \omega_e \chi_e = 81.4(6) \) cm\(^{-1} \) (see Table 2.4). For a simple 1D Morse oscillator model of the OH stretch vibration, the equilibrium bond strength, \( D_e \), is related to the vibrational anharmonicity by \( \omega_e \chi_e = \omega_e^2/(4D_e) \). This translates into an equivalent Morse oscillator dissociation energy of \( D_0 \approx D_e - \frac{1}{2}\omega_e = 126(3) \) kcal/mol, in reasonable agreement with the experimental \( D_0 \) value for H\(_2\)O of 119(1) kcal/mol\(^{27} \).

### 2.4.2 Intramolecular alignment of the transition dipole moment vector

The relative a-type to b-type intensity ratios for \( 3\nu_{OH} \) and \( 4\nu_{OH} \) are 2.7(10):1 and 6.7(5):1, respectively. These values can be further augmented by data from Benedict et al. for \( \nu_{OH} \),\(^{10} \) which yield an a-type to b-type ratio of 1.4(1):1. These data clearly indicate a strong dependence of intensity ratios, and thus the intramolecular
alignment of the HOD transition dipole moment vector, on OH vibrational quanta. Our analysis proceeds as follows. For sufficiently small amplitude vibrations, vibrational and rotational motion can be approximately decoupled; in this limit, the transition dipole moment vector is defined by

$$\tilde{M}_{v',v''} = \langle v' | \tilde{\mu}(\tilde{R}) | v'' \rangle$$  \hspace{1cm} (2.3)

In Eqn. 2.3, $\tilde{\mu}(\tilde{R})$ is the dipole moment operator, $\tilde{R}$ represents all internal displacement coordinates, and thus $\tilde{M}_{v',v''}$ is solely a function of initial ($v''$) and final ($v'$) vibrational state. For vibrational excitation in a triatomic asymmetric top such as HOD, this transition dipole moment vector lies in the molecular plane and therefore supports “hybrid” a- and b-type bands. The fractional intensity of each type is determined by the angle between the transition moment and the a and b inertial axes, respectively. Figure 2.4 depicts the location of these inertial axes as referenced to the HOD equilibrium geometry.

In terms of $\tilde{M}_{v',v''}$, the fractional a-type or b-type intensities of a vibrational band can be written as

$$I_{a/b} = \frac{| \tilde{M}_{v',v''} \cdot (\tilde{a} / \tilde{b}) |^2}{| \tilde{M}_{v',v''} \cdot \tilde{a} |^2 + | \tilde{M}_{v',v''} \cdot \tilde{b} |^2}$$  \hspace{1cm} (2.4)

where $\tilde{a}$ and $\tilde{b}$ are unit vectors along the a and b axes. This expression can be more
Figure 2.4. Diagram of the alignment of the transition dipole moment, $\tilde{M}_{v'-v''}$, in the plane of the HOD molecule. The geometry of HOD with respect to the $a$ and $b$ axes of the molecule is determined from the equilibrium bond lengths and bond angles given by Benedict et al.\textsuperscript{10} The angle $\theta_{v'-v''}$ between $\tilde{M}_{v'-v''}$ and the OH bond is listed in Table 2.7 for the OH vibrational series $\nu_{OH}$, $3\nu_{OH}$, and $4\nu_{OH}$.

conveniently rewritten in terms of experimentally measured $a$-type to $b$-type intensity ratios as

$$
\frac{I_a}{I_b} = \frac{\left| \tilde{M}_{v'-v''} \cdot \tilde{a} \right|^2}{\left| \tilde{M}_{v'-v''} \cdot \tilde{b} \right|^2} = \frac{\cos^2 \theta_a}{\cos^2 \theta_b} = \cot^2 \theta_a \tag{2.5}
$$

where $\theta_a$ and $\theta_b$ are the angles between $\tilde{M}_{v'-v''}$ and the $\tilde{a}$ and $\tilde{b}$ axes, with $\theta_a + \theta_b = \pi/2$. Based on the known HOD equilibrium geometry\textsuperscript{10} and $\theta_a$ determined from Eqn. 2.5, the angle between the transition dipole moment vector and the vibrationally
excited OH bond is given by $\theta_{v',v''} = 59^\circ - \theta_a$ (see Fig. 2.4). Table 2.7 summarizes the results for the series of OH stretch overtone transitions. Interestingly, $\vec{M}_{v',v''}$ does not lie along the OH bond, i.e., $\theta_{v',v''} \neq 0$. Furthermore, there is a clear counterclockwise rotation of the transition dipole moment away from the OH bond with increasing vibrational excitation.

**Table 2.7.** Experimental and theoretical angle between the transition dipole moment and the OH bond.

<table>
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<tr>
<th>Band</th>
<th>2D, bond-dipole</th>
<th>2D, dipole surface</th>
<th>3D, dipole surface</th>
<th>Experiment</th>
</tr>
</thead>
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<tr>
<td>$\nu_{\text{OH}}$</td>
<td>3°</td>
<td>25°</td>
<td>24(1)°</td>
<td>19(1)°</td>
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<tr>
<td>3$\nu_{\text{OH}}$</td>
<td>1°</td>
<td>31°</td>
<td>29(1)°</td>
<td>28(2)°</td>
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<td>4$\nu_{\text{OH}}$</td>
<td>1°</td>
<td>40°</td>
<td>36(1)°</td>
<td>38(1)°</td>
</tr>
</tbody>
</table>

$^a$ Uncertainties represent two standard deviations obtained from the least-squares fit.

In order to gain physical insight into these trends, we next predict the intramolecular alignment of $\vec{M}_{v',v''}$ at various levels of theory. This requires solving for the wave functions $\Psi_{v'}(\vec{R})$ and $\Psi_{v''}(\vec{R})$ for each vibrational level and choosing a trial form of the dipole moment surface, $\vec{\mu}(\vec{R})$. The transition dipole moment $\vec{M}_{v',v''}$ can then be calculated directly from Eqn. 2.3.

The first approach we explore in an attempt to reproduce the behavior of the experimental transition moment vector is based on a simple linear “bond-dipole”
model of the vibrational excitation. Explicitly, this calculation involves approximating the dipole moment surface of the molecule by placing point charges at each of the atoms (+δ at H and D, -2δ at O) that are not allowed to redistribute with vibrational excitation. Stated simply, this model predicts a purely linear dependence of dipole moment on OH/OD stretch excitation and therefore explicitly neglects contributions from “electrical anharmonicity” in the dipole moment surface. The potential energy surface for nuclear displacements is taken from Polyansky et al.23 The vibrational wave functions on this potential surface are then obtained by solving for the two-dimensional (2D) OH/OD stretching wavefunctions with the bend coordinate fixed at 104.5°. Such a model includes only the “mechanical anharmonicity” inherent in the OH stretching coordinate and furthermore neglects any mixing between pure stretching excitations and bend-stretch combinations.

As can be seen from Fig. 2.5 and Table 2.7, this calculation qualitatively fails to reproduce the experimental results. Specifically, θ_ν'-ν'' ≈ 0; that is, $\vec{M}_{\nu'-\nu''}$ is predicted to lie nearly along the OH bond for each overtone transition. This behavior is easily understood by examining in more detail the OH/OD stretch nature of this excitation. The dependence of the 2D wave functions on number of OH stretch quanta is shown in Fig. 2.6 from the ground state up to ν_{OH} = 4. These plots show extremely little mixing with the OD stretch coordinate, r_{OD}, consistent with a pure “local-mode” stretch excitation along the OH bond. In this limit, the dipole moment vector $\vec{\mu}(\vec{R})$ can be expanded in a Taylor series in r_{OH} to produce the following
Figure 2.5. Plot of the experimentally and theoretically determined angle of $\tilde{M}_{\nu',\nu''}$ with the OH bond for a series of OH stretch excitations (see Table 2.7). Despite the local-mode nature of the OH stretch excitation, this angle grows to almost 40° for the highest measured vibrational band ($4\nu_{\text{OH}}$). This figure clearly demonstrates the failure of the bond-dipole approximation to reproduce the experimentally determined angles, as well as the near-quantitative agreement between experiment and calculations, which include the dipole surface of water from Gabriel et al.\textsuperscript{30}
Figure 2.6. Plot of the 2D OH/OD stretch wavefunctions for $v_{OH} = 0, 1, 3,$ and 4 calculated on the potential energy surface of H$_2$O from Polyansky et al.$^{23}$ The uniformity in the OD coordinate among OH vibrational levels demonstrates the nearly pure “local-mode” character of the OH stretch in HOD.
expression for the transition moment $\tilde{M}_{v',v''}$:

$$
\tilde{M}_{v',v''} = \mu |_{r_{\text{OH}}=r} \langle v'|v'' \rangle + \frac{d\mu}{dr_{\text{OH}}} |_{r_{\text{OH}}=r} \langle v'| (r_{\text{OH}} - r_{\text{OH}}) |v'' \rangle + \ldots \quad (6)
$$

For anything but a pure rotational transition with $\Delta v=0$, the first term in $\tilde{M}_{v',v''}$ is zero due to orthogonality of the different vibrational wave functions. In the local-mode, bond-dipole approximation, the only nonvanishing contribution to $\tilde{M}_{v',v''}$ arises from $d\mu/dr_{\text{OH}}$. Since only the component of $\mu$ parallel to the OH bond changes with $r_{\text{OH}}$, $\tilde{M}_{v',v''}$ would thus lie parallel to the OH bond, with $\theta_{v',v''} = 0$. These predictions are in clear disagreement with experiment, indicating that a more sophisticated model of the HOD dipole moment surface is necessary. The small but nonvanishing values of $\theta_{v',v''}$ predicted from this model simply reflect weak mixing of OH and OD stretch vibrations due to a perturbative breakdown of the local-mode picture.

A much improved dipole moment surface can be obtained from the \textit{ab initio} work of Gabriel \textit{et al.}\textsuperscript{31} which conveniently provides $\mu(\mathbf{R})$ as an explicit function of intramolecular coordinates. A second set of predictions for the overtone transition moment vector is performed with this alternate dipole surface but still for 2D OH/OD stretch degrees of freedom. Thus, this model incorporates “electrical anharmonicity” in the dipole surface while still neglecting possible coupling between bend and stretch excitations. The results of these calculations are reported in Table 2.7 and plotted in Fig. 2.5. Both the magnitude of $\theta_{v',v''}$ and the vibrationally dependent “tilt” away from the OH bond are now in quite reasonable agreement with experiment. These results provide strong confirmation of the dipole moment surface of Gabriel \textit{et al.} and
indicate that electrical anharmonicity in the H$_2$O dipole moment surface plays the
dominant role in intramolecular alignment of $\vec{M}_{v'-v''}$ in the OH overtone stretch
manifold of HOD.

In principle, there could be additional contributions to this intramolecular
alignment of $\vec{M}_{v'-v''}$ from mixing between HOD bend and OH/OD stretch motion on
the potential energy surface. Indeed, the role of 2:1 Fermi resonant bend-stretch
coupling has proven quite important in theoretical studies of intramolecular
vibrational relaxation (IVR) in overtone CH excited hydrocarbons.$^{31-37}$ Furthermore,
it is conceivable that overall rotation of the HOD molecule can be responsible for an
enhanced Coriolis-induced coupling of the different vibrational modes. As a final
test, therefore, we relax all constraints on vibrational mode mixing by repeating these
HOD calculations in all 3 intramolecular and 3 overall rotational degrees of freedom.
To do this, we use the TRIATOM suite of programs developed by Tennyson et al.$^{38}$
to calculate rovibrational wave functions on the full 3D potential energy surface of
Polyansky et al.$^{23}$ These wave functions are then used with the same dipole moment
surface of Gabriel et al. to predict the series of OH stretch overtone spectra in HOD,
explicitly calculating intensities of $J_{K\alpha K\epsilon}$-resolved HOD rovibrational transitions.
These rovibrational transitions can in turn be readily assigned and their intensities
used to determine the theoretical alignment, $\theta_{v'-v''}$, of the transition moment vector as a
function of OH overtone excitation via Eqn. 2.5. The results in Table 2.7 and Fig. 2.5
demonstrate that this potential and dipole surface also reproduce $\theta_{v'-v''}$ quite
adequately as well as the experimentally observed tilt away from the OH bond with
increasing OH vibrational excitation. However, the agreement is not appreciably
improved from the simpler 2D calculations for the OH stretch manifold, indicating that stretch-bend interactions are not as important as electrical anharmonicity in controlling the alignment of the transition dipole moment vector in HOD.

Finally, with the ab initio dipole moment surface for water, one can now explicitly investigate why the transition moment vector “tilts” away from the OH bond with overtone stretch excitation. This is difficult to represent for a 2D vector quantity as a function of three intramolecular coordinates. However, as one compromise, Fig. 2.7 displays the two nonvanishing orthogonal projections of the full dipole surface i) $\mu_\parallel$ parallel to the OH bond and ii) $\mu_\perp$ perpendicular (but in plane) to the OH bond, where a positive sense of $\mu_\parallel$ and $\mu_\perp$ corresponds to the O-H and $\approx$O-D bond directions, respectively. These two projections are plotted as a function of $r_\text{OH}$, with the OD bond length and HOD bend angle fixed near the equilibrium values. To establish the relevant length scale, the equilibrium OH separation and classical turning points for $v_\text{OH} = 4$ are indicated. In qualitative agreement with the linear bond-dipole model, the component of $\ddot{\mu}$ parallel to the OH bond varies approximately linearly with $r_\text{OH}$, though with some additional curvature at high $r_\text{OH}$. However, in clear contrast to bond-dipole predictions, the corresponding perpendicular component of $\ddot{\mu}$ is far from independent of the OH bond length. Indeed, the magnitude of $\mu_\perp$ decreases by nearly 30% of the increase in $\mu_\parallel$ over the range of $v_\text{OH} = 4$ classical turning points. The latter implies $d\mu_\perp/dr_\text{OH}$ is nonzero, and specifically that the component of $\vec{M}_{v',v}$ perpendicular to the OH bond is nonzero. Consequently, $\vec{M}_{v',v}$ must rotate away from the OH bond, in direct contrast to the bond-dipole picture.
Figure 2.7. Components of the dipole moment surface of HOD (= dipole surface of H₂O from Gabriel et al.⁴⁰) parallel (μ∥) and perpendicular (μ⊥) to the OH bond as a function of rOH, at the equilibrium values of the OD bond length and HOD bend angle. The equilibrium OH bond length and the classical turning points for νOH = 4 are noted. As expected, μ∥ is roughly linear in OH bond displacement for sufficiently small rOH, i.e., consistent with a simple bond-dipole model. However, over the same range of displacements, μ⊥ strongly decreases with rOH, which is in direct contrast with bond-dipole predictions and responsible for counterclockwise rotation of the vibrational transition moment vector (Mv→v') away from the OH bond axis.
As a final note, the combination of Fig. 2.7 and a nearly perpendicular HOD bond angle imply that the component of the dipole moment along the OD bond must be *decreasing* with OH stretch excitation over the range of $r_{\text{OH}} < 1.6 \text{ Å}$. However, this trend must eventually reverse, since in the limit of infinite $r_{\text{OH}}$ separation, $\mu$ asymptotically approaches the dipole moment of isolated OD radical. This would yield $\mu_{\perp} = \sin(104.5^\circ) \cdot 1.65 \text{ D} = 1.60 \text{ D}$, which is substantially larger than the $\approx 1.35 \text{ D}$ value theoretically predicted at $r_{\text{OH}} = 1.6 \text{ Å}$. This behavior further underscores the dramatic importance of electrical anharmonicity in the dipole moment surface and therefore the relevance of detailed comparisons between *ab initio* theory and experiment for such fundamental molecular systems as H$_2$O.

### 2.5 Summary

High-resolution infrared and visible photoacoustic spectroscopy is used to investigate the second and third OH stretch overtone bands of HOD. Rotational analysis of these data permits $A_v$, $B_v$, and $C_v$ rotational constants and vibrational origins to be determined for $v_{\text{OH}} = 3$ and 4. In conjunction with earlier studies of the ground state and first OH stretch excited manifold, the vibrational dependence of these spectroscopic data can be well fit by simple Dunham and Birge-Sponer analyses in $v_{\text{OH}}$. More quantitatively, the $3v_{\text{OH}}$ and $4v_{\text{OH}}$ vibrational origins for HOD (in the Born-Oppenheimer approximation) can be used to test the accuracy of current *ab initio*/empirical potential energy surfaces by Polyansky *et al*. Agreement between experiment and full 3D quantum variational calculations on this surface is excellent: $0.8 \text{ cm}^{-1}$ and $0.1 \text{ cm}^{-1}$ for $3v_{\text{OH}}$ and $4v_{\text{OH}}$, respectively.
Experimental intensities of a-type and b-type transitions within each of the $\nu_{OH}$, $3\nu_{OH}$, and $4\nu_{OH}$ manifolds are analyzed to determine the intramolecular alignment of the transition dipole moment vector. This vector is found to lie significantly away from the OH bond and furthermore “tilts” systematically with increasing OH stretch excitation. These results are in clear contrast with simple bond-dipole model predictions, which for a local-mode excitation would be perfectly aligned along the OH bond, suggesting the importance of electrical anharmonicity in the dipole moment surface. This is explicitly tested by further comparison with predictions from an \textit{ab initio} dipole moment surface of Gabriel \textit{et al.}, which are in excellent qualitative agreement with experimental results. The absence of significant contributions to this transition dipole alignment from bend-stretch rotationally induced vibrational mixing is explicitly tested by comparing 2D OH/OD stretch calculations (i.e., at fixed HOD bend angle) with full QM variational rovibrational calculations (with both 3D vibrational and external rotational motion included). These overtone results underscore the importance of nonlinear effects in the dipole moment surface (i.e., electrical anharmonicity) as the predominant influence on intramolecular alignment of the transition dipole moment vector.


References for Chapter 2


22. Tennyson, J., private communication


CHAPTER 3
OPEN-SHELL CLUSTER FORMATION VIA LASER PHOTOLYSIS:
QUASICLASSICAL TRAJECTORY STUDIES OF
Ar_n-H_2S AND Ar_n-SH CLUSTER DYNAMICS

3.1 Introduction

Over the past decade, the study of radical van der Waals complexes has been the focus of considerable interest. An especially active area in this field has been the study of rare gas-radical hydride cluster species, with particular emphasis on complexes of rare gases such as Ne, Ar, and Kr with OH(OD),^1-22 and SH(SD)^23-28 radicals, which have been mapped out both experimentally and theoretically. Such prototype systems are ideal for developing an understanding of radical solvation and close-range inelastic energy transfer effects, as well as providing the fundamental basis for further studies of radical complexes with reactive species.^1,29-31

Typical preparation methods of such rare-gas/radical clusters involve generation of the radical from an appropriate hydride precursor (e.g., SH/OH from H_2S, H_2O) via UV photolysis or discharge, followed by coexpansion of the radical with the rare-gas partner in a supersonic jet. The spectroscopy and dynamics of these
clusters can then be probed via laser-induced fluorescence (LIF) or resonance-enhanced multiphoton ionization (REMPI) by pumping to rovibrational levels of an excited electronic state, usually many centimeters downstream from the source. High-resolution studies of these vibrationally and rotationally cold clusters have provided a wealth of spectroscopic information about intermolecular potential energy surfaces in the electronically excited-state; a recent example is the development of high quality empirical potential energy surfaces by Miller and coworkers for R-SH complexes (R = Ar, Kr, Ne)\textsuperscript{26,27} out of the first excited (A) state. Such studies do not, however, significantly explore the ground-state cluster potential surface, since the collisional cooling process produces population overwhelmingly in the lowest rovibrational levels. While this cooling clearly aids in the spectroscopic analysis of the excited state, it also limits the range of ground-state quantum states available for dynamical studies. Alternative spectroscopic methods for characterizing the ground-state potential surface have been stimulated emission pumping studies by Lester and coworkers on Ar/Ne-OH\textsuperscript{13,32,33} as well as the dispersed fluorescence studies of Miller and coworkers on Ne-OH\textsuperscript{19} and Ne/Ar/Kr-SH.\textsuperscript{28}

At the same time, a number of studies have been carried out investigating photodissociation dynamics in small clusters. Systems sampled by these techniques include complexes of one or few rare-gas atoms with small molecules, in an effort to link gas-phase photolysis of monomer precursors with photodissociation in solvated environments. These studies raise the intriguing possibility that the photolyzed atom can, in some circumstances, leave behind a bound, highly excited open-shell cluster. Several groups have previously provided indirect experimental evidence for such
products; examples include I-HI from (HI)$_n$ photodissociation$^{34}$ and Ar-I from Ar-HI photodissociation.$^{35}$ Theoretical calculations by Juanes-Marcos and Garcia-Vela of Ar-Cl from Ar-HCl photolysis$^{36,37}$ and Bowman and coworkers of Ar-OH from Ar-H$_2$O have also predicted these open-shell cluster products.$^{38}$

More recently, direct spectroscopic evidence from our group has been presented for the production of bound, rovibrationally excited radical clusters from photolysis of closed-shell precursor clusters.$^{38-40}$ Via this technique, the rare gas and UV chromophore are coexpanded in a slit supersonic jet to form cold, closed-shell clusters. The monomer hydride is then photolyzed within the cluster, the fast H atom escapes with high efficiency, and the resulting radical cluster is probed via LIF. The time delay (typically 100 ns) between photolysis and probe lasers is shorter than the timescale for subsequent collisions in the jet, thus probing strictly unimolecular dynamics for formation of open-shell clusters.

Specifically, this technique has been demonstrated to be an efficient source of hot Ar-SH and Ar$_2$-SH radical clusters from photolysis of Ar-H$_2$S and Ar$_2$-H$_2$S followed by H atom ejection. Since these open-shell clusters are formed with high internal excitation, this in principle opens up a wide range of the ground-state potential surface for detailed investigation. An important preliminary and dynamically intriguing question to address, however, is how such a relatively “violent” photolysis event can produce weakly bound radical clusters so efficiently. Figure 3.1 outlines the key features of this process. Ar$_n$-SH ($n = 1, 2$) clusters are formed from Ar$_{15}$-H$_2$S photolysis via the following sets of pathways:
Figure 3.1. Schematic representation of the production of Ar$_n$-SH (n = 1, 2) clusters from photolysis of Ar$_n$-H$_2$S precursors. Pathways 1 and 3 depict “nonfragmentary” photolysis, in which excess energy is accommodated by the cluster, and pathway 2 depicts a “boil-off” mechanism, in which excess energy is removed by the escape of an Ar atom.

\[
\text{Ar}_n\text{-H}_2\text{S} + h\nu \rightarrow \text{Ar}_n\text{-SH} + \text{H} \quad (3.1)
\]

\[
\text{Ar}_n\text{-H}_2\text{S} + h\nu \rightarrow \text{Ar}_{n-1}\text{-SH} + \text{Ar} + \text{H} \quad (3.2)
\]

Ar$_n$-SH radical clusters are in effect produced by two mechanisms: i) “boil off,” in which one Ar atom escapes to remove excess energy, and ii) “nonfragmentary,” in which this excess energy is successfully accommodated by the remaining radical cluster. Indeed, it is initially surprising that the clusters survive this photolysis process at all: the excess photolysis energy is as much as two orders of magnitude larger than the radical-cluster binding energy in this interaction. The simple
dynamical explanation is that by conservation of momentum, the light H atom can carry off as much as 95% of the photolysis energy. The remaining excess energy from H₂S photolysis is further reduced by transformation into the Arₙ-SH center-of-mass (COM) frame, which further increases the probability that internal energy will not exceed the binding energy of the open-shell cluster.

While simple conservation principles begin to explain how the energy is disposed, several dynamical aspects warrant further investigation. First of all, previous experimental work has provided estimates of the efficiency of each formation process by comparison with LIF signals from SH monomer populations in the jet. However, uncertainty in radiative lifetimes of the monomer and cluster species, as well as the extent of Arₙ-H₂S clustering in the jet, distribute these estimates over approximately an order of magnitude range. Second, we would like to probe the energetics of cluster formation, with particular attention to the “nonfragmentary” photolysis pathways (i.e., where no additional Ar atom is boiled off to stabilize the nascent complex). Experimentally, the dominant features in the cluster LIF spectra have been attributed to intermolecular progressions (e.g. van der Waals stretch and librational modes) out of the lowest vibrational states of Ar-SH and Ar₂-SH. However, this cannot explain the strong intensity peaking at the highest-energy end of the spectrum, which one speculates arise from highly internally excited clusters near the dissociation limit in the ground electronic state. Thus, it is necessary to show that the intracluster photolysis process can produce highly rovibrationally excited (albeit long-lived) molecules, as well as to study how that excess intermolecular energy is distributed. Furthermore, once these hot free-radical clusters
are generated by unimolecular photolysis, they experimentally exhibit a much slower cooling on a 10-µs timescale. It is therefore interesting to determine whether this is a purely due to bimolecular cooling by collisions (which would imply remarkably high energy-transfer efficiencies), or if any *noncollisional* processes (such as unimolecular dissociation of clusters with \( E > D_e \)) might contribute to the decrease in average internal excitation.

In order to address these issues, we have used quasiclassical trajectory calculations to simulate the unimolecular photolysis dynamics in Ar-H\(_2\)S and Ar\(_2\)-H\(_2\)S photolysis. In these simulations, the ground-state Ar\(_n\)-H\(_2\)S wavefunction is used to generate and sample from an appropriate distribution of initial coordinates and momenta. This initial wavefunction is projected (in a Franck-Condon sense) onto an excited-state, repulsive surface on which the photolysis dynamics are calculated. The resulting trajectories allow us to explore the dynamics of H atom photoejection and subsequent stabilization of the open-shell van der Waals cluster. The remainder of this chapter is organized as follows. Section 3.2 describes the details of the computational methodology for generating initial conditions and calculating the photolysis trajectories. Section 3.3 describes the results of these quasiclassical trajectories, including the lifetimes of radical clusters, the energetics and dynamics of cluster formation, and branching ratios among photolysis products. Section 3.4 summarizes the key conclusions of this study.
3.2 Computational Details

3.2.1 Ground-state potential surfaces: Ar\textsubscript{n}-H\textsubscript{2}S(\tilde{X})

In order to generate the initial conditions for Ar\textsubscript{n}-H\textsubscript{2}S and subsequently calculate the photodissociation dynamics, two potential surfaces are required: one for the ground electronic state, Ar\textsubscript{n}-H\textsubscript{2}S(\tilde{X}), and one for the first excited electronic state accessed by the photolysis pulse. Neglecting three-body terms, one could calculate what one needs with only the relevant two n=1 (i.e., Ar-H\textsubscript{2}S) surfaces; unfortunately, neither dimer potential surface is currently available. However, for our current purpose we can obtain a qualitatively correct description of the initial state sampling simply by substituting the V(R,\theta,\phi) Ar-H\textsubscript{2}O potential of Cohen and Saykally(AW2),\textsuperscript{41} where R represents the distance from the Ar atom to the center of mass of the H\textsubscript{2}S (i.e., H\textsubscript{2}O) subunit; \theta, rotation of the Ar in the H\textsubscript{2}S plane; and \phi, Ar rotation out of this plane. In these coordinates, (\theta, \phi) = (0°, 0°) is defined with Ar along the C\textsubscript{2V} axis of the H\textsubscript{2}S, proximal to the H atoms. The minimum energy configuration is located at (R, \theta, \phi) = (3.636 Å, 74.3°, 0°), i.e., rotated 74.3° away from the C\textsubscript{2V} axis in the plane of the H\textsubscript{2}O, with an energy of 143 cm\textsuperscript{-1}. The ground-state wavefunction for this system is highly angularly delocalized with near free rotation in \theta. The sampling for the larger Ar\textsubscript{2}-H\textsubscript{2}S clusters requires an Ar-Ar potential as well. This interaction is described by the semiempirical Ar-Ar interaction potential of Aziz and Chen (HFD-C\textsuperscript{42}), with a well depth of 99.5 cm\textsuperscript{-1} and an equilibrium Ar-Ar distance of 3.759 Å.
3.2.2 Excited-state potential surfaces: Ar$_n$-H$_2$S(A)

In the excited state, the interaction between the Ar and H$_2$S subunits can no longer be approximated by the corresponding Ar-H$_2$O surface, since the dissociative H-SH interaction lies at the heart of the excited-state potential. Furthermore, an intermolecular vibrational SH potential must be included for any dynamics calculations. Since the H$_2$S is thus fragmented into two subunits, the dissociative H atom and the remaining SH radical, the interaction between the Ar and H$_2$S is likewise separated into Ar-SH and Ar-H interactions.

The dissociative potential of the H$_2$S monomer is modeled after the \textit{ab initio} calculations of Theodorakopoulos \textit{et al.} for the lowest dissociative state, the $^1A''$ state.\cite{Theodorakopoulos43} In these calculations, the non-breaking SH bond distance ($r$) and HSH bond angle are fixed at their equilibrium values (2.52 Å and 92.2°), and the excited-state potentials are calculated as a function of the breaking SH bond distance. The lowest adiabatic dissociative state represents two strongly coupled diabatic states ($^1A_2$ and $^1B_1$) crossing near 2.2 $\alpha_0$ and as such is not well modeled by a single exponential fit.\cite{44} To approximate this state, we fit the \textit{ab initio} points outside the crossing region, i.e., those with $r > 2.2 \alpha_0$, to a single exponential. The parameters obtained from this exponential fit are given in Table 3.1. As noted above, this potential is essentially only valid for a fixed non-breaking SH bond distance and HSH bond angle; however, for a rapid photodissociation process, the H atom should depart before any significant SH rotation or vibration occurs. Thus, we calculate this potential based solely on the dissociative SH bond distance. The remaining, nondissociating bond in the H$_2$S
subunit is modeled by a Morse oscillator potential with parameters obtained from Ramsay (see Table 3.1).45

<table>
<thead>
<tr>
<th>Table 3.1. Parameters of the potential.</th>
</tr>
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<tbody>
<tr>
<td>HS-H Dissociation: ( V = A \exp(-B r_{HS-H}) )</td>
</tr>
<tr>
<td>A</td>
</tr>
<tr>
<td>B</td>
</tr>
<tr>
<td>SH Stretch: ( V = D_c (1 - \exp(-\alpha(r-r_e))^2 )</td>
</tr>
<tr>
<td>( r_e )</td>
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<td>( D_c )</td>
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<td>( \alpha )</td>
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No full potential is available for the Ar-SH interaction; we have thus chosen to adapt the spin-orbit averaged Ar-OH potential of Lester, Clary, and coworkers\(^{13}\) by replacing the mass of oxygen with the mass of sulfur. This potential is defined in Jacobi coordinates \((R, \theta)\), with \( R \) as the distance from the Ar to the OH center of mass, and \( \theta \) as the angle between \( R \) and the OH internuclear axis \((\theta = 0^\circ \text{ for H pointed toward the Ar})\). The minimum energy is 127 cm\(^{-1}\) in the linear OH-Ar configuration, and the equilibrium distance between the Ar and the OH center of mass is 3.7 Å. This surface overestimates the binding energy of Ar-SH: \( D_0 \) for Ar-OH is 107 cm\(^{-1}\),\(^3\) while \( D_0 \) for Ar-SH is estimated to be 82 cm\(^{-1}\).\(^24\) In addition, a recent
model potential developed by Yang et al. demonstrates that the Ar-SH ground-state potential is weaker, but more isotropic, than the Ar-OH potential. We thus expect that our calculations may overestimate the number of bound Arₙ-SH clusters formed from Arₙ-H₂S photolysis; however, the effects on the relative efficiencies for Ar-SH and Ar₂-SH production should be less significant. The remaining interaction for Ar-H₂S, i.e., Ar-H, is modeled by the potential of Tang and Toennies.

For Ar₂-H₂S, the Ar-Ar interaction is described by the potential of Aziz and Chen used for the ground electronic surface (Sect. 3.2.1).

**3.2.3 Initial-condition sampling**

The initial conditions for the quasiclassical trajectory calculations are generated in two steps; the first involves sampling the ground-state potential surface in a manner approximately consistent with the ground-state wavefunction. This process is initially detailed for the Ar-H₂S calculations, after which the necessary modifications for the Ar₂-H₂S photolysis simulations are described.

To sample the ground-state potential energy surface also requires a rough estimate of the ground-state zero-point energy. The zero-point energy of Ar-H₂O is 44.65 cm⁻¹ above the potential minimum. In the pseudodiatomic approximation, this energy is proportional to the inverse square root of the reduced mass; thus, we scale the Ar-H₂O zero-point energy by \( \sqrt{\mu_{\text{Ar-H₂O}}/\mu_{\text{Ar-H₂S}}} \) for Ar-H₂S, resulting in an energy eigenvalue of 36.68 cm⁻¹. The zero-point energy for the trimer (Ar₂-H₂S) is estimated as twice that of the dimer (Ar-H₂S), since there are now two such pseudodiatomic modes.
Next, we generate a microcanonical ensemble of relative Ar-H$_2$S positions, i.e., with each initial condition having a total energy equal to this ground-state zero-point energy. Most quasiclassical sampling techniques based on the ground-state eigenfunction typically require first calculating the eigenfunction, then weighting the sampling of coordinates and momenta consistent with the probability distribution. However, for the present purposes, the ground-state potential is quite approximate, thus a more qualitative sampling method will suffice. To that end, we sample the relative positions of the Ar and H$_2$S subunits with a probability that decreases exponentially with potential energy. This distribution mimics the relationship between the ground-state potential energy function and probability distribution of a harmonic oscillator.

For a one-dimensional, quantum-mechanical harmonic oscillator, the ground-state probability distribution is described by

\[ P(R) = \left| \Psi_{\text{H.O.}} \right|^2 = N e^{-\mu \omega R^2 / \hbar} \]  

(3.5)

where $N$ is a normalization constant, $\mu$ is the reduced mass of the oscillator, and $\omega$ is its vibrational frequency. Since the potential energy of the harmonic oscillator is given by $V(R) = \frac{1}{2} \mu \omega^2 R^2$, and its ground-state energy, $E_{\text{g.s.}}$, is equal to $\hbar \omega / 2$, this probability distribution can be rewritten as

\[ P(R) = N e^{-V(R)/E_{\text{g.s.}}} \]  

(3.6)
with $V(R) = 0$ at the potential minimum. Thus, the probability distribution in coordinate space for a harmonic oscillator is an exponentially decreasing function of the potential energy, with $P$ maximized at the potential minimum and down by a factor of $e$ at the classical turning points (i.e., where $V = E_{g.s.}$). This probability distribution thus reproduces the classically allowed region of a 1D harmonic oscillator and goes to zero in the classically forbidden regions.

In a similar vein, we describe the probability in coordinate space for an Ar at a particular point on the Ar-H$_2$S surface by:

$$P(R, \theta, \phi) = N e^{-V_{Ar-H_2S}(R, \theta, \phi)/E_{g.s.}} \tag{3.7}$$

where $E_{g.s.} = 44.65$ cm$^{-1}$ and $V_{Ar-H_2S}(R, \theta, \phi)$ is the Ar-H$_2$S potential energy. Operationally, we sample the Ar-H$_2$S surface by randomly placing the Ar within a (10 Å)$^3$ box centered on the H$_2$S. If the potential energy at this point is greater than the ground-state eigenenergy, this initial condition is rejected; otherwise, its relative probability is calculated from Eqn. 3.7 (with $N$ fixed to 1), and compared with a random number on the interval [0,1]. If the calculated probability is greater than this random number, this initial position is accepted. A similar procedure is carried out for the Ar$_2$-H$_2$S clusters. Since for two separable harmonic oscillators, the total probability is given by the product of the probabilities for the individual oscillators, the total Ar$_2$-H$_2$S probability is estimated as

$$P = N e^{-\left[\frac{V_{Ar-H_2S} + V_{Ar^2-H_2S}}{E_{g.s.}}\right]/E_{g.s.}} \tag{3.8}$$
where $E_{g.s.}$ is the ground-state energy of a single Ar-H$_2$S interaction. A plot of 500 initial Ar-H$_2$S positions is given in Fig. 3.2. In this plot, $x$ and $y$ are coordinates in the H$_2$S plane defined with respect to its COM: $y$ lies along the C$_{2v}$ axis, with positive $y$ above the S atom, and $z$ is perpendicular to the plane. The maximum density of initial positions peaks at the Ar-H$_2$S minimum, but the spread in points adequately represents the “floppy” nature of the intermolecular potential.

Once the relative Ar-H$_2$S positions, and thus the Ar-H$_2$S potential energy, has been determined, the remaining zero-point energy is placed in kinetic energy relative to the center of mass of the cluster. In the frame of a stationary H$_2$S, the magnitude of this momentum for the single-Ar case is approximately

$$p_{Ar} = m_{Ar} \sqrt{\frac{2 (E_{g.s.} - V_{Ar-H_2S})}{\mu_{Ar,H_2S}}}$$

(3.9)

where $\mu_{Ar,H_2S}$ is the reduced mass of the Ar and H$_2$S subunits. The orientation of the Ar velocity with respect to the H$_2$S subunit is then randomly selected. A plot of this distribution of momenta relative to the H$_2$S is given in Fig. 3.3. For the two-Ar case, the relative orientation of the two momenta also affects total energy in the COM frame. Consequently, the magnitudes and relative orientations of the momenta are randomly sampled up to the maximum value given by Eqn. 3.9. The final momenta are then each scaled such that the resulting kinetic energy in the COM frame is consistent with the chosen zero point and potential energies.
Figure 3.2. Initial condition sampling for the Ar position relative to the H$_2$S subunit for 500 trajectories of Ar-H$_2$S. With respect to the COM of H$_2$S, x and y are in the H$_2$S plane, with positive y above the S atom and along the C$_{2v}$ axis; z is perpendicular to this plane. The sampling probability decreases exponentially with potential energy, so that the maximum density is at the Ar-H$_2$S minimum and the spread in points mimics the “floppy” nature of the intermolecular potential.
Figure 3.3. Initial condition sampling for the Ar momentum relative to the H$_2$S subunit for 500 trajectories of Ar-H$_2$S, with coordinates defined as in Figure 3.2. All excess ground state energy above the Ar-H$_2$S potential energy is placed in Ar momentum, with random orientation with respect to the H$_2$S subunit.
3.2.4 Photoexcitation and trajectory calculations

Once the initial positions and momenta for the Ar and H$_2$S subunits are determined, each initial condition is promoted to the excited-state surface, and the internal energy is adjusted to equal the excess energy from the photolysis. If this process were strictly vertical (in a Franck-Condon sense), the relative positions and momenta of the atoms would be unchanged by the photoexcitation. Simply substituting the ground-state potential with the excited-state potential, however, would not ensure the appropriate excited-state internal energy, i.e., the sum of the initial ground-state and photolysis energies minus the SH bond dissociation energy. Since the part of the $\tilde{A}$-state potential surface most relevant to the photolysis is the dissociative H-SH bond potential, we optimize the dissociative H-SH bond distance so that the total energy in the cluster is equal to the appropriate excited-state internal energy. In effect, this step initially places all of the photoexcitation into potential energy. Two cases are examined: photolysis at 248 nm, which provides 8855 cm$^{-1}$ above the bond dissociation energy, and at 193 nm, which provides 20,300 cm$^{-1}$ of excess energy.

Once the initial conditions are projected onto the excited-state surface in this manner, the photodissociation trajectories are calculated by integrating Hamilton's equations of motion in Cartesian coordinates with a variable-order, variable-stepsize, Adams-method numerical integrator. Trajectories are typically integrated until all Ar-SH distances exceed 20 $a_0$, or until a fixed integration time has elapsed (1 ns for Ar-H$_2$S photolysis, 250 ps for Ar$_2$-H$_2$S). Conservation of energy is verified to be better than one part in $10^6$, more typically in $10^7$, over the duration of each trajectory.
Approximately 500 trajectories are initially calculated for each initial cluster size and photolysis wavelength; additional trajectories are subsequently calculated as detailed in the next section. For each trajectory, the momenta and positions of all atoms are recorded as a function of time, typically in 60-fs steps, for subsequent analysis of product branching ratios, lifetimes of cluster species, energetics of bound clusters, and dynamical pathways.

3.3 Results

Our first step in examining the results of these photolysis trajectory calculations is to determine the timescale on which the radical clusters are formed and fall apart, as well as to take a preliminary look at which species are generated. Next, we analyze the energetics of the radical clusters, first by investigating the overall energy partitioning among the various rotational and vibrational modes of the cluster for the whole product distribution, then by focusing on individual trajectories. This examination leads to a discussion of the dynamics of cluster formation, and more specifically, the role of cluster angular momentum. Finally, we bring these pieces together in order to determine overall product branching ratios for comparison with experimental results.

3.3.1 Time-dependent radical concentrations

We begin the trajectory calculations by examining the 193-nm photolysis of Ar-H$_2$S and Ar$_2$-H$_2$S, for which the simplest picture emerges. The concentrations of radical species as a function of time after photolysis for Ar-H$_2$S and Ar$_2$-H$_2$S
photolysis at this wavelength are depicted in Figs. 3.4a and b. Both calculations converge on this 1-ns timescale: the concentration of each radical species levels off such that little change occurs past the 10-ps mark, i.e., few additional radical clusters would be predicted to fall apart if the calculations were continued for additional time. As seen in Fig. 3.4a, the concentration of bound Ar-SH formed from Ar-H₂S drops dramatically such that by the end of the calculation, little or no bound radical cluster product remains.

In contrast, for Ar₂-H₂S photolysis, a significant amount of Ar-SH remains bound: the calculation levels off with roughly 20% of the trajectories following this pathway. Yet few or no trajectories produce Ar₂-SH product. Taken together, these two calculations demonstrate that for 193-nm photolysis of Ar-H₂S and Ar₂-H₂S, the primary product is Ar-SH, formed from “boiling off” one Ar atom from Ar₂-H₂S photolysis. This result is not surprising: 193-nm photolysis releases 20,300 cm⁻¹ of excess energy; even a dynamical reduction by 20 (≈ M₁₁₅/M₁) is an order of magnitude larger than can be accommodated in the cluster without boiling off at least one subunit.

The photolysis of Ar-H₂S and Ar₂-H₂S at 248 nm reveals more complex behavior (Figs. 3.4c and d). In both cases, significant numbers of radical clusters survive for the duration of the calculation (1 ns for Ar-H₂S and 250 ps for Ar₂-H₂S precursors). These cluster concentrations level off for Ar-H₂S photolysis (note the log (time) axis), suggesting satisfactory convergence in the calculations. For the Ar-H₂S precursor, Ar-SH appears to be formed at 248 nm with roughly 20% efficiency,
Figure 3.4. Time-dependent radical concentrations from photolysis of Ar$_n$-H$_2$S clusters at two wavelengths. a) Ar-H$_2$S photolysis at 193 nm. b) Ar$_2$-H$_2$S photolysis at 193 nm. c) Ar-H$_2$S photolysis at 248 nm. d) Ar$_2$-H$_2$S photolysis at 248 nm.
providing additional confirmation that the nonfragmentary photolysis channel for Ar-H₂S can indeed result in significant open-shell cluster formation. By way of contrast, the radical cluster species concentrations for 248 nm Ar₂-H₂S photolysis do not appear to stabilize asymptotically on the 250-ps timescale of this calculation. Rather, the Ar₂-SH concentrations decrease approximately linearly with logarithmic time, such that ~25% of the initially formed Ar₂-SH clusters fragment with each 10-fold increase in time.

These calculations clearly support a significant channel for open-shell radical cluster (Ar-SH or Ar₂-SH) formation at both 193 nm and 248 nm. The dominant channel at 193 nm is Ar-SH formed by fragmentary photolysis, i.e., ejection of a hot H atom from Ar₂-H₂S followed by boil-off a single Ar atom. The efficiency for this open-shell cluster formation process is much higher at 248-nm photolysis, since there can now be contributions from both nonfragmentary Ar-H₂S and Ar₂-H₂S photolysis as well as from Ar₂-H₂S photolysis followed by subsequent boil off. Since the Ar₂-H₂S photolysis at 248 nm has not converged, it cannot yet be determined how many additional Ar₂-SH clusters will fall apart, nor what products they will form. At this stage, then, it is difficult to probe the relative importance of the photolysis pathways.

In principle, this issue could be resolved by carrying out the calculations for a longer time. However, based on the near-linear dropoff of Ar₂-SH concentration with logarithmic time, a calculation nearly two orders of magnitude longer would be required for convergence. Rather than simply extending the computational time, we first examine the energetics and dynamics of cluster formation to look for a way to predict propensities towards various pathways and to estimate final branching ratios.
In the ensuing analysis, we primarily focus on the photolysis of Ar-H$_2$S at 248 nm; results for clusters of all types will then be summarized in Sect. 3.3.4.

3.3.2 Energetics of radical cluster formation

In the corresponding experimental work, our group observed that photolysis of weakly bound closed-shell precursors produced rotationally and vibrationally hot radical clusters. Accordingly, we will explore the energetics of bound radical clusters formed from Ar-H$_2$S photolysis at 248 nm, looking at the total energy left in the cluster as well as how it is partitioned among the various rotational and vibrational modes.

As can be observed in Fig. 3.4c, the trajectories divide into two groups: those in which the radical cluster falls apart to form Ar and SH, and those which remain bound on the timescale of the calculation (1 ns). Since this calculation is nearly converged (i.e., the radical concentrations level off), we can then separately examine the energetics of bound and unbound clusters, assuming that those clusters remaining bound on this timescale will be bound for all time. In doing this, we take advantage of the rapid departure of the H atom; once it has left the precursor closed-shell cluster, no additional forces act upon the resulting radical cluster, and thus all energy in the COM frame of the radical cluster remains there for all time. Consequently, we can calculate the COM energy of the radical cluster immediately after the H atom has departed. Thus, the calculation can be halted when the H atom interaction with the cluster is negligible; this point is chosen to be 20 $a_0$ away from the S atom, where the
H-SH interaction is less than $10^{-14}$ cm$^{-1}$. To obtain better statistics for the subsequent analysis, we have calculated an additional 5000 trajectories of Ar-H$_2$S at 248 nm.

Figure 3.5 contains a histogram of the energy remaining in the Ar-SH COM frame after photolysis, separated into bound and unbound at the end of the 1-ns calculation. Superimposed is a dividing line at the dissociation energy of the Ar-SH (i.e., Ar-OH) potential surface, $D_e = 127$ cm$^{-1}$. As expected, all unbound clusters have internal energy greater than $D_e$; however, only approximately half of the bound clusters (henceforth “energetically bound”) have $E$ less than $D_e$, and half (henceforth “quasibound”) have $E$ greater than $D_e$. This result is initially puzzling: it would seem that all clusters with $E > D_e$ should ultimately fall apart.

To investigate further, we first determine the partitioning of energy in all bound Ar-SH clusters (i.e., energetically bound and quasibound) by separating the internal energy into $E_{vdW}$ (cluster van der Waals stretch energy), $E_{rot}$ (cluster end-over-end rotation), and $E_{SH}$ (vibration and libration of the SH subunit). Since $E_{SH}$ is significantly smaller than $E_{vdW}$ and $E_{rot}$ (i.e., $\leq 10\%$), we can focus exclusively on the $E_{vdW}$ and $E_{rot}$, with histograms of the energy partitioning given in Fig. 5.6. The clusters are quite vibrationally hot; however, the $E_{vdW}$ distribution ends abruptly at the dissociation limit. The excess cluster energy lies rather in rotation, with the end-over-end rotational energy distribution extending significantly beyond the dissociation limit (Fig. 5.6b).

The reason behind this unequal partitioning is clear: only $E_{vdW}$ (not $E_{rot}$) > $D_e$ will cause the cluster to dissociate. However, for quasibound clusters (i.e., with total $E > D_e$), sufficient transfer from $E_{rot}$ to $E_{vdW}$ might seem inevitable. In contrast, the
Figure 3.5. Histogram of the energy remaining in 5000 Ar-SH clusters after photolysis, separated into bound and unbound at the end of 1 ns. The line at 127 cm$^{-1}$ denotes the dissociation energy ($D_e$) of the Ar-SH. Notably, half of the bound clusters at the end of this calculation have $E > D_e$. 
Figure 3.6. Histograms of the energy partitioning between a) $E_{\text{vdW}}$, van-der-Waals-stretch vibrational modes and b) $E_{\text{rot}}$, end-over-end rotational of the Ar-SH cluster. While the vibrational energy distribution tails off at the dissociation limit ($D_e = 127 \text{ cm}^{-1}$), the rotational energy distribution clearly exceeds this limit.
convergence of the cluster calculations (Fig. 3.4c) indicates that relatively few, if any, of the clusters remaining bound at 1 ns will ultimate fall apart. The quasibound clusters must therefore be subject to a *dynamical* constraint preventing intracluster rotational-to-vibrational energy transfer; this possibility is explored in the next section.

### 3.3.3 Dynamics of radical cluster formation

As noted above, the “quasibound” clusters, i.e., those with $E > D_e$ that remain bound at the end of the 1-ns calculation, can contain energy above the dissociation limit as long as that energy is trapped in rotation. Since this must correlate to high angular momentum states, we next look at the angular momentum distributions for both energetically bound and quasibound trajectories.

Figure 3.7 contains a histogram representing the total radical-cluster angular momenta for bound Ar-SH clusters from 248-nm photolysis. A clear distinction between the energetically bound and quasibound distributions exists: the center of the angular momenta of quasibound clusters, near $40\hbar$, is shifted approximately $10\hbar$ higher than that of energetically bound clusters. Importantly, the center of each distribution exceeds the average pre-photolysis angular momentum (from the initial condition sampling) by $> 20\hbar$; thus, most of the angular momentum observed in these bound clusters is generated by photolysis. In addition, it represents an unusually hot distribution of clusters: for a peak value of $J = 40\hbar$, the rotational temperature would be greater than 300 K, much higher than temperatures typically available by coexpanding rare-gas atoms with pre-generated radicals. Correspondingly, we might
Figure 3.7. Distribution of total radical-cluster angular momenta for bound Ar-SH clusters from 248 nm photolysis, partitioned into energetically bound (E < D_e) and quasibound (E > D_e). The center of the angular momenta of quasibound clusters is approximately 10h higher than that of energetically bound clusters; both have rotational temperature ≥ 300 K.
expect these high angular momentum states to constrain cluster dynamics in a way not typically observed in jet expansions.

Such a constraint can be shown to exist for diatomic molecules, in which incorporating the kinetic energy from orbital angular momentum (L) into an effective potential, \( V_L^{\text{eff}}(R) = V(R) + \frac{L^2}{2\mu R^2} \), can produce a barrier at a given value of \( R = R^* \). Any trajectory with total energy less than \( V_L^{\text{eff}}(R^*) \) and \( R < R^* \), will remain classically bound, regardless of whether its total energy exceeds the dissociation limit of the diatomic. Indeed, Garcia-Vela has demonstrated that such a barrier can prevent Ar-Cl dissociation subsequent to Ar-HCl photolysis.\(^{36}\) For the triatomic Ar-SH, since the SH bond distance is smaller than the Ar-SH distance and the H atom is much lighter than the S, we might anticipate behavior similar to that of a pseudodiatomic. Thus, we next explore the possibility that the quasibound trajectories are held bound by an angular momentum barrier.

First, we must determine how to calculate such a barrier for the triatomic Ar-SH complex. In the diatomic case, \( V_L^{\text{eff}}(R) \) is obtained by invoking the orbital angular momentum as a constant of the motion; in the triatomic case, the total angular momentum (J) is instead conserved. Pollack has shown that for triatomics, an effective potential can be written which may contain a rigorous barrier to dissociation;\(^{49}\) for Ar-SH, this effective potential can be written as

\[
V_J^{\text{eff}}(R, r, \theta) = V(R, r, \theta) + \frac{J^2}{2I},
\]

\[
I = \frac{m_{\text{Ar}} m_{\text{SH}}}{m_{\text{Ar-SH}}} R^2 + \frac{m_{\text{S}} m_{\text{H}}}{m_{\text{SH}}} r^2 \quad (3.10)
\]
where R is the distance between the Ar and the center of mass of SH, r is the SH bond distance, \( \theta \) is the angle between these two vectors, and J is the total angular momentum.

Finding the total angular momentum barrier, defined as \( E_{\text{barrier}} \), requires two steps. First, \( V_J^{\text{eff}} \) is minimized as a function of \((r, \theta)\) at parametric values of R, producing \( V_J^{\text{eff}}(R) \). Second, \( E_{\text{barrier}} \) is determined by maximizing \( V_J^{\text{eff}}(R) \) for \( R \) outside the well region, i.e., \( E_{\text{barrier}} \equiv V_J^{\text{eff}}(R^*) \), where \( R = R^* \) is the location of this maximum. Operationally, since the minima in \( V_J^{\text{eff}}(R) \) should occur near the equilibrium value of \( r \) (see Table 3.1) and \( \theta = 0^\circ \), we set \( V_J^{\text{eff}}(R) = V_J^{\text{eff}}(R, r = r_{\text{eq}}, \theta = 0^\circ) \), then find \( E_{\text{barrier}} \) from this potential. As in the diatomic case, if photolysis generates an Ar-SH cluster with \( R < R^* \) and total energy less than \( E_{\text{barrier}} \), it will remain classically bound. Importantly, the \( V_J^{\text{eff}} \) obtained in this fashion produces a minimum barrier, which corresponds to all angular momentum lying in end-over-end tumbling of Ar-SH; when SH angular momentum is nonzero, the width of the barrier is larger.

To estimate the barrier height for trajectories in our calculations, we have calculated \( V_J^{\text{eff}}(R) \) for several representative values of J; these effective potentials are plotted in Fig. 3.8. Notably, while \( E_{\text{barrier}} \) is only on the order of a few wavenumbers for the lowest angular momentum \((20\hbar)\), it rises nearly to \( 100 \text{ cm}^{-1} \) for an angular momentum of \( 60\hbar \). Clearly, the angular momenta sampled by the Ar-SH clusters, as seen in Fig. 3.7, provide barriers sufficient to accommodate energies far above the dissociation limit. Accordingly, we expect to find a significant number of photolysis
Figure 3.8. Effective potential, $V_j^{\text{eff}}$, for several representative values of $J$ as a function of $R$, with $r$ fixed to its equilibrium value (see Eqn. 10). The asterisks designate $R = R^*$, i.e., the location of the effective angular momentum barrier. This barrier rises nearly to 100 cm$^{-1}$ for an angular momentum of 60ℏ.
trajectories with $E > D_e$ but less than $E_{\text{barrier}}$. Any such dynamically bound trajectories will be designated as “quasibound.”

To determine which trajectories are quasibound, we return to those shown in Fig. 3.4. These trajectories are separated into three categories (energetically bound, quasibound, and unbound) by calculating the total internal energy and comparing to $E_{\text{barrier}}$, which is in turn obtained from maximizing Eqn. 3.10 with respect to $R$ for each trajectory. We find that for photolysis of Ar-H$_2$S at 248 nm, nearly all the trajectories with $E > D_e$ that survive to 1-ns (i.e., quasibound trajectories) have $E < E_{\text{barrier}}$ and are thus dynamically bound. Thus, we can conclude that the angular momentum barrier plays a significant role in the classical dynamics of cluster formation.

The question remains, however, whether such high rotational states will live for sufficient time to be experimentally detected. From a quantum-mechanical perspective, the finite height of the angular momentum barrier provides a finite probability of tunneling, although tunneling might seem unlikely for a system involving heavy Ar and S masses. We follow the general procedure of Child$^{50}$ to obtain a JWKB estimate of the tunneling lifetime, $\tau$:

$$\tau = \frac{\pi}{\omega} \left( \frac{[\kappa^2 (1 + \kappa^2)]^{1/4}}{(1 + \kappa^2)^{1/2} - \kappa} \right)$$

where

$$\kappa = \exp \left[ -\int_{b}^{c} k(R) dR \right]$$

$$k(R) = \left\{ 2\mu_{\text{Ar-SH}} \left[ E - V(\text{Ar-SH}) \right] \right\}^{1/2} / \hbar,$$
ω is the classical attempt frequency, and b,c are inner and outer points, respectively, in R at which $V_j^{\text{eff}} = E_{\text{tot}}$. We set ω at 40 cm$^{-1}$, which is approximately the vibrational frequency of Ar-SH. This tunneling lifetime can then be compared to the experimental delay between the photolysis and probe pulses (typically 100 ns) to estimate how many quasibound clusters would fall apart before being detected.

Figure 3.9 contains the tunneling lifetimes calculated for quasibound clusters resulting from photolysis of Ar-H$_2$S at 248 nm. These lifetimes are plotted as a function of $\Delta E/E_{\text{barrier}}$, where $\Delta E$ is the energy above the dissociation limit such that as $\Delta E/E_{\text{barrier}} \to 0$, the total energy decreases toward the dissociation limit. X’s represent Ar-SH clusters whose tunneling lifetimes are shorter than 100 ns (i.e., tunneling on a timescale shorter than the photolysis-probe delay), and o’s represent clusters whose tunneling lifetimes are greater than that delay. Not surprisingly, the shortest tunneling lifetimes are clustered near $\Delta E/E_{\text{barrier}} \to 1$, i.e., when the total internal energy of the cluster approaches the barrier height. Intriguingly, tunneling lifetimes shorter than the 100-ns experimental timescale represent approximately half of the quasibound clusters; from this initial estimate, we would expect that nearly half thus fall apart prior to detection.

As discussed above, angular momentum of the SH subunit increases the width of the barrier “seen” by the molecule thus drastically increasing the tunneling lifetime of a given cluster. Accordingly, we would expect fewer clusters to tunnel than indicated by this 1D estimate. Nevertheless, this effect opens the possibility that tunneling may contribute to the dramatic cluster cooling observed experimentally as the photolysis-probe delay increases up to 10 μs. However, since our calculations
Figure 3.9. Tunneling lifetimes of quasibound clusters versus $\Delta E/E_{\text{barrier}}$ from photolysis of Ar-H$_2$S at 248 nm, where $\Delta E$ is the energy in the cluster above the dissociation limit and $E_{\text{barrier}}$ is the barrier height. The x’s represent lifetimes shorter than 100 ns (the photolysis-probe delay), and o’s represent lifetimes greater than that delay. While trajectories with tunneling lifetimes less than 100 ns are clustered near $\Delta E/E_{\text{barrier}} \to 1$, these represent approximately half of these quasibound trajectories.
confirm a significant population of clusters with $E < D_e$ (i.e., which cannot undergo quantum mechanical tunneling), loss of the hottest clusters by tunneling is not the only source of the observed cooling. In addition, the large dynamic range observed in the tunneling lifetimes (from one vibrational period to billions of years) indicates that few clusters will fall apart in the range of experimental delays (<10% of the trajectories in Fig. 3.9 have lifetimes in the 100-ns to 10-µs). Thus, while tunneling may contribute to an overall loss of signal in comparison with classical predictions, it is not likely to be the source of the dramatic cooling on the experimental timescale.

3.3.4 Efficiency and mechanisms of cluster formation: comparison with experiment

With an understanding of the energetics and dynamics of radical cluster formation, we have a basis for predicting the relative contributions of various photolysis mechanisms to the experimental spectra. For this purpose, we summarize the branching ratios between photolysis products in Table 3.2. These branching ratios include all classically bound clusters (i.e., energetically bound and quasibound), since the number of clusters predicted to tunnel cannot be precisely determined (as discussed in the previous section). The frequency of bound versus unbound trajectories can be estimated from relative populations in calculations given in Fig. 3.4. However, some calculations had either not converged by the end of the calculation or had not produced measurable products.

To aid in determining branching ratios among the photolysis products, we thus perform additional calculations on systems nonconverged results. We first focus on Ar-H$_2$S, for which we can calculate the internal energy and angular momentum of the
**Table 3.2.** Calculated product branching ratios for Ar-H$_2$S and Ar$_2$-H$_2$S photolysis at 193 nm and 248 nm.

<table>
<thead>
<tr>
<th>$\lambda_{\text{photolysis (nm)}}$</th>
<th>Precursor</th>
<th>Product distribution, %</th>
<th>Ar-SH</th>
<th>Ar$_2$-SH</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Total</td>
<td>E &lt; $D_e$</td>
<td>$D_e &lt; E &lt; E_{\text{barrier}}$</td>
</tr>
<tr>
<td>193 Ar-H$_2$S</td>
<td>0.06(2)$^a$</td>
<td>0</td>
<td>0.06(2)</td>
<td></td>
</tr>
<tr>
<td>193 Ar$_2$-H$_2$S</td>
<td>17(2)</td>
<td>12(2)</td>
<td>4(1)</td>
<td>0</td>
</tr>
<tr>
<td>248 Ar-H$_2$S</td>
<td>24(2)</td>
<td>13(2)</td>
<td>11(1)</td>
<td></td>
</tr>
<tr>
<td>248 Ar$_2$-H$_2$S</td>
<td>51(3)</td>
<td>50(3)</td>
<td>0.8(4)</td>
<td>0.8(4)</td>
</tr>
</tbody>
</table>

$^a$ Numbers in parentheses represent 2$\sigma$.

Cluster as soon as the H atom flies off and thus obtain branching ratios among bound, quasibound, and unbound clusters. Calculations at both wavelengths converged in the original 1-ns timescale, but no Ar-SH product was observed at 193 nm. Thus, we have calculated an additional 20,000 trajectories at 193 nm, halting the trajectories after H-atom flyoff and determining if any radical clusters will survive. Out of these, none are energetically bound, but 11/20,000 are quasibound.

For Ar$_2$-H$_2$S, we can also use the understanding of cluster energetics and dynamics to explore the photolysis in more detail, although the picture is not quite as simple, i.e., the classical fate of the cluster is not necessarily determined after H atom flyoff. If the total internal energy of the cluster is less than the dissociation energy for either Ar-Ar or Ar-SH, then we expect Ar$_2$-SH to remain classically bound. This
allows interrogation of the Ar$_2$-H$_2$S trajectories at 248 and 193 nm to determine if any form bound Ar$_2$-SH. For 248-nm photolysis, 4/500 have energy below the barrier to boiling off any subunit and thus form Ar$_2$-SH, while none out of 5500 at 193 nm do. The remaining clusters contain sufficient energy to boil off one or more of the subunits (Ar or SH), with SH boil-off resulting in an unbound cluster and Ar boil-off in a bound, quasibound, or unbound Ar-SH cluster. Since prior to the boil off of a subunit, the fate of the cluster cannot be determined, the calculation must continue until one subunit escapes.

While cluster concentrations from the 193-nm Ar$_2$-H$_2$S trajectories level off during the timescale of the original calculation, the 248-nm trajectories do not. Correspondingly, we propagate forward those 248-nm trajectories still containing Ar$_2$-SH at the end of the previous 250-ps calculation for an additional decade of time, i.e., 2.5 ns. Based on the observation of a ~25% drop in concentration in each decade of time (see Fig. 3.4), we might expect an additional ~25% loss during this extended calculation. Instead, the dissociation rate decreases such that only an additional ~11% fall apart (i.e., approximately 25% remain after 2.5 ns). This decreased rate may imply that some ultimately unbound clusters will survive long enough to be probed; however, the binding energy of the Ar-OH potential used is larger than the binding energy of Ar-SH, and our estimates represent an upper limit to the dissociation lifetimes that would be observed experimentally.

More important for our branching ratio estimates, all of these clusters boil off an Ar to form Ar-SH. We thus anticipate all of the remaining trajectories in this group (i.e., those which still contain Ar$_2$-SH after 2.5 ns) will ultimately fall apart to
Ar + Ar-SH, rather than Ar$_2$ + SH or Ar + Ar + SH. Accordingly, we have estimated the net product branching ratios in Table 3.2 based on this assumption.

This estimate thus completes the branching ratios in Table 3.2, providing the basis for elucidating the dominant cluster formation mechanisms as well as for comparing with experimental results. By measuring relative Ar-SH/Ar$_2$-SH signals as a function of reciprocal argon concentration, the relative importance of the various photolysis channels were experimentally determined at both photolysis wavelengths. The key results are highlighted below and discussed in the context of the trajectory calculations.

First of all, even at the highest photolysis energy, some fraction of the Ar-SH species observed experimentally resulted from Ar-H$_2$S photolysis, i.e., from a nonfragmentary pathway. This result is supported by our trajectory calculations, with a nearly 20% survival rate of Ar-SH from Ar-H$_2$S at 248 nm and a small but nonzero survival rate at 193 nm. Incidentally, all of the 193-nm clusters are quasibound (i.e., with D$_e$ < E < E$_{\text{barrier}}$), compared to half of the 248-nm trajectories. This must result from accommodation of a much larger excess photolysis energy, producing hotter clusters. Also notable is the efficiency of the “boil-off” mechanism for Ar-SH production from Ar$_2$-H$_2$S; 17% and 51% of Ar$_2$-H$_2$S precursors follow that path at 193 nm and 248 nm, respectively. In each of these cases, fewer Ar-SH clusters are quasibound than bound, presumably because the extra Ar atom typically carries away sufficient energy so that the remaining cluster contains E < D$_e$.

In contrast to the importance of the nonfragmentary pathways for Ar-H$_2$S, nonfragmentary photolysis of Ar$_2$-H$_2$S (i.e., producing Ar$_2$-SH) is not a major channel
at either wavelength. At first, this might seem surprising: given a particular amount of energy to accommodate, Ar$_2$-SH has more modes of motion for energy disposal than Ar-SH. However, while additional modes may delay dissociation, the excess energy can eventually build up in a particular mode and lead to boil off of one subunit. In addition, if H$_2$S dissociation were strictly uncoupled from interactions with the Ar atom(s), less kinetic energy would be “lost” by transforming the velocity of the dissociating SH into the COM frame of the radical cluster with two Ar atoms present than with one Ar present. In this limit, an Ar$_2$-SH cluster must accommodate more energy than Ar-SH; thus, the boil-off mechanism dominates.

The relative importance of photolysis mechanisms in the trajectory calculations leads us to two addition points of comparison with experiment. First, experimental evidence showed that at 193 nm, fragmentary photolysis of Ar$_2$-H$_2$S is more dominant over nonfragmentary photolysis than at 248 nm. In other words, an Ar$_2$-SH cluster is more likely to boil off an atom at the higher photolysis energy, consistent with the greater excess energy generated at 193 nm. This observation agrees with our calculations, which yield no Ar$_2$-SH product from 193-nm photolysis of Ar$_2$-H$_2$S; however, we cannot predict whether additional trajectories would produce any such product and thus cannot exactly determine the relative importance of these pathways. Second, the experiments showed that the probability of nonfragmentary photolysis of both Ar$_2$-H$_2$S and Ar-H$_2$S decreases with photolysis energy, but that nonfragmentary photolysis of Ar$_2$-H$_2$S decreases more slowly than Ar-H$_2$S. Clearly, while the calculations agree that nonfragmentary photolysis decreases as a function of collision energy for both precursor clusters, the second
point cannot be addressed without any Ar$_2$-SH product from 193-nm photolysis of Ar$_2$-H$_2$S.

Having explored the dynamics of the Ar$_n$-H$_2$S photolysis system, we now expand our focus to investigate more generally the feasibility of radical cluster formation from photolysis of closed-shell precursors. To that end, we work through the simple ballistic model proposed previously\textsuperscript{39} to estimate the energetics of radical cluster formation, focusing on precursors containing clusters of H$_2$S/H$_2$O (designated H$_2$X) with a single additional subunit, typically a rare gas (designated R$_g$).

In this model, the first assumption is that the H$_2$X is uncoupled from interactions with the accompanying subunit during the photolysis step. Consequently, by conservation of momentum, the departing H atom must carry away most of the excess energy from the photolysis, leaving the following in XH translational energy:

\[
T_{XH} = \frac{m_{XH} \cdot v_{XH}^2}{2} = \frac{h\nu - D_0 \cdot (HX-H)}{(1 + m_{XH}/m_H)}
\]  

(3.12)

For H$_2$S, this reduces the photolysis energy imparted to the SH by ~34-fold from the excess photolysis energy; for H$_2$O, by ~17-fold. The recoil energy of the XH is further reduced by transformation into the COM frame of the remaining radical cluster, with a larger reduction for lighter collision partners:

\[
E_{Rg-XH} = \frac{\mu_{Rg-XH} \cdot v_{XH}^2}{2} = \frac{\mu_{Rg-XH} \cdot h\nu - D_0 \cdot (HX-H)}{(1 + m_{XH}/m_H)}
\]  

(3.13)
Eqn. 3.13 thus represents an upper limit on the COM energy imparted to the radical cluster by photolysis of the monomer.

Using Eqn. 3.13, we calculate this COM cluster energy for photolysis of H\textsubscript{2}O and H\textsubscript{2}S with a variety of cluster partners, plotted in Fig. 3.10 as a function of collision partner mass. The photolysis wavelengths represented are 193 nm and 248 nm for H\textsubscript{2}S, and 193 nm for H\textsubscript{2}O; for comparison, the experimental dissociation energies of the radical clusters are also shown. Several interesting trends can be seen in this figure. First of all, decreasing the mass of the collision partner does indeed decrease the COM energy. However, a similar trend is observed in the binding energies of the radical clusters, so simply reducing the mass of the collision partner would not ensure an increased probability of radical cluster formation. Second, the photolysis products of H\textsubscript{2}S and H\textsubscript{2}O at 193 nm nearly overlap on this chart. This results from two competing effects: the lighter mass of O versus S causes the H atom to carry away less energy, but the H-OH bond is stronger than the H-SH bond, leaving less excess energy from the photolysis within the cluster.

Third, and most importantly, it is clearly feasible to produce bound open-shell clusters even when the COM energy estimated by this ballistic model is larger than \( D_0 \). Indeed, even though \( E_{\text{COM}} \) for Ar-H\textsubscript{2}S photolysis at 193 nm is nearly fourfold larger than the binding of Ar-SH, free-radical clusters are observed both experimentally and theoretically. This raises the possibility that \textit{any} of the clusters found in Fig. 3.10 might be formed via photolysis of the closed-shell precursor.
Figure 3.10. COM cluster energy versus collision partner mass for photolysis of H₂O and H₂S clustered with a single collision partner (calculated from Eqn. 3.13). Superimposed are the dissociation energies for appropriate rare-gas/radical clusters (denoted with a + and labeled). These calculations assume no potential-energy interaction between the collision partner and radical during the photolysis process and thus represent an upper limit to the COM energy.
3.5 Conclusions

We have carried out quasiclassical trajectory calculations for the photolysis of Ar-H₂S and Ar₂-H₂S at 193 nm and 248 nm. These calculations serve as a basis for comparison to our earlier experiments on photolysis of these clusters in a supersonic jet expansion, in which we observed a remarkable efficiency for formation of the radical cluster species Ar-SH and Ar₂-SH from photolysis of the closed-shell precursors.

First, the quasiclassical photolysis calculations confirm the overall efficiency of radical cluster formation. Indeed, for photolysis of Ar-H₂S at 248 nm, roughly 20% of the precursors form bound Ar-SH clusters. Even at the shorter photolysis wavelength of 193 nm, the fragmentary photolysis of Ar₂-H₂S forms Ar-SH clusters with roughly 20% efficiency. The timescales on which unbound radical clusters fall apart are typically much shorter than the experimental timescale, ranging from ~5 ps for 193 nm photolysis of Ar-H₂S to ~10 ns for 248 nm photolysis of Ar₂-H₂S. The remarkable efficiency of radical cluster formation results in part from the fact that the relatively light H atom, by conservation of momentum, carries away the majority of the excess photolysis energy in kinetic energy.

However, the calculations confirm that the clusters retain sufficient energy in their COM frame for significant intracluster rovibrational excitation. The energy found in these clusters is primarily partitioned between relative rotation and vibration of the Ar and SH subunits. Ar-SH vibrational states up to the dissociation limit are populated, indicating that the photolysis process yields bound clusters that sample
significant regions of the potential energy surface. In addition, rotational energies up to and beyond the dissociation limit are found in bound clusters, pointing to the existence of an angular momentum barrier to dissociation. Indeed, nearly half of the bound Ar-SH clusters from photolysis of Ar-H₂S at 248 nm, and all of the bound Ar-SH from photolysis at 193 nm, contain total energy greater than the dissociation limit. However, that energy, trapped in rotation, is unavailable for transfer into vibration; thus, the clusters are classically bound. Quantum mechanical tunneling calculations indicate that as an upper limit, roughly half of these quasibound clusters may fall apart prior to probing on the experimental timescale (i.e., 100-ns delay between photolysis and probe pulses).

These calculations provide a basis for comparing the relative efficiencies of two radical-cluster formation mechanisms: nonfragmentary (in which no Ar atoms are lost) versus “boil off” (in which one Ar atom carries away the excess energy). Overall, the nonfragmentary production of Ar-SH from photolysis of Ar-H₂S is demonstrated to be remarkably efficient at the longest photolysis wavelength (248 nm), while the “boil off” mechanism produces a large fraction of bound Ar-SH clusters (≈ 20%) from Ar₂-H₂S, even at the shortest wavelength (193 nm). Finally, the overall efficiency of this method for bound closed-shell cluster production from Arₙ-H₂S photolysis provides evidence that this technique could be extended to bound clusters of other hydrides (e.g., H₂O) and clustering species (e.g., H₂, Kr, Ne).
References for Chapter 3


48. NAG Fortran Library (Oxford University: Oxford, 1997)


CHAPTER 4

DYNAMICS OF COLLISIONAL ALIGNMENT IN SUPersonic
EXPANSIONS: TRAJECTORY STUDIES OF HE + CO, O₂ AND CO₂

4.1 Introduction

Probing and ultimately controlling the dynamics of chemical reactions at the quantum state-to-state level has long been a goal of chemical physics research. At the highest level of detail, studies of bimolecular reaction dynamics would permit the stereochemistry to be manipulated, influencing what region of the potential surface is sampled as the reagent molecules approach and collide. One key step in this overall scheme is to orient or align the colliding molecules with respect to some lab-/body-fixed axis frame, either by static (DC) fields, optical (AC) fields, or simply directed collisions in an anisotropic flow.¹ Depending on the efficiency of these processes, such techniques ultimately offer the opportunity to probe the detailed topology of a reactive potential energy surface, or, in other words, the “steric effect” in a chemical reaction.

This general area of molecular control of stereodynamics has witnessed enormous growth over the past 30 years, primarily exploiting alignment and/or
orientation of rotational angular momentum states in external fields. Mathematically, orientation and alignment refer to ordered moments of the $m_j$ distribution (the z-axis projection of $j$). Oriented samples correspond to $\langle m_j \rangle \neq 0$, with the lowest order quantum-mechanical orientation given by

$$O_0^{(1)} = \langle j | j_z | j | m_j \rangle / \sqrt{j(j+1)}$$  \hspace{1cm} (4.1)$$

where the outer brackets represent an average over the $m_j$ distribution. Alternatively, aligned samples can have $\langle m_j \rangle = 0$ but require a non-uniform distribution in $|m_j|$, with a lowest order alignment given by

$$A_0^{(2)} = \langle j | j_z^2 - j^2 | m_j \rangle / \sqrt{j(j+1)}$$  \hspace{1cm} (4.2)$$

In the classical limit, this orientation and alignment can be related to the first and second Legendre moments, respectively, of the corresponding angular distribution of $j$. For collision systems symmetric with respect to the relative velocity vector (i.e., in the absence of any external fields), the final $m_j$ and $-m_j$ populations are exactly equal, which precludes any orientation effects. However, the distributions in $|m_j|$ can be non-uniform and therefore result in finite rotational alignment. In general, a distribution with an excess of $j$ states parallel or perpendicular to the alignment axis corresponds to $A_0^{(2)} > 0$ or $A_0^{(2)} < 0$, respectively.

The use of angular momentum quantum states to influence or control bimolecular collision geometries was originally developed by the Bernstein$^3$ and
Brooks\textsuperscript{4} groups. In these studies, a $|jkm\rangle$ state-selected molecular beam of symmetric-top CH$_3$I molecules was focused with an inhomogeneous hexapole electric field and subsequently oriented along a specific laboratory direction with a homogeneous electric field. By crossing this oriented beam of CH$_3$I with a beam of Rb or K atoms, it was demonstrated that reaction preferentially occurs when the iodine end of CH$_3$I is pointed toward the reactive alkali species, thus providing first experimental insights for steric effects in simple atom-abstraction processes.

Although the hexapole focusing methods have enjoyed widespread use,\textsuperscript{5-8} this technique is typically constrained to molecules exhibiting a large, first-order Stark effect. Alternatively, electric-field techniques have been developed that exploit the second-order Stark effect to align the rotational states of linear molecules.\textsuperscript{9-11} More recently, Loesch and coworkers\textsuperscript{12-14} and Friedrich \textit{et al.}\textsuperscript{15,16} have utilized strong homogeneous electric fields to create highly oriented “pendular” states of rotationally cooled linear molecules by the so-called “brute force” technique. Such methods have been particularly successful in linear hydrogen-bonded clusters,\textsuperscript{17-21} where the large dipole moments and small rotational constants make them especially convenient to manipulate into the pendular regime.

The use of DC electric field methods for alignment and orientation requires the molecule to have a large permanent dipole moment, which significantly limits the range of applicability. Alternatively, magnetic-field alignment techniques developed by Herschbach and coworkers can be applied more generally to both polar and nonpolar molecules, but with the restriction that these species must be paramagnetic.\textsuperscript{22,23} In principle, optical (AC) field methods offer more generality; for
example, polarized light can be used to orient or align molecules by single-photon excitation, selective photodissociation, Raman scattering, laser-induced AC Stark effect, or intense non-resonant laser fields. Indeed, much of the work in the area of rotational alignment has been carried out simply using single-photon excitation followed by polarized fluorescence detection, with the necessary theoretical framework developed by Zare and coworkers and Meyer for parallel bands of linear and symmetric-top molecules, and by Weida and Parmenter for perpendicular transitions of symmetric-top molecules as well as a-, b-, and c-type transitions of asymmetric tops. Unlike static DC field methods, rotational alignment via single-photon excitation requires no permanent dipole moment; however, it does require significant transition strengths and a relatively long-lived upper state.

A more general alternative is the use of collisions in an anisotropic velocity distribution to create the alignment, as pictured schematically in Fig. 4.1 for linear molecules without internal degrees of freedom. When a velocity gradient exists between such molecules, collisions along the direction of flow will preferentially align their angular momenta (\(j\)) perpendicular to the flow. Stated physically, the molecules with \(j\) parallel to the flow present a larger cross sectional area for collisional reorientation, while molecules with \(j\) perpendicular to the flow are less likely to be hit. As modeled by Zare and coworkers, even if all such collisions simply randomize the direction of \(j\), this will lead to a net alignment of angular momenta perpendicular to the gas flow (i.e., negative alignment). This concept of
Figure 4.1. A schematic depiction of collisional alignment in supersonic expansions. The lighter, faster-moving “diluent” atoms (white circles) collide with heavier, slower-moving “seed” rotor molecules (gray ovals) along the expansion axis. Rotor molecules with $\mathbf{j}$ parallel to the expansion axis present a larger collisional cross section than those with $\mathbf{j}$ perpendicular and thus are more subject to reorienting collisions.
alignment by reorienting collisions, first presented by Gorter,\textsuperscript{48} can be easily extended to alignment in supersonic expansions. For an expansion mixture containing a lighter “diluent” gas and a heavier “seed” gas, velocity gradients cause the slower-moving seed gas molecules to undergo multiple, anisotropic collisions with the faster-moving diluent gas molecules. These directed collisions align seed molecule rotations by creating an anisotropic distribution of $m_j$ along the expansion axis.

Indeed, such anisotropically aligned distributions of seed molecules in a supersonic expansion were observed as early as the 1970s by the Zare group, who studied directed collisions in a neat expansion of Na atoms (“diluent”) with small concentrations of Na\textsubscript{2} (“seed”) to align the rotations of the dimers.\textsuperscript{47} Since then, many experimental studies have demonstrated collisional alignment of rotor molecules for a wide range of collision partners and expansion conditions, producing aligned distributions of Na\textsubscript{2},\textsuperscript{49,50} I\textsubscript{2},\textsuperscript{51-55} CO\textsubscript{2},\textsuperscript{56} CO,\textsuperscript{57} O\textsubscript{2},\textsuperscript{58-60} and N\textsubscript{2}.\textsuperscript{61} These studies demonstrate the powerful generality of collisional alignment: in principle, any non-spherical molecule (i.e., with an anisotropic state-to-state collision cross section) can be rotationally aligned by collisions in a directed flow.

While several studies have attempted to characterize the alignment process, contrasting descriptions of the collisional mechanism have arisen. For example, experimental IR-based studies by Weida and Nesbitt demonstrate that alignment of CO\textsubscript{2} seeded in a He expansion becomes increasingly negative as a function of CO\textsubscript{2} rotational angular momentum;\textsuperscript{56} this is quite similar to the observations of Hefter \textit{et al.}\textsuperscript{49} in Na expansions, which indicate increasingly negative alignment of Na\textsubscript{2} with $j$ up to $j = 10$. Conversely, under certain expansion conditions Herschbach and
coworkers find that alignment of I₂ in Ne becomes less negative with I₂ rotational angular momentum, though only a limited number of rotational levels were accessed with their laser excitation source. Quite recently, studies of the alignment dependence on the final velocity of the "seed" molecule have produced more strikingly contradictory results. For example, experiments performed by the Aquilanti group on O₂ and N₂ with a range of diluent gases including He indicate that rotor molecules moving faster than the average are increasingly aligned with j perpendicular to the expansion axis. On the other hand, studies by Harich and Wodtke in He + CO expansions lead to exactly the opposite conclusion, i.e., the faster CO molecules are preferentially aligned with j parallel to the expansion axis.

In parallel with this experimental work, there have been several theoretical studies of collisional alignment in supersonic expansions. Early efforts by Sanders and Anderson and more recent ones by Pullman et al. have explored alignment of I₂ by Ar collisions. Sanders and Anderson specifically address the evolution of rotational alignment over multiple collisions but do not identify the mechanism for how this alignment is created on a collision-by-collision basis. Conversely, Pullman et al. focus exclusively on the single-collision regime, exploring the alignment dependence on impact parameter, collision energy, and I₂ initial angular momentum as a function of an Ar-I₂ model interaction potential. For all potentials studied, classical trajectories fall primarily into two regimes: trajectories at small impact parameters produce more molecules with j perpendicular to the collision axis, while those at large impact parameters produce more with j parallel. In addition, potentials with an attractive well exhibit "sticky," long-lived collision complexes. This
ultimately leads to aligned molecules with \( j \) perpendicular to the relative velocity vector, although with overall alignments typically smaller in magnitude than direct collisions.

The recent experimental results highlight important new theoretical issues not adequately addressed by previous work. For example, the final \( j \)-state and velocity dependence of the rotational alignment remain relatively unexplored. Furthermore, the contradictory velocity dependences reported for He + O\(_2\) and He + CO alignment studies raise the possibility of extreme sensitivity to the molecular interaction potential. Given these qualitative differences and the importance of the interaction potential suggested by the Ar-I\(_2\) collisional alignment simulations, further study of the role of the interaction potential in these particular systems would appear to be in order.

The focus of this chapter is a detailed investigation of collisional alignment mechanisms in supersonic expansions. To facilitate comparison with experiment, three collision systems (He + CO\(_2\), He + CO, and He + O\(_2\)) have been studied that are based on realistic interaction potentials. Using classical trajectory calculations, the supersonic jet expansion conditions are simulated by producing multiple collisions between He “diluent” gas atoms and single “seed” molecules along the expansion axis. To address the possible dependence of alignment effects on initial collision velocity, these studies are performed for three different collision energies corresponding roughly to three different temperature regions (\( \approx 300 \) K, 100 K and 20 K) in the expansion. These simulations permit direct comparison with experimental
results, as well as an opportunity to investigate the mechanism for alignment formation on a collision-by-collision basis.

The remainder of this chapter is organized as follows. In Sect. 4.2, we describe the details of the computations used to model the supersonic expansions. In Sect. 4.3, we discuss the results of these computations, addressing both multicollisional alignment effects and single-collision mechanistic details. In Sect. 4.4, we compare these results to experiments and discuss the implications. The conclusions of our studies are summarized in Sect. 4.5.

### 4.2 Computational Approach

To investigate the mechanism of collisional alignment in supersonic expansions, classical trajectory calculations are used to simulate multiple-collision dynamics between light “diluent” gas atoms and heavier “rotor” molecules. To address the dependence of alignment on relative velocity, three different regions of the expansion are represented, corresponding to 300 K \( (E_{\text{com}} = 266 \text{ cm}^{-1}) \), 100 K \( (E_{\text{com}} = 89 \text{ cm}^{-1}) \) and 20 K \( (E_{\text{com}} = 18 \text{ cm}^{-1}) \) collision conditions. The choice of \( \text{O}_2 \), \( \text{CO} \), and \( \text{CO}_2 \) “seed” rotor molecules and He “diluent” atoms enables direct comparison of these trajectory calculations to the experiments of Aquilanti et al.,\(^{58}\) Harich and Wodtke,\(^{57}\) and Weida and Nesbitt.\(^{56}\) A multicollision simulation consists of a single rotor molecule undergoing many successive but uncorrelated collisions (up to \( N_{\text{coll}} \approx 200 \)) with He atoms at the same energy (details provided below). From several thousand of these multicollision simulations, we group the results together in an ensemble of rotors (i.e., \( N_{\text{ensemble}} \approx N_{\text{sim}} \cdot N_{\text{coll}} \approx 500,000 \)), from which the relevant
statistics for collisional development of the rotational alignment can be explored for each choice of rotor molecule and region of the expansion.

For each multicollision simulation, we first need an appropriate He-rotor interaction potential. While details of the diluent-seed potentials have been neglected in early hard-sphere theories of collisional alignment,47 in light of the qualitative discrepancies observed for He + O₂ versus He + CO collision systems,47,48,49 we choose to model the He-rotor interactions as accurately as possible, with potentials experimentally determined from crossed molecular beam scattering or cluster IR-spectra studies. Figure 4.2 shows contour maps of the potentials used for He-O₂,64 He-CO,65 and He-CO₂.66 At first glance, the He-O₂ and He-CO potentials appear qualitatively similar in terms of well depth and degree of anisotropy. However, unlike the symmetric He-O₂ potential, the He-CO potential differs slightly from one end of the rotor molecule (θ = 0°) to the other (θ = 180°). Furthermore, the He-CO well is slightly shallower than for He-O₂ (Dₑ = 23 versus 26 cm⁻¹). The He-CO₂ potential differs from the other two by its significantly greater anisotropy and much deeper well (Dₑ ≈ 41 cm⁻¹).

While the He-rotor intermolecular potentials may or may not prove critically important to the collisional dynamics, it is reasonable to assume that the dynamics are less sensitive to rotor intramolecular potentials. For this reason, we approximate the rotor intramolecular degree of freedom as harmonic oscillator(s), with parameters given in Table 4.1. Furthermore, the O₂ and CO vibrational frequencies are reduced by roughly threefold to expedite longer time steps in the numerical integration.
Figure 4.2. Contour plots of the potential energy surfaces for a) He-O$_2$, b) He-CO, and c) He-CO$_2$. R represents the distance between the He atom and the center of mass of the rotor, while $\theta$ represents the angle between the rotor axis and the position of the He atom. $\theta$ equal to 0° or 180° corresponds to a collinear configuration, while $\theta$ equal to 90° corresponds to a T-shaped configuration (for He-CO, the C points toward the He at 0°). The solid contours represent 20-cm$^{-1}$ increments in the positive region of the potential, while the dashed contours represent 2-cm$^{-1}$ increments in the negative region. The well depths are approximately a) 26 cm$^{-1}$ for He-O$_2$, b) 23 cm$^{-1}$ for He-CO, and c) 41 cm$^{-1}$ for He-CO$_2$. 

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Table 4.1. Intramolecular harmonic potential parameters and effective “hard sphere” He + rotor cross sections, used to normalize the number of collisions (see text for details).

<table>
<thead>
<tr>
<th>Potential Parameters</th>
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</thead>
<tbody>
<tr>
<td></td>
<td>μ(amu)</td>
<td>r_e (Å)</td>
<td>ω_1 (cm⁻¹)</td>
<td>ω_2 (cm⁻¹)</td>
<td>ω_3 (cm⁻¹)</td>
<td>266 cm⁻¹</td>
<td>89 cm⁻¹</td>
<td>18 cm⁻¹</td>
<td></td>
</tr>
<tr>
<td>O²</td>
<td>32</td>
<td>1.207</td>
<td>600</td>
<td></td>
<td></td>
<td>21</td>
<td>25</td>
<td>28</td>
<td></td>
</tr>
<tr>
<td>CO</td>
<td>28</td>
<td>1.128</td>
<td>600</td>
<td></td>
<td></td>
<td>24</td>
<td>29</td>
<td>33</td>
<td></td>
</tr>
<tr>
<td>CO₂</td>
<td>44</td>
<td>1.16</td>
<td>1351.2</td>
<td>672.2</td>
<td>2396.4</td>
<td>26</td>
<td>29</td>
<td>31</td>
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</table>

Since these vibrational spacings are still more than twofold larger than the highest collision energies sampled, translational-vibrational (T-V) energy transfer effects are still anticipated (and numerically verified) to be insignificant. However, since the low-frequency bending mode of CO₂ (ν₂ ≈ 667 cm⁻¹) is already close to this limit, the known experimental harmonic frequencies are used for each CO₂ vibrational frequency. In all cases, vibrational excitation from a single collision is verified to be ≤ 2% and more typically ≈ 0.1% of the zero-point energy for the lowest-frequency vibration.

Initial conditions for the He and rotor are selected following the procedure of Raff and Thompson. For each expansion region, we select a single collision energy corresponding to \( \frac{1}{2} \mu <v_{rel}^2> \), where \( \sqrt{<v_{rel}^2>} \) is the rms relative speed of the rotor and He gas at the characteristic temperature, placed entirely in He atom velocity towards a
stationary rotor atom. This temperature is also used for Boltzmann sampling of initial rotational states, so that the collisions do not significantly heat up or cool the ensemble. The initial coordinates of the rotor are obtained by random selection of its orientation in the rotational plane. The result is monoenergetic collisions with an isotropic, Boltzmann distribution of rotors at the given temperature with no initial alignment. Trajectories are initiated at sufficiently large He.rotor distances so that intermolecular interactions are negligible (≤0.1% of the well depth), with the He placed at a random distance (10-20 Å for O2 and CO, 15-30 Å for CO2) “upstream” of the rotor along the collision axis. Initial impact parameters for the collision are also randomly sampled from a uniform distribution (i.e., weighted by $2\pi b_{\text{db}}$), with a maximum value ($b_{\text{max}}$) of 5 Å for He + CO and He + O2 and 7 Å for He + CO2. Convergence with respect to maximum impact parameter is explicitly verified for each collision system. In the He + O2 system, for example, trajectory ensembles have been studied with $b_{\text{max}}$ ranging from 2.0 Å to 10.0 Å; the resulting collisional alignment grows rapidly with $b_{\text{max}}$ up to ≈2.8 Å, then grows by ≤10% for a 3.6-fold further increase in $b_{\text{max}}$ from 2.8 Å to 10 Å. For multiple collisions with a single rotor molecule, the rotor’s center-of-mass translation is reset to zero at the end of each collision, while its rotational speed and angle with respect to the collision axis are retained.

The trajectories are calculated by integrating Hamilton's equations of motion in Cartesian coordinates with a variable-order, variable-stepsize, Adams-method numerical integrator.69 To ensure that a collision has had the opportunity to occur, each trajectory is run for a minimum time period $\tau = 2R_0/v_0$, where $R_0$ is the initial
He-rotor distance and $v_o$ is the initial relative velocity. The trajectory terminates when the He-rotor interaction potential is negligible, i.e., less than $10^{-4}$ of the total kinetic energy. Step size constraints are chosen to maintain conservation of energy better than $10^{-4}$ and typically $10^{-5}$ for a single-collision trajectory. This permits sufficient computational speed without significantly affecting the predicted alignments: for example, a test ensemble of 100 multicollision simulations of He-O$_2$ at 266 cm$^{-1}$ calculated with 100-fold tighter constraints yields asymptotic alignments differing by less than the statistical uncertainty ($<3\%$). For every collisional event in a multicollision simulation, we record the impact parameter ($b$), the magnitude of the classical initial and final rotor angular momenta ($j_i, j_f$), the initial and final projections of $j$ along the collision axis {$j_i, j_f$}, and the final rotor velocity along that axis. These values provide the necessary information for analysis of alignment as a function of number of collisions, collision energy, angular momentum, and final rotor velocity for comparison with experimental results. In particular, this enables the alignment formation to be examined on a collision-by-collision basis.

Once a trajectory in an ensemble has been generated, the final alignment is calculated as follows. For a given $m_j$ state, the classical angle between the rotor angular momentum vector, $j$, and the collision axis is obtained from $\theta = \cos^{-1}(m_j/j)$. For a distribution of final $m_j/j$ states and hence values of $\theta$, the alignment can be described by an expansion in even-order Legendre polynomials,

$$
\rho(\cos\theta) = \frac{1}{2}[1 + a_2P_2(\cos\theta) + a_4P_4(\cos\theta) + \ldots], \quad (4.3)
$$
where $\rho$ is the probability density of molecules with $\mathbf{j}$ pointing at an angle $\theta$ with respect to the collision axis. For this normalized probability distribution, i.e., $\int \rho(\cos \theta) \ d(\cos \theta) = 1$, the coefficients are obtained simply from $a_n = (2n+1)\langle P_n(\cos \theta) \rangle$. Although higher order ($n = 4, 6, \ldots$) alignment information in these distributions is clearly available, only the lowest ($n = 2$) term can be determined experimentally from a one-photon absorption study. Thus, we focus on the $a_2$ alignment values, calculated from the expectation value of $P_2(\cos \theta)$, i.e.,

$$a_2 = 5\langle P_2(\cos \theta) \rangle = \frac{5}{N_{\text{sim}}} \sum_{i=1}^{N_{\text{sim}}} P_2(\cos \theta_i) \quad (4.4)$$

where $N_{\text{sim}} = 2000-5000$ represents the number of trajectories averaged. As expected, all odd moments of the Legendre expansion explicitly vanish within statistical uncertainty for all multicollision simulations. Since each rotor in a simulation has undergone multiple collisions with He, the net $a_2$ alignment of the ensemble is obtained by calculating $\langle P_2 \rangle$ over all of the multicollision simulations at that collision number. The net result is the $a_2$ alignment as a function of number of collisions for each ensemble of trajectories. For comparison with experimental results, the quantum mechanical quantity $A_0^{(2)}$ approaches $\frac{5}{3}a_2$ in the high-$j$, semiclassical limit.²
4.3 Results

4.3.1 Multicollision alignment

In this subsection, the results of the multicollision simulations are presented, with a focus on i) the rate with which the alignment develops with collision number, and ii) how the magnitude of this alignment depends on collision energy and potential. To make things simpler, we focus initially on the He + O₂ simulations, which provide the least computationally intensive system for sampling and testing various parameters. As described in Sect. 4.2, the a₂ alignment parameter can be calculated as a function of the number of collisions (N_{coll}) by averaging P₂(cosθ) for each collision over all simulations within a given ensemble. It is more meaningful to renormalize N_{coll} to the effective number of hard-sphere collisions by

\[ Z_{\text{eff}} = N_{\text{coll}} \sigma / (\pi b_{\text{max}}^2) \]  

where σ represents the effective hard-sphere collision cross section at each collision energy as determined from the potential (see Table 4.1) and b_{max} is the maximum impact parameter sampled.

A plot of a₂ for the three collision energies (266 cm⁻¹, 89 cm⁻¹, and 18 cm⁻¹) is presented in Fig. 4.3 as a function of Z_{eff}. First of all, within statistical error, the alignment parameter decreases more or less smoothly from isotropic (i.e., a₂ ≈ 0) to an asymptotic value near a₂ ≈ -0.4. The negative sign of this asymptotic alignment is in good agreement with experiment and indeed confirms that more molecules are
Figure 4.3. A plot of the alignment of He + O₂ versus effective collision number (Z_{eff}) at three collision energies: 266 cm⁻¹, 89 cm⁻¹, and 18 cm⁻¹. The three traces demonstrate a remarkable insensitivity to collision energy: all three reach asymptotic alignments within 30% of each other, despite a 15-fold variation in collision energy.

aligned with \( j \) perpendicular than \( j \) parallel to the collision axis. Secondly, this asymptotic behavior is typically achieved in \( \leq 10 \) effective hard sphere collisions. Finally, even though the final rotational distributions vary dramatically for the three collision energies, the asymptotic alignments are within \( \approx 30\% \). In other words, the classical magnitude of the final rotor alignment is rather insensitive to collision energy.
For a quantitative comparison of these He + O$_2$ alignment results with the other potentials, the alignment versus collision number has been fit to a rising exponential of the form $a_2 = a_2^\infty \left[1-e^{-Z_{\text{eff}}/\beta}\right]$, where $a_2^\infty$ corresponds to the asymptotic value of $a_2$ and $\beta$ corresponds to the number of collisions to achieve $(1-1/e) \approx 63\%$ of this asymptotic alignment. The results of these fits for simulations on all three potentials are summarized in Figs. 4.4a and b. As expected, $a_2^\infty < 0$ for all potentials, indicating a net excess of rotors with $j$ perpendicular versus parallel to the expansion axis. Moreover, the asymptotic alignments obtained for all three potentials (but most especially He + O$_2$ and He + CO) reflect a surprising insensitivity to a nearly 15-fold change in collision energy. However, significant variations are observed when comparing results between different potentials, specifically in i) the magnitude of asymptotic alignment ($a_2^\infty$) and ii) $\beta$, the 1/e number of collisions required to reach this alignment. For example, $|a_2^\infty|$ increases substantially from O$_2$ to CO to CO$_2$. Furthermore, roughly an order of magnitude as many collisions are required to reach these asymptotic alignment values for CO versus O$_2$ and CO$_2$.

Closer inspection of the three collision potentials indicates angular anisotropy to be the source of these effects, i.e., the variation in $R$ on a given isoenergy contour for a full revolution of the rotor (see Fig. 4.2). In particular, this angular anisotropy increases from He-O$_2$ to He-CO to He-CO$_2$: the zero-energy contour for He-O$_2$ varies by only $\Delta R \approx 0.4$ Å, which should be compared with the much larger anisotropy values of $\approx 0.8$ Å and $1.0$ Å exhibited for He-CO and He-CO$_2$ potentials, respectively. Since this angular anisotropy is the only way the dynamics distinguish side versus
Figure 4.4. Results of fitting the alignment versus collision number data for He + O₂, CO₂, and CO to $a_2 = a_2^\infty \left[1 - e^{-Z_{eff}/\beta}\right]$. Errors bars correspond to $\pm 2\sigma$ in the fit. a) The asymptotic alignment, $a_2^\infty$, is insensitive to collision energy for all three potentials and increases from O₂ to CO to CO₂, reflecting the increased anisotropy of the potentials (see Fig. 4.2). b) $\beta$, the number of collisions to achieve $(1-1/e) \approx 63\%$ of this asymptotic alignment, increases dramatically from He + O₂/CO₂ to He + CO, reflecting presence of odd terms in addition to even terms of a Legendre expansion of the He + CO potential.
end-on collisions, one therefore expects and observes the net alignment to increase from He + O\textsubscript{2} to He + CO/CO\textsubscript{2}.

Also notable is the substantial *decrease* in alignment for the lowest energy collisions of He + CO\textsubscript{2} versus the relatively energy independent alignments observed for He + CO and He + O\textsubscript{2} (see Fig. 4.4a). This effect can be attributed to the greater well depth for He-CO\textsubscript{2}.\textsuperscript{64-66} Since 18-cm\textsuperscript{-1} collision energies correspond to less than half the depth of the He-CO\textsubscript{2} well, one expects far more long-lived collisions than observed for He-O\textsubscript{2} and He-CO. The presence of such “sticky” collision trajectories ultimately results in memory loss of the initial direction of the relative velocity vector, thereby diminishing the net alignment.\textsuperscript{63} Indeed, additional He + O\textsubscript{2} trajectories have been performed at $E_{\text{com}} = 9$ cm\textsuperscript{-1} (i.e., less than half the He-O\textsubscript{2} well depth) that indicate resulting O\textsubscript{2} alignments to be similarly reduced at these lower collision energies. In general, however, these results indicate a remarkably low sensitivity to collision energy, which motivates our focus on trajectory ensembles at a single collision energy in the following sections.

More striking is the large difference in rates at which these three systems come to the asymptotic alignment value, as seen in Fig. 4.4b. While the asymptotic alignment magnitudes can be rationalized by anisotropy differences in the potentials, the reason for the larger number of collisions needed to align CO is less apparent. However, one feature of the CO potential that distinguishes it from the others is the asymmetry of the two rotor ends, which contributes additional odd versus even terms in the Legendre expansion of the potential. As a result, the potential is significantly asymmetric with respect to He-CO and He-OC configurations, with a well closer to
the C end. In addition, the shift between the bond midpoint and center of mass makes the CO rotational axis asymmetric with respect to hard-sphere potential edges of the O and C atoms. A slowly approaching He atom therefore preferentially collides with the C end of the rotor, sampling the potential well region non-uniformly. This asymmetric sampling consequently requires a much larger number of collisions for CO to reach asymptotic alignment than for either CO$_2$ or O$_2$.

4.3.2 Dependence on Rotor Angular Momentum

As mentioned in Sect. 4.1, several experimental studies indicate a dependence of alignment on final rotational quantum state. Both Hefter et al.$^{49}$ and Weida and Nesbitt$^{56}$ have found alignment to increase with $j$; interestingly, this alignment appears to vanish when extrapolated to $j = 0$, which has led to the suggestion that this $j$-dependence might result from the $2j + 1$ quantum mechanical degeneracy of the rotational level. Indeed, a simple geometric model based on these ideas qualitatively predicts a monotonic increase in $A_0^{(2)}$ to an asymptotic value with $j$.$^{56}$ This makes it especially intriguing to see if these $j$-dependent trends are reproduced from a purely classical perspective.

To illustrate how the alignment depends on the rotor angular momentum, $j$, we again focus on the He + O$_2$ ensemble data at a single collision energy (266 cm$^{-1}$), though similar trends at all other collision energies are observed as well. As described previously, $a_2$ is calculated after each collision by averaging $P_2$ over all of the multicollision simulations. However, prior to the calculation of $a_2$, each rotor is first sorted into a bin according to its postcollision angular momentum, $j$. Three bin
ranges are chosen to examine the alignment behavior at “low,” “intermediate,” and “high” j values relative to a 300 K distribution. These bins are j/<j> = 0.0-0.4, 0.8-1.2, and 1.6-2.0 (where <j> = 10.2 for O₂ at 300 K) and correspond to the darkened regions shown in Fig. 4.5. At each collision number in a multicollision ensemble, the j-dependent alignment is extracted from <P₂> for all the rotors in a given j bin.

**Figure 4.5.** The distribution of rotor angular momenta (j) after a single collision at 266 cm⁻¹ (300 K). This is divided into “low” (j/<j> = 0.0-0.4), “intermediate” (j/<j> = 0.8-1.2), and “high” (j/<j> = 1.6-2.0) angular momentum bins for calculating the alignment dependence on j.
A plot of this j-dependent alignment of O$_2$ as a function of collision number is given in Fig. 4.6. Notably, the asymptotic alignment depends quite strongly on j, starting at essentially zero (within uncertainty) for the lowest range of j values and becoming increasingly negative with increasing j. This result is consistent with the work of Weida and Nesbitt in He + CO$_2$ coexpansions,\textsuperscript{56} as well as the work of Hefter \textit{et al.} in Na + Na$_2$ expansions.\textsuperscript{49} This is a particularly interesting result to obtain from purely classical calculations, since vanishing alignment at low j has previously been rationalized in terms of j-dependent degeneracies.\textsuperscript{56} However, there is a similar j-dependence in the semiclassical density of rotational states, which also vanishes in the limit of j = 0. Thus, while it is not surprising that such alignment trends can be reproduced by purely classical trajectory calculations, this will necessitate further discussion in Sect. 4.4 of alternative, non-quantum mechanical explanations for this j-dependence.

With the j-dependent alignments corroborated by He + O$_2$ simulations, we extend our study to the other two potentials. Specifically, the distributions of a$_2$ versus collision number are sorted into the same j/$\langle j \rangle$ bins for the multicollision ensembles of He + CO and He + CO$_2$ at 266 cm$^{-1}$ (with $\langle j \rangle$ = 8.8 and 20.0 at 300 K for CO and CO$_2$, respectively) and fit to a rising exponential. The results of this fit, given in Fig. 4.7, show that the trends are the same for all three potentials, with the alignment monotonically increasing with rotor angular momentum. The variation in magnitude among potentials within each j/$\langle j \rangle$ range simply reflects the variation in overall alignment noted previously in Fig. 4.4a.
Figure 4.6. Alignment ($a_2$) as a function of effective collision number ($Z_{\text{eff}}$) for low ($j/\langle j \rangle = 0-0.4$), intermediate ($j/\langle j \rangle = 0.8-1.2$), and high ($j/\langle j \rangle = 1.6-2.0$) angular momentum values for the He + O$_2$ collision system. The magnitude of the asymptotic alignment increases with $j$ in this system.
Figure 4.7. Asymptotic alignment ($a_2^\infty$) for He + O$_2$, CO, and CO$_2$ for low ($j/\langle j \rangle = 0-0.4$), intermediate ($j/\langle j \rangle = 0.8-1.2$), and high ($j/\langle j \rangle = 1.6-2.0$) angular momentum values. Error bars represent $\pm 2\sigma$ in the exponential fit. While the magnitudes of the alignments vary among the potentials, the trend for all three potentials is that alignment increases with $j$. 
The next step is to investigate how this alignment is created, specifically by identifying correlations between initial and final states in the production of an aligned distribution. One important observation in this regard is evident in Fig. 4.4b, i.e., the alignment grows in gradually over several collisions. Thus, one plausible mechanism is that the incoming alignment of a rotor molecule (i.e., classically \( m/\ell \)) influences the probability of a given final alignment. From this perspective, the rotor alignment is formed by a series of \( m/\ell \)-changing collisions that ultimately funnel the angular momentum states into an aligned distribution. To explore this possibility, the individual collision trajectories are analyzed to obtain a probability map for all \( (m/j)_{i} \rightarrow (m/j)_{f} \) transitions. In order to improve the statistics, approximately 500,000 single-collision simulations are included for each of the potentials. Furthermore, the single-collision \( (m/j)_{i} \rightarrow (m/j)_{f} \) distributions are additionally split into the same \( j/\langle j \rangle \) bins used above, but where \( j \) now refers to the angular momentum state prior to the collision.

Sample He + O\(_2\) probability maps of \( (m/j)_{f} \) versus \( (m/j)_{i} \) for the three ranges of \( j/\langle j \rangle \) are presented in Fig. 4.8 and indicate several features worth noting. First of all, for the lowest values of \( j/\langle j \rangle \) (Fig. 4.8a), single collisions from each \( (m/j)_{i} \) produce a large spread in \( (m/j)_{f} \), i.e., little correlation exists between the initial alignment of an O\(_2\) molecule and its final alignment after a collision. However, as \( j \) increases from Fig. 4.8a to c, this spread in \( (m/j)_{f} \) for a given \( (m/j)_{i} \) narrows dramatically, collapsing into a tight band along \( (m/j)_{f} \approx (m/j)_{i} \). Thus, the rotor’s initial alignment with respect to the collision axis is largely conserved for high \( j \).
Figure 4.8. Plot of initial $m/j$ versus final $m/j$ for an ensemble of 500,000 He + O$_2$ collisions at 266 cm$^{-1}$ for a) low ($j/<j> = 0-0.4$), b) intermediate ($j/<j> = 0.8-1.2$), and c) high ($j/<j> = 1.6-2.0$) angular momentum values. As $j/<j>$ increases, the spread in $(m_j/j_f)$ for each $(m_j/j_i)$ narrows considerably, reflecting the increased gyroscopic stability of higher $j$ states.
This result is not limited to the He + O$_2$ system: He + CO and He + CO$_2$ studies also demonstrate that the spread in (m$_j$/j)$_f$ decreases by roughly an order of magnitude from the lowest to the highest j range. Simply stated, single collisions are far less effective at scrambling molecular alignment at high j than low j; this physically reflects the increased gyroscopic stability of more rapidly spinning rotor molecules. This also begins to explain the strong j dependence of the asymptotic alignments observed, since any alignment created by a series of collisions is far more easily erased by additional collisions for low j than for high j rotors.

The next stage in investigating how alignment is created is to determine the types of collisions that change m$_j$/j, i.e., to explore whether m$_j$- or j-changing collisions predominate. To this end, the single-collision He + O$_2$ trajectories are sorted by size of the collisional change in m$_j$ (i.e., $\Delta m_j$) and in j (i.e., $\Delta j$); the resulting distributions can be analyzed by i) what fraction of collisions produce significant changes in m$_j$ or j and ii) the magnitude of these changes. To facilitate this comparison, “non-collisional” events are excluded by limiting the maximum impact parameter to be the average hard-sphere collision radius of O$_2$ (2.9 Å), and both $\Delta m_j$ and $\Delta j$ are scaled by $\langle j \rangle$. Figure 4.9 reports histograms of the resulting distributions. Notably, >70% of the collisions produce non-negligible changes for both m$_j$ and j (i.e., greater than 5% of $\langle j \rangle$). More importantly, the $\Delta m_j$ and $\Delta j$ distributions are quite similar, implying that neither type of collision predominates in developing the rotor alignment. The relevance of this finding to previous studies will be explored in Sect. 4.4.
Figure 4.9. Distributions of a) $\Delta m_j / \langle j \rangle$ and b) $\Delta j / \langle j \rangle$ for an ensemble of 500,000 He + O$_2$ collisions at 266 cm$^{-1}$. The similarity in these distributions indicates that both $\Delta m_j \neq 0$ and $\Delta j \neq 0$ collisions are significant in creating alignment.
4.3.3 Velocity dependence

In addition to providing insight into j-dependent alignment, the single-collision regime can be used to examine the dependence of the alignment on the final rotor velocity. Indeed, discrepancies between the studies of Aquilanti et al.\textsuperscript{58} and Harich and Wodtke\textsuperscript{57} on this velocity dependence provided the initial incentive for these calculations, specifically to address whether subtle differences in the two intermolecular surfaces could be responsible for such clear differences in experimental results.

Since the multicollision simulations demonstrate the alignment to be insensitive to collision energy, we simply consider the 500,000-trajectory, single-collision ensembles at 266 cm\textsuperscript{-1} (300 K) for each potential. To carry out this comparison, the change in rotor velocity component along the expansion axis (i.e., from zero initially to its post-collision value) is recorded for each trajectory. The average final velocity (normalized to the velocity predicted for a head-on elastic collision) is then calculated for each bin of (m j/j)\textsubscript{f}. In order to prevent statistical skewing by non-collisions at large impact parameter, we exclude events with a final velocity \( \leq 10\% \) of the elastic upper limit. To examine the results for a possible j-dependence, the single-collision data are separated into j bins defined previously.

Fig. 4.10 contains a plot of the post-collision rotor velocity versus final m/j state, with the velocity expressed as a percent difference from the average final velocity integrated over all alignments, i.e., \( \Delta v/<v> \). The upward curvature at the ends of this distribution clearly demonstrates that on average, molecules with \( |m/j| \approx 1 \) are faster than \( |m/j| \approx 0 \). Stated explicitly, molecules with j \textit{parallel} to the
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Figure 4.10. The percent difference of the final rotor velocity from the alignment–averaged final rotor velocity, $\Delta v/<v>$ versus $(m_j/j)_f$. The data are binned by $(j/j_f)$ and He + rotor potential as follows: ● = 0.0-0.4, He + O$_2$; ▲ = 0.8-1.2, He + O$_2$; ■ = 1.6-2.0, He + O$_2$; ○ = 0.0-0.4, He + CO; △ = 0.8-1.2, He + CO; □ = 1.6-2.0, He + CO. Error bars represent $\pm 2\sigma$ of the mean. The upward curvature of this data indicates that, on average, molecules with $|m_j/j_f| \approx 1$ (i.e., $j$ parallel to the collision axis) are faster than those with $|m_j/j_f| \approx 0$ (i.e., $j$ perpendicular). This trend is the same for all potentials and ranges of $j$ shown.
expansion axis are on average moving faster than those with \( j \) perpendicular, with a roughly 15% spread in velocity around the average velocity after a single collision. In addition, this velocity-dependent alignment is virtually identical for He + O\(_2\) and He + CO, thus ruling out any major dependence on subtle differences in the two intermolecular potentials. Furthermore, this trend is robustly independent of angular momentum, i.e., the data for all \( j \) ranges in Fig. 4.10 overlap within statistical uncertainties. In summary, these calculations predict the faster (slower) rotor molecules to exhibit a more positive (negative) alignment, i.e., \( j \) preferentially parallel (perpendicular) to the expansion axis, with little sensitivity to the interaction potential or rotational quantum number.

These velocity-dependent trends are most consistent with the results of Harich and Wodtke. To quantify the comparison between theory and experiment, Harich and Wodtke’s velocity dependent alignment data for He + CO(\( j=6 \)) have been reanalyzed as a classical distribution of \( m_j/j \) states as a function of final velocity. For each \( m_j/j \), an average final rotor velocity is calculated and plotted in Fig. 4.11 as \( \Delta v/\langle v \rangle \). Superimposed on this line is the final velocity distribution of rotor molecules obtained from our calculations, averaging over all \( j \) values and both potentials. The trends in the experimental and calculated data are clearly quite similar: molecules aligned with \( j \) perpendicular to the collision axis (\( |m_j/j| = 0 \)) travel more slowly than those with \( j \) parallel (\( |m_j/j| = 1 \)). The implications of these results will be further developed below.
Figure 4.11. Comparison of the experimental jet-expansion data of Harich and Wodtke to the overall average $\Delta v/\langle v \rangle$ versus $(m_j/j)_f$ obtained by averaging the classical-trajectory data in Fig. 4.11 over all $j$ and both potentials. Both the multicollision experimental results and the single-collision classical trajectories demonstrate the same trend: on average, molecules with $|m_j/j_f| \approx 1$ are faster than those with $|m_j/j_f| = 0.$
4.4 Discussion

Several of the results obtained in this study warrant further discussion. First of all, the overall trends in the theoretical alignments are in excellent agreement with experiment. The multicollision simulations predict $a_2 < 0$ for all potentials, supporting the simple picture that rotor molecules with $j$ parallel to the expansion axis present a larger cross section to the colliding He diluent and thus are more likely to experience realigning collisions. Somewhat more surprisingly, this alignment appears to be quite insensitive to collision energy. Specifically, the asymptotic alignments indicate less than 40% changes over an order of magnitude range in $E_{\text{com}}$ for all three collision systems tested. Indeed, only at energies significantly lower than the well depth for each collision system do the alignments decrease noticeably, a trend that can be ascribed to increased probability of long-lived versus direct collision trajectories. This indicates that high velocity slip conditions (e.g., at the throat of the expansion) or much slower collisions (e.g., further downstream) can both contribute to the rotor alignment, provided that the relative velocities are sufficiently well aligned with respect to the expansion axis. This is especially relevant to comparisons between experimental results, where different expansion conditions yield different final jet temperatures, velocity slips, and thus relative scalar speeds of the diluent gas and rotor species.

In the multicollision ensembles, the maximum alignments ranged from a lower limit of $a_2 \approx -0.46(1)$ (for He + O$_2$), to $a_2 \approx -0.73(1)$ (for He + CO), to the highest value of $a_2 \approx -1.03(1)$ (for He + CO$_2$). By way of contrast, experimental studies for He + CO$_2$ indicate maximum CO$_2$ alignment of $A_0^{(2)} \approx -0.115$,$^{56}$ which in
the classical limit corresponds to $a_2 = -0.29$, i.e., ≈ threefold smaller than obtained from the current work. Similarly, the experimental CO alignment (integrated over all velocities) for He + CO studies is $A_0^{(2)} = -0.08$; this corresponds classically to $a_2 = -0.2$, which is also roughly threefold smaller than suggested by the multicollision simulations. In essence, despite excellent qualitative agreement for alignment trends as a function of both velocity and rotor angular momentum, the maximum alignment values theoretically predicted are quantitatively much higher than those measured experimentally.

These discrepancies reflect the different nature of collisions in the simulations versus the jet expansions. In the theoretical simulations, all collisions occur at the same center of mass energy and are directed initially along the expansion axis. In contrast, the collisions in a supersonic expansion take place over a range of relative energies as the molecules cool and, more importantly, over a wider range of collision angles. The distribution of relative energies is not responsible for these differences, since the alignment results are quite insensitive to collision energy. Likely to be much more relevant is the subsequent influence of this cooling on the distribution of collision velocities in the expansion. At large values of velocity slip, most diluent gas-seed gas collisions are strongly aligned along the expansion axis; however, as this velocity slip approaches zero, collisions with the seed gas molecule will be far less aligned. For example, the studies of Weida and Nesbitt indicate that velocity slip for CO$_2$ in the late stages of a He + CO$_2$ expansion is as low as a few percent; thus, most collisions are essentially isotropic with respect to the laboratory-frame expansion axis. This excess of non-directional collisions can lead to efficient scrambling of the
rotational alignment produced up to that stage; indeed, Halpern et al.\textsuperscript{70} and Schade et al.\textsuperscript{71} have demonstrated such collisional loss of alignment for acetylene and NO, respectively. This effect has been explicitly noted in the He + CO\textsubscript{2} studies: as a function of distance downstream, the net CO\textsubscript{2} alignment reaches a maximum and then steadily decreases due to nominally unaligned collisions late in the expansion. The neglect of velocity slip/angular effects in the current theoretical studies clearly leads to an overestimation of the asymptotic alignment values, i.e., in the direction consistent with the observed differences.

Despite these quantitative differences between the magnitudes of theoretical and experimental alignments, the agreement is qualitatively quite good and provides support for a closer examination of the underlying alignment mechanism. For example, when alignment is further partitioned by rotor angular momentum, the classical trajectory simulations demonstrate that the asymptotic values increase monotonically with j for each of the three intermolecular potentials. Contrary to previous interpretations, this j-dependent alignment can not be ascribed entirely to quantum effects contributing at low j, since the same trends are clearly evident also in classical trajectory calculations. This j dependence is most likely due to increased gyroscopic stability, i.e., the faster a classical rotor is spinning, the more stability it exhibits toward collisional torques changing the alignment. This point is most dramatically made in Figs. 4.6a-c, which indicate a significant decrease in the distribution of \( m_j / j \) with increase in j after a single collision. As a result, once high-j molecules become aligned, they are less likely to be tilted away from this alignment by subsequent collisions. This concept of the stability of higher j states against \( m_j / j \)-
changing collisions is supported by studies of pressure-broadening coefficients, which generally indicate a rapid decrease with increasing j state.\textsuperscript{72-76} Furthermore, Hulsman and Korving report that cross sections for reorienting collisions between Ar and Na\textsubscript{2} decrease strongly with angular momentum, with a dependence nearly proportional to $1/j^2$.\textsuperscript{50}

This discussion of j-dependent alignments would seem to suggest that multiple, m\textsubscript{j}-changing collisions are the primary mechanism for alignment in supersonic expansions. Indeed, previous work by Weida and Nesbitt\textsuperscript{56} demonstrates that alignment of CO\textsubscript{2} in a supersonic expansion becomes increasingly negative with j, a phenomenon they attribute to m\textsubscript{j}-changing collisions. Likewise, a quantum close-coupled calculation by Werner and coworkers\textsuperscript{77} on collisional alignment of N\textsubscript{2}\textsuperscript{+} ions with He demonstrate cross sections for m\textsubscript{j}-changing collisions (at fixed j) that are significantly larger than j-changing collisions (at fixed m\textsubscript{j}). Consequently, the alignment observed by Dressler \textit{et al.}\textsuperscript{78} in the corresponding He drift tube experiment has been attributed to m\textsubscript{j}-changing collisions at more or less fixed j. More recent work by Anthony \textit{et al.} on these He-N\textsubscript{2}\textsuperscript{+} drift tube experiments demonstrates that the most negative alignments occur at high j.\textsuperscript{79}

Herschbach and coworkers have developed an alternate explanation of the collisional alignment involving j-changing collisions. Experimentally, they monitor alignment of I\textsubscript{2} as a function of final jet temperature, observing that as the final temperature decreases, the negative alignment of a given j state reaches a maximum and begins to decrease again, eventually becoming positive under certain expansion conditions.\textsuperscript{54} They ascribe this phenomenon to a contribution from \textit{anisotropic}
rotational cooling: molecules with $j$ perpendicular to the collision axis experience a greater torque than those with $j$ parallel and are thus cooled more rapidly. Consequently, this would predict an excess of rotors with $j$ predominantly perpendicular to the expansion axis at low $j$ (i.e., cooler temperatures) and relatively fewer molecules with $j$ perpendicular in the high $j$ states, and thus a net $a_2$ alignment that becomes more positive with increasing $j$. Since the collision energy used in each of our calculations is the mean temperature used to sample the rotational distribution (i.e., the two are roughly equivalent), these studies cannot directly assess the validity of the anisotropic rotational cooling model relative to the other models. However, it is clear from Fig. 4.9 that both $m_j$- and $j$-changing collisions are occurring at similar frequencies and contribute to the $m_j/j$ alignment.

The velocity-dependent alignments presented in Fig. 4.10 demonstrate several interesting points. First of all, the sign of the resulting velocity-averaged alignment is correctly predicted to be negative, irrespective of the magnitude of the velocity slip. However, when one investigates alignment as a function of deviations away from the average speed, the results are more subtle. Specifically, the rotor molecules moving faster than the average ($\Delta v > 0$) have a greater propensity for $j$ perpendicular to the expansion axis than the more slowly moving velocity groups ($\Delta v < 0$). Most importantly, this behavior is exhibited for all values of $j$ for both He + CO and He + O$_2$ collision systems and so does not appear to be sensitive to the detailed shape of the intermolecular potential. Over multiple collisions in a supersonic expansion, this effect predicts a net negative alignment ($a_2 < 0$) for the slower rotor molecules and positive alignment ($a_2 > 0$) for the faster molecules, i.e., exactly the same trend
reported by Harich and Wodtke in supersonic expansions of He + CO. Such behavior supports the simple physical picture discussed by Harich and Wodtke that rotor molecules with $j$ parallel to the expansion axis present a larger collisional cross section to the diluent gas, preferentially experiencing more directed collisions and hence more forward acceleration with respect to the average rotor speed.

In further support of this interpretation, both the computational results and the work of Harich and Wodtke can be compared with the work of Anthony et al. on velocity-resolved collision-induced alignment of $N_2^+$ in a He drift tube.\textsuperscript{79,80} Interestingly, these studies reveal that faster $N_2^+$ drift velocities are associated with more negative alignment (the alignment even becomes positive at the lowest velocities for the lowest $j$ values). At first glance, this greater propensity for $j$ perpendicular versus $j$ parallel to the drift axis at the highest ion velocities would appear to be in disagreement with both the supersonic jet He + CO studies and the current theoretical results. However, as pointed out by Harich and Wodtke, the rotor molecules in supersonic expansions are \textit{accelerated} by collisions with the faster-moving diluent gas, while the ions in a drift tube, pulled through the buffer gas by an external electric field, are \textit{decelerated} by collisions with the buffer. As a result, the fast end of the velocity distribution reflects those ions which have suffered fewer collisions, which is therefore consistent with the more negative alignments (i.e., $j$ perpendicular preferred over $j$ parallel) observed experimentally at higher velocities.

By way of contrast, experiments on He + O\textsubscript{2} and He + N\textsubscript{2} by Aquilanti and coworkers indicate that alignment in a supersonic expansion becomes more negative for the higher velocity molecules, i.e., the concentration of rotors with $j$ perpendicular
to the expansion axis increases with $\Delta v > 0$. This is qualitatively different from the He + CO results of Harich and Wodtke, the He + N$_2^+$ ion alignment studies of Anthony et al., and the theoretical predictions from the current work. There are at least two factors that should be considered as possible sources for this discrepancy. First of all, not all the experiments of Aquilanti and coworkers have been performed on collision systems (e.g., He + N$_2$) sampled in other studies. However, the theoretical results obtained in this work are robustly independent of the intermolecular potential for all three systems (He + CO, He + O$_2$, He + CO$_2$); it would be quite surprising if the behavior for He + N$_2$ were somehow significantly different. Furthermore, the theoretical trends observed in the current study for the two systems investigated by Harich and Wodtke and Aquilanti and coworkers, i.e., He + CO and He + O$_2$, are essentially identical.

Secondly, the experiments on He + O$_2$ by Aquilanti and coworkers have been performed under much stronger expansion conditions, thus sampling lower $j$ values than in the He + CO experiments. In this regard, it is worth noting that calculations in this work have been carried out over nearly a 15-fold range of jet temperatures, though none as low as Aquilanti and coworkers. Indeed, quantum cross section calculations have been performed by Aquilanti and coworkers for the He-O$_2$ collision system$^{81}$ in which authors attribute the quite different velocity effects between their studies and those of Harich and Wodtke to differences in expansion conditions. Specifically, Aquilanti and coworkers probe in only a very small solid angle along the forward-/backward-scattered direction while Harich and Wodtke necessarily average over a broader range of angles. Therefore, one possible explanation might be that the
different scattering angles sampled in the two experiments produce different velocity-dependent alignments. However, this would also suggest a strong dependence of these velocity effects on impact parameter, whereas our calculations indicate essentially identical alignment trends (i.e., \( j \) perpendicular faster than \( j \) parallel) for all impact parameters, with \( b_{\text{max}} \) as low as 0.1 Å. In essence, these classical trajectory calculations do not provide a satisfactory explanation for the experimental discrepancies in velocity dependent alignments but do indicate that differences in scattering for the two intermolecular potentials (He + O\(_2\) vs. He + CO) are not sufficient to resolve this issue.

4.5 Summary

Classical trajectory calculations have been carried out on experimentally determined potentials for He-O\(_2\), He-CO, and He-CO\(_2\) to explore the collisional mechanism for rotational alignment and to facilitate comparison with previous experimental studies. These calculations demonstrate that for multiple collisions between a light “diluent” gas, He, and a heavy “seed” rotor, the rotor molecules become anisotropically aligned with a clear propensity towards \( j \) perpendicular to the expansion axis. This alignment grows in with an approximately exponential dependence on the number of collisions and a 1/e collision number that varies from \( \approx 2 \) to 30. The sign and magnitude of this asymptotic alignment are found to be remarkably insensitive to collision energy over more than an order of magnitude dynamic range, as well as to the detailed shape of the interaction potential.
In addition to this examination of the overall alignment from multiple-collision simulations, j-dependent effects have also been explored. These simulations reveal the asymptotic alignment to depend strongly on rotor angular momentum, increasing in magnitude with j for all three potentials studied and conversely vanishing as j tends toward zero. The evidence of this behavior in a purely classical simulation indicates that experimental trends of vanishing alignment for low j states cannot be simply ascribed to quantum effects near j = 0. Investigated on a collision-by-collision basis, the higher j states appear to be far more stable with respect to collisional destruction of the alignment. Specifically, the statistical spread in the final alignment \( (m_j/j)_f \) for a given initial alignment \( (m_j/j)_i \) narrows dramatically with j, consistent with the simple physical picture of greater classical gyroscopic stability for more rapidly spinning rotors.

With regard to velocity dependent alignments, the calculations indicate that molecules moving faster than the average velocity have their angular momenta preferentially aligned parallel to the expansion axis, in agreement with the experimental observations of He + CO collisions by Harich and Wodtke. This provides theoretical support for this physical picture of the alignment process: rotor molecules with \( j \) parallel to the relative velocity axis are struck from behind more often by seed gas molecules than rotors with \( j \) perpendicular to this axis and thus are preferentially accelerated ahead of the average rotor velocity distribution. These simple models are also consistent with the velocity dependent He + \( \text{N}_2^+ \) ion drift experiments of Anthony et al. but as yet do not appear to be consistent with the behavior reported by Aquilanti for He + O\(_2\) and He + \( \text{N}_2\) collision dynamics.
References for Chapter 4


69. NAG Fortran Library (Oxford University: Oxford, 1997)


81. Aquilanti, V., private communication
CHAPTER 5
EXPLORING THE ROLE OF VIBRATIONAL NONADIABATIC EFFECTS IN VIBRATIONALLY MEDIATED CHEMICAL REACTIONS

5.1 Introduction

Over the past decade, the possibility of influencing chemical reactions by vibrationally mediated chemistry has enjoyed a great deal of interest and success. Originally pioneered by Crim and coworkers and Zare and coworkers for the reaction of H with water and its isotopes, it has since been extend to variety of reactive atoms (H, Cl, O) and molecular reaction partners (H₂O/HOD, HCN, CH₄). Such systems provide the tantalizing possibility of pre-excitation of a particular bond in a molecule leading to selective reaction.

One means of exploring the degree of selectivity imparted by vibrational excitation has been to examine the branching ratios among possible products. For example, in the reaction of H with vibrationally excited HOD, Bronikowski showed that the relative branching ratio for OD/OH production was at least 25 from v_{OH}=1, while the branching ratio for OH/OD was at least 8 from v_{OD}=1. Similar effects have been demonstrated for the reaction of HOD with other atoms and at other levels.
of vibrational excitation, both experimentally\(^2-7\) and theoretically\(^{14-20}\). In addition, the Crim group’s studies of nearly isoenergetic vibrational states of \(\text{H}_2\text{O}\) containing differing amounts of local-mode stretch and bend excitation demonstrated increased reactivity with \(\text{H}\) atoms when all quanta were placed in the stretch excitation\(^2,3\).

Another approach to determining vibrational selectivity has been to monitor how excitation in the nonreactive bond translates into product-state excitation. For example, the Crim group monitored the OH vibrational states resulting from reaction of \(\text{H}\) and \(\text{Cl}\) atoms with \(\text{H}_2\text{O}\) in two states, \(|04\rangle\) and \(|13\rangle\), where \(|nm^{(\pm)}\rangle\) denotes symmetric and antisymmetric combinations, respectively, of local mode stretches with \(n\) quanta in one bond and \(m\) quanta in the other\(^3,4\). These studies revealed a marked propensity toward production of OH in \(v=0\) in the first case and OH in \(v=1\) in the second.

From these demonstrations of mode-specific reaction a “spectator bond” paradigm has emerged, i.e., the concept that the nonreactive bond does not participate in the reaction dynamics, and any initial excitation in that bond should be retained in the final product distribution. Underlying this paradigm is an assumption of vibrational adiabaticity in the reactive species, i.e., that the initial vibrational state prepared in the reactive molecule is essentially unaffected by the approach of the reactive atom. This view of these reaction systems has increased in popularity such that reduced-dimensionality 4-atom reactive scattering calculations often fix the length of the nonreactive bond\(^{21}\).

However, a significant amount of experimental and theoretical evidence demonstrates that the nonreactive bond may not always play the role of a spectator in
mode-specific reactions. Such an effect is quite dramatically demonstrated in recent experiments by the Crim group on Cl + HCN, which produced similar excitation of the product CN stretch from both Cl + HCN(004) and Cl + HCN(302), where the first quantum number corresponds to a normal mode of predominately CN stretch character, and the third to a normal mode of predominantly CN character. Their initial explanation for this phenomenon was that the Cl + HCN reaction proceeds via a complex, resulting in intramolecular vibrational redistribution (IVR) prior to reaction. However, Schatz and coworkers have carried out quantum scattering calculations on the related H + HCN reaction which allow the CN bond to vibrate while constraining HHC to be collinear, a geometry that removes the possibility of complex formation. They determine that excitation to HCN(100), i.e., one quantum of mostly CN stretch character, significantly enhances reaction cross section to H₂ + CN and lowers the threshold energy relative to H + HCN(000); in fact, this threshold decreases by nearly 100% of input vibrational energy.

Similar effects, albeit on a smaller scale, can be observed in the earlier studies of the reactivity of water and its isotopes mentioned previously. For example, Crim and coworkers noted a decrease in relative OH v=1/v=0 production from Cl + H₂O|13> versus H + H₂O|13>. Similarly, Schatz and coworkers noted in an early quasiclassical trajectory study that excitation of the OD bond in HOD or of highly excited bend states of H₂O (5-7 quanta) provides some enhancement of the H reactivity above the ground state. A later study by this group, examining lower levels of vibrational excitation in HOD, again demonstrated that excitation of the OD stretch, in addition to enhancing the reaction probability of the D atom, increases H
reactivity to a lesser extent. More recent 6D quantum calculations of H + HOD by Zhang and Light also indicate that excitation of the OD bond does cause a slight enhancement of reaction probability for the OH bond.

At the heart of these studies is the apparent breakdown of the local mode nature of the initial excitation of the reactant. The approach of the reactive atom must cause a redistribution of vibrational energy in the reactant molecule, occurring on the timescale of a chemical reaction. Correspondingly, the question emerges: what happens to the excited vibration as the atom approaches? In each of the previous studies, the primary focus has been on examining the product distribution rather than the details of the interaction of the atom with the molecular vibrations.

To address these issues, we explore vibrationally nonadiabatic effects in chemical reactions, focusing on a model system for the collinear reaction of Cl with reduced-dimensionality, linear water isotopes. Our first goal will be to determine in a time-independent fashion how the vibrational eigenfunctions of this model water system are affected as the Cl atom distance is parametrically decreased, focusing primarily on the v=1 stretch polyad in water. Our second goal will then be to follow the dynamics of the reaction in a time-dependent fashion via wavepacket propagation. In doing so, we hope to demonstrate the insight that can be gained from such a time-dependent approach.

5.2 Computational Approach

To study the reaction dynamics of Cl with water isotopes in various vibrational levels, the computational process can be divided up into three major steps.
For simplicity, these computations are primarily described for Cl + H\textsubscript{2}O but can be applied to the other systems to be studied, i.e., Cl + D\textsubscript{2}O and Cl + HOD (with the approach of the Cl atom along the OH bond). First, we calculate the eigenstates and eigenenergies of the water molecule as a parametric function of the Cl-H\textsubscript{2}O internuclear distance. In doing so, we assume that the vibrational motion is separable from the relative Cl + H\textsubscript{2}O motion, similar to the Born-Oppenheimer separation of nuclear and electronic motion,\textsuperscript{23} in order to calculate an adiabatic basis of vibrational eigenfunctions. Thus, the total wavefunction is composed of vibrational and internuclear parts,

\[ \Psi^{\text{total}} = \sum_n \Psi_n \chi_n \]  

(5.1)

where \( \Psi \) represents the total wavefunction, \( \psi \) represents the internuclear part, and \( \chi \) represents the vibrational part. The vibrational eigenstates, \( \chi_n \), are determined by solving the time-independent Schrödinger equation for the OH bonds with parametric dependence on the Cl-H\textsubscript{2}O distance:

\[ H(r_1, r_2; R) \chi_{n}^{\text{vib}}(r_1, r_2; R) = E_n(R) \chi_{n}^{\text{vib}}(r_1, r_2; R) \]  

(5.2)

where \( r_1 \) is the distance between the O atom and the H atom \textit{proximal} to the Cl, \( r_2 \) is the distance between the O atom and the H atom \textit{distal} to the Cl, and \( R \) is the distance from the Cl to the center of mass of the water. A plot of this coordinate system is given in Fig. 5.1. The changes in these eigenfunctions with \( R \) provide insight into
Figure 5.1. Coordinate system for Cl + HOH reactive scattering calculations. R represents the distance from the Cl atom to the center of mass of water, while \( r_1 \) is the length of the proximal OH bond (i.e., closest to the Cl), and \( r_2 \) is the length of the distal OH bond. With appropriate isotopic substitutions, this coordinate system is also used for Cl + DOD and Cl + HOD (replacing H with D on the distal OH bond).

how the water vibrations are affected by the approach of Cl. In addition, the \( E_n \)'s provide one-dimensional (1D) adiabatic potential surfaces for relative Cl-H\(_2\)O motion. Accordingly, along an *uncoupled* adiabatic potential curve, the Schrödinger equation describing the intermolecular Cl-H\(_2\)O motion can be exactly written as

\[
\left( \frac{-\hbar^2}{2\mu_{\text{Cl-HOH}}} \frac{\partial^2}{\partial R^2} + E_n(R) \right) \psi_n(R) = E\psi_n(R) \\
\]

In the second step of the computational process, we must be able to transfer probability among the adiabatic curves in order to allow for inelastic or reactive scattering. These curve-crossing probabilities are governed by the nonadiabatic terms in the intramolecular Hamiltonian, essentially, a breakdown in the separation between
vibrational and intermolecular motions. In this adiabatic basis, the couplings between
the curves depend on the rate of change of the vibrational eigenstates as a function of
$R$, thus depending on the velocity of approach of the Cl atom in a classical
interpretation. The transition probabilities can therefore be used to estimate a
characteristic curve-crossing velocity for the transition between low-velocity,
adiabatic behavior and high-velocity, diabatic behavior.

In the final step of the computational process, we carry out time-dependent
wavepacket propagation for the relative Cl-H$_2$O motion, starting with an initial
entrance channel (e.g. the symmetric or antisymmetric vibration of H$_2$O), following
the dynamics, and probing the products. These three steps are described in detail
below.

5.2.1. *Calculating vibrational wavefunctions at each Cl-water distance*

This calculation first requires a potential surface describing the interactions of
the four atoms, as well as means of representing and calculating the eigenfunctions.

The potential surface used to describe the Cl + H$_2$O interaction is based on the
triatomic O + HCl London-Eyring-Polanyi-Sato (LEPS) potential surface given by
Persky and Broida,$^{24}$ with parameters given in Table 5.1. This surface is used to
describe the interaction of one OH stretch with the approaching Cl; this stretch is
designated the “proximal” OH stretch, $r_1$. The other OH stretch is solely described
the Morse potential part of the LEPS surface and is designated the “distal” OH
stretch, $r_2$. Thus, in the subsequent calculations, the Cl atom is only allowed to
approach the proximal end of the molecule. Physically, this potential surface does
not accurately describe the Cl + H₂O interaction because products and reactants are nearly isoenergetic, while Cl + H₂O should be endothermic by 5640 cm⁻¹.²⁵ The surface was rather designed to lower artificially lower the reactive channels so that the reactive channels were more accessible at the ν=1 level, simplifying our computations by limiting the number of vibrational eigenfunctions calculated. Clearly, this feature of the potential surface, as well as the linear configuration chosen for water, indicates that no quantitative comparison with experiment will be made. Rather, this system will provide a simple model for the dynamics of reaction with a heavy-light-heavy molecule; in addition, we will discuss which conclusions are valid more universally.

Table 5.1. LEPS parameters for the Cl + H₂O potential surface.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>O-H</th>
<th>H-Cl</th>
<th>O-Cl</th>
</tr>
</thead>
<tbody>
<tr>
<td>β(Å⁻¹)</td>
<td>2.295</td>
<td>1.868</td>
<td>2.290</td>
</tr>
<tr>
<td>Δ (cm⁻¹)</td>
<td>37,230</td>
<td>37,250</td>
<td>23,600</td>
</tr>
<tr>
<td>rₑ(Å)</td>
<td>0.970</td>
<td>1.275</td>
<td>1.570</td>
</tr>
<tr>
<td>k</td>
<td>0.170</td>
<td>0.158</td>
<td>-0.250</td>
</tr>
<tr>
<td>r⁺</td>
<td>1.154</td>
<td>1.453</td>
<td></td>
</tr>
</tbody>
</table>

After choosing the potential surface for the four-atom interaction, a representation for the vibrational eigenfunctions, χₙ, must be designated. For this purpose, we use a Fourier expansion of the wavefunction on an evenly spaced grid,
such that the expansion coefficients are equivalent to the amplitude of the wavefunction in momentum space. The momentum wavefunction can thus be obtained via a Fourier transform of the coordinate wavefunction; with FFT techniques, the length of this computation scales as $N_g \log N_g$ ($N_g$ is the number of grid points). Such a representation takes advantage of the local nature of the kinetic energy operator in momentum space, where calculation of the kinetic energy operation requires only a simple multiplication step and scales as $N_g$. The complete Hamiltonian operation thus scales approximately as $N_g \log N_g$, rather than the $N_g^2$ typically necessary for calculating derivatives of the wavefunction in position space. Altogether, the Hamiltonian in the COM frame of H$_2$O for the vibrational eigenfunctions, with parametric dependence on the distance between the Cl and H$_2$O center of mass, is exactly given by

$$
H = T + V
$$

$$
V = V(r_1, r_2, R)
$$

$$
T = \hbar^2 \left[ \frac{-\partial^2}{2\mu_{OH} \partial r_1^2} + \frac{-\partial^2}{2\mu_{OH} \partial r_2^2} + \frac{\partial^2}{m_o \partial r_1 \partial r_2} \right]
$$

(5.4)

where $V$ is the potential energy from the LEPS potential, $T$ is the kinetic energy of the OH stretches, and $r_1$, $r_2$, and $R$ are as defined previously. The size of the grid chosen to represent these eigenfunctions is $16 \times 128$ points, with spacings $(\Delta r_1, \Delta r_2) = (0.079, 0.057) \text{ Å}$. The larger number of points in $r_1$ is designed to encompass both...
product and reactant wells; the spatial extent represented is thus \((r_1, r_2) = ([0.63, 7.94], [0.63, 1.90]) \, \text{Å}\).

With this representation of vibrational eigenfunctions, we use a relaxation method to determine the ground-state vibrational eigenfunction,\(^{27,28}\) propagating an initial trial wavefunction via the time-propagation operator in imaginary time, \(\tau = \text{i} t\):

\[
\chi_{\text{trial}}(\tau) = e^{-\text{i}Ht/\hbar}\chi_{\text{trial}}(0) \tag{5.5}
\]

Since any trial wavefunction represents a superposition of all the eigenstates of the Hamiltonian, each eigenstate will be damped out exponentially at a rate proportional to its energy; thus, the ground-state eigenfunction will die out most slowly. Accordingly, as \(\tau \to \infty\), \(\chi_{\text{trial}}\) will collapse to the ground-state eigenfunction. Thus, obtaining the ground state eigenfunction requires repeated application of the propagation operator \(e^{-\text{i}Ht/\hbar}\) to the trial wavefunction. Since the relaxation process does not preserve the norm of the wavefunction, the length of the timestep is limited by the need to renormalize \(\chi_{\text{trial}}\) repeatedly to avoid reaching machine precision.

Next, the excited-state eigenfunctions are calculated via the same relaxation method. However, for each excited state, all previously determined lower eigenstates are first projected out from the trial wavefunction, so that an expansion of the trial wavefunction in the eigenfunctions of the system contains only excited-state wavefunctions. Accordingly, propagation in imaginary time will collapse the wavefunction to the lowest excited state included, i.e., the next-higher state in energy.
In practice, all lower eigenstates are projected out at each imaginary timestep to avoid collapsing to a lower state via numerical instabilities.

To employ this relaxation technique for determining the eigenstates, we expand the propagation operator in imaginary time in a series of Chebychev polynomials, i.e.,

\[
e^{-\frac{H\tau}{\hbar}} \equiv \sum_{n=0}^{N} a_n(\tau) T_n(-\frac{H\tau}{\hbar})
\]

(5.6)

where the \(T_n\) are real Chebychev polynomials and the \(a_n\) are the expansion coefficients described below.\(^{27}\) Because Chebychev polynomials are exponentially convergent on \([-1, 1]\), the Hamiltonian must be renormalized such that its eigenvalues span that range, with

\[
\Delta E = E_{\text{max}} - E_{\text{min}} = (T_{\text{max}} + V_{\text{max}}) - V_{\text{min}}
\]

(5.7)

\[
E_{\text{avg}} = \frac{(E_{\text{max}} + E_{\text{min}})}{2},
\]

(5.8)

where \(T_{\text{max}}\) and \(T_{\text{min}}\) are the upper and lower limits on kinetic energy, and \(V_{\text{min}}\) is the minimum potential energy. Eqn. 5.6 is then rewritten as

\[
e^{-\frac{H\tau}{\hbar}} \equiv e^{E_{\text{avg}}\frac{\tau}{\hbar}} \sum_{n=0}^{N} a_n\left(\frac{\Delta E\tau}{2\hbar}\right) T_n\left(-\frac{2[H - E_{\text{avg}}]}{\Delta E}\right)
\]

(5.9)
the multiplicative factor preceding the expansion is a phase factor resulting from the renormalization of the Hamiltonian. The expansion coefficients $a_n$ are from modified Bessel functions, $I_n$,

$$a_n = (2-\delta_{bn})I_n(\Delta E\tau/2\hbar) ,$$  \hspace{1cm} (5.10)

and the Chebychev expansion is calculated from the recursion relation

$$T_n(X) = 2XT_{n-1}(X) - T_{n-2}(X) ,$$  \hspace{1cm} (5.11)

where $X = -2(H-E_{\text{ave}})/\Delta E$, $T_0(X) = 1$, and $T_1(X) = X$. This series exponentially converges for $N > (\Delta E\tau/2\hbar)^{1/2}$. Since $\Delta E$ increases as the range of eigenvalues increases, more polynomials must be included for exponential convergence. Consequently, we truncate the potential and kinetic energies so that the upper limit is two times the estimated maximum eigenenergy (set to be ~20,000 cm$^{-1}$ above the potential minimum).

Once an eigenstate has been calculated, its quality can be estimated by computing the energy dispersion$^{29}$

$$D(\tau) = \sqrt{\langle \chi(\tau) | H^2 | \chi(\tau) \rangle - \langle \chi(\tau) | H | \chi(\tau) \rangle^2}$$  \hspace{1cm} (5.12)

which equals zero for a pure eigenstate.
We first employ the Chebychev propagation to calculate the vibrational eigenstates at a Cl-H$_2$O separation of 7.94 Å, i.e., in a region where coupling caused by the Cl atom among vibrational states of water should be negligible. Eigenstates from both the Cl + H$_2$O and HCl + OH wells are included. Subsequently, we incrementally vary the Cl-H$_2$O distance from 7.94 to 2.12 Å on a uniform spatial grid of 512 points in R. For efficient convergence, we use the eigenstate calculated at the previous R as the initial guess for the calculation at the next R. The convergence of these eigenstates is verified for each R to approach machine precision (limited from 16 digits to 8 digits by the square root in Eqn. 5.12), with D < 0.008 cm$^{-1}$. This process generates adiabatic potential curves as a function of R, with one curve for each vibrational wavefunction. These vibrational potential energy surfaces, $E_n(R)$, thus govern the Cl-H$_2$O intramolecular motion. In additional calculations, similar surfaces are obtained for Cl + D$_2$O and Cl + HOD on the same Cl + H$_2$O potential surface, i.e., varying only the mass of the isotope.

5.2.2. *Adiabatic coupling terms*

To calculate the coupling elements between adiabatic curves, an assumption of separate timescales for vibrational and nuclear motion is no longer valid. Thus, terms involving the derivative of the vibrational motion with respect to the nuclear coordinate must be added back into the nuclear Schrödinger equation given in Eqn. 5.3, which can now be written as$^{30}$
where $E_n(R)$ is an adiabatic vibrational potential energy surface calculated as above, $E$ is the total energy of the system, and $\tau_{nm}$ and $\rho_{nm}$ are the coupling terms

\[
\tau_{nm}(R) = \frac{\hbar^2}{\mu_{\text{Cl-HO}} \mu_{\text{Cl-HO}}} \langle \chi_n \left| \frac{\partial}{\partial R} \chi_m \right| \rangle,
\]

\[
\rho_{nm}(R) = \frac{\hbar^2}{2\mu_{\text{Cl-HO}}} \langle \chi_n \left| \frac{\partial^2}{\partial R^2} \chi_m \right| \rangle.
\]

Operationally, we follow the method of Tuvi and Band\cite{Tuvi1983} to symmetrize these coupling terms to preserve the hermiticity of the Hamiltonian. This process requires rewriting the Schrödinger equation as

\[
\left[ -\frac{\hbar^2}{2\mu_{\text{Cl-HO}}} \frac{\partial^2}{\partial R^2} + E_n(R) - E \right] \psi_n(R) =
\sum_m \left[ \tau_{nm}(R) \frac{\partial}{\partial R} + \rho_{nm}(R) \right] \psi_m(R),
\]

where

\[
\rho_{nm}(R) = \rho_{nm}(R) - \frac{\partial}{\partial R} \left[ \tau_{nm}(R) \right]
= -\frac{\hbar^2}{2\mu_{\text{Cl-HO}}} \left\langle \chi_n \left| \frac{\partial}{\partial R} \frac{\partial}{\partial R} \chi_m \right| \right\rangle.
\]
Equation 5.16 is analytically equivalent to 5.13; however, all derivatives of the vibrational eigenfunctions with respect to R in $\tau_{nm}$ and $\tilde{\rho}_{nm}$ are now first derivatives, facilitating numerical computation. We calculate these derivatives to second order, additionally taking advantage of the hermiticity of $\tilde{\rho}_{nm}$ and anti-hermiticity of $\tau_{nm}$ to average each element with its transpose or the complex conjugate of its transpose, respectively.

In addition to using the coupling terms for calculating the wavepacket dynamics, we can estimate relative curve-crossing velocities in the following way. The most significant coupling term is typically $\tau_{nm}$; as described by Child, $\frac{\partial}{\partial R}$ is related to the momentum operator, such that $|\tau_{nm} \frac{\partial}{\partial R}|$ is related semiclassically to equal $|\mu_{\text{Cl-HO HOH}} v_{\text{rel}}(R)/\hbar|$, where $v_{\text{rel}}(R)$ is the relative Cl-H$_2$O velocity at a given R. $|\tau_{nm} \frac{\partial}{\partial R}|$ becomes most significant as it approaches the magnitude of the energy spacings between nearest adiabats, i.e., $|E_n(R)-E_m(R)|$. We can thus estimate the characteristic transition velocity by setting these two terms equal to each other and solving for $v_{\text{rel}}(R)$ to obtain a characteristic transition velocity, $v_{nm}(R)$:

$$v_{nm}(R) = \frac{|E_m(R) - E_n(R)|}{\left\langle \chi_n \frac{\partial}{\partial R} \chi_m \right\rangle}$$

(5.18)

$v_{nm}(R)$ is thus the characteristic $v_{\text{rel}}$ for the transition between the $n^{th}$ and $m^{th}$ adiabats, similar to a Landau-Zener velocity for crossing between diabats; its minima (i.e., the most likely crossing points) occur at values of R corresponding to avoided crossings between adiabats. At relative Cl-H$_2$O velocities smaller than the minimum in $v_{nm}(R)$...
at a crossing region, we would thus expect the system to proceed adiabatically. Correspondingly, these velocities should aid in our predictions for the curve-crossing dynamics.

5.2.3. Wavepacket propagation

The final step in this process is determining how the choice of initial \( \text{H}_2\text{O} \) vibrational state and relative Cl-H\(_2\text{O} \) velocity influence the dynamics of the Cl + H\(_2\text{O} \) collision by performing time-dependent wavepacket scattering calculations. In brief, our approach is to begin a Gaussian wavepacket on one of the adiabats at a large Cl-H\(_2\text{O} \) separation and propagate forward in real time, using a Chebychev expansion of the propagation operator. When the wavepacket reaches the Cl-H\(_2\text{O} \) interaction region, the coupling terms between the adiabats allow for transfer of probability to other states. The flux in each output channel is calculated as the wavepacket exits the interaction region to determine the relative amounts of each product state. After the region of flux calculation, an appropriately scaled damping operator is placed on each of the output channels so that the wavefunction does not reflect or transmit at the end of the grid. The details of this phase of the computation are given below.

The time-dependent technique resembles time-independent methods by permitting determination of the branching ratios among elastic, inelastic and reactive scattering channels after the wavepacket has entered and exited the interaction region. Unlike time-independent methods, this technique has the important advantage of following the flow of probability among channels as a function of time to determine how the wavepacket makes transitions at crossing regions. The disadvantage of this
technique is that rather than providing monoenergetic scattering probabilities, the
wavepacket must (by the Heisenberg uncertainty principle) contain some spread in
momentum. While the energy-dependent scattering can nevertheless technically be
recovered, it requires calculating the outgoing flux for extended periods of time (i.e.,
without damping). For our purposes, this difficulty can more simply be overcome by
making the wavepacket appropriately broad in coordinate space and thus narrow in
momentum space. Thus, the initial conditions for the wavepacket propagation are
selected in the following way.

For each of the three reaction systems, the initial Gaussian wavepackets have
center momenta at a near-thermal velocity, with additional momenta explored for Cl
+ H$_2$O. For Cl + H$_2$O, Cl + D$_2$O, and Cl + HOD, initial momenta are 10.0, 10.4, and
10.2 au, respectively, scaled to have equivalent kinetic energy in all three collision
systems. The additional momenta selected for Cl + H$_2$O are 15.0 and 20.0 au; thus,
the three Cl + H$_2$O momenta correspond to relative energies of 510, 1100, and 2000
cm$^{-1}$ and speeds of 101,000, 152,000, and 202,000 cm/s (for comparison, the mean
relative speed of Cl and H$_2$O at 300 K is 73,000 cm/s). The spatial extent of all
wavepackets is chosen to be 0.26 Å; for Cl + H$_2$O, the Gaussian width in momentum
space ($\Delta p = 2.0$ au) is less than the spacing between the three momenta (5.0 au).
These wavepackets are then centered at R = 6.9 Å, away from the interaction region.
Convergence of the calculation with respect to this choice of distance is explicitly
verified for each momentum and mass combination by comparison with the output
flux from wavepackets begun at 6.35 Å; the flux in each channel varies by $\leq 1\%$ of its
own value.
As with the eigenfunction relaxation method described above, a Chebychev expansion is used for the propagation operator. However, since the wavepacket propagation is in real time, the expansion is modified in this way:

\[ e^{-\frac{\mathbf{H}t}{\hbar}} \equiv e^{\frac{i\mathbf{E}_{\text{avg}} t}{\hbar}} \sum_{n=0}^{N} a_n \left( \frac{\Delta E t}{2\hbar} \right) \varphi_n \left( \frac{-2[\mathbf{H} - E_{\text{avg}}]}{\Delta E} \right) \] (5.19)

where the \( \varphi_n \) are imaginary Chebychev polynomials defined on \([-i,i]\). The expansion coefficients, \( a_n \), are calculated from Bessel functions, \( J_n \), via \(^{26}\)

\[ a_n = (2 - \delta_{0n}) i^n J_n (\Delta E t / 2\hbar) \] (5.20)

The recursion relation for the Chebychev polynomials is similar to the one given in Eqn. 5.11, with modifications for damping out the wavefunction in the exit channel described below; however, this expansion converges exponentially for \( N > (\Delta E \tau / 2\hbar) \) (note the lack of square root). The Chebychev propagator preserves the norm of the wavepacket, and in principle, the timestep can be of unlimited size, at the cost of additional terms in the expansion. However, in order to be able to monitor the flux and observe the wavepacket propagation, the timestep is chosen to be 12.5 fs; correspondingly, the typical size of the Chebychev expansion is on the order of 300-400 polynomials. With this expansion, preservation of the total norm of the wavepacket is verified to be better than one part in \( 10^8 \) per timestep, with approximately 100 timesteps required for each propagation.
After the wavefunction exits the interaction region, the flux out of each exit channel is averaged over a series of points prior to the absorbing boundary. The accumulated flux at each point in a given channel is thus obtained from

\[
F = \sum J(t)\Delta t = \frac{\Delta t}{\mu_{CI-HOH}} \sum R \left[ |\psi^*(R, t)|^2 \frac{\hbar}{i} \frac{\partial}{\partial R} |\psi(R, t)| \right],
\]

where \( \Delta t \) is the size of the timestep. Since the initial norm of the wavepacket equals 1, the accumulated flux summed over all channels should also equal 1; we thus explicitly verify that this accumulated flux agrees to \( \leq 1\% \) with the wavepacket probability lost by the end of the calculation.

After the wavepacket passes through the region in which the flux is calculated, a damping operator is applied at each time propagation step to absorb the wavepacket, preventing reflection from or transmission through the end of the grid. Following Mandelshtam and Taylor, this damping operator has the form

\[
e^{-\gamma(R)},
\]

where

\[
\gamma(R) = c(R-R_0)/(R_{\text{max}}-R_0), \quad R \geq R_0
\]

\[= 0, \quad R < R_0
\]
with $R_{\text{max}}$ equal to the largest Cl-H$_2$O radius (7.94 Å), and $c$ and $R_0$ as adjustable parameters such that the damping operator decreases from $\exp\{-\gamma(R_0)\} = 1$ to $\exp\{-\gamma(R_{\text{max}})\} = \exp(-c)$. The operator is incorporated into the Chebychev expansion of the propagation operator by

$$
\phi_n(X) = e^{-\gamma(R)}[2X\phi_{n-1}(X) - e^{-\gamma(R)}\phi_{n-2}(X)],
$$

(5.24)

where $X = -2(H-E_{\text{avg}})/\Delta E$, $\phi_0(X) = 1$, and $\phi_1(X) = \exp\{-\gamma(R)\}X$. The operator thus acts on the wavepacket via multiplication by $\exp\{-\gamma(R)\}$ in the region $[R_0, R_{\text{max}}]$.

We determine the optimal parameters for this operator by fixing $R_0$ such that $(R_{\text{max}} - R_0) = 1.32$ Å, i.e., significantly larger than the deBroglie wavelength of the lowest input momentum (for $p = 10$ au, $\lambda_{\text{deBroglie}} = 0.32$ Å), and varying $c$. Trial wavepackets with one center momentum are propagated towards this absorbing boundary on a single potential curve (with all couplings turned off); $c$ is optimized by minimizing the survival probability for this wavepacket (i.e., reflection plus transmission). This procedure is repeated for a range of center momenta; in all cases, the survival probability is robustly insensitive to ~20-30% changes in $c$. Accordingly, the optimal choice of $c$ for any center momentum can be estimated from a quadratic least-squares fit of these data points. The parameters from this least-squares fit are given in Table 5.2.
Table 5.2. Table of parameters from quadratic fit of optimal damping parameters, \( c \), for \( \text{Cl} + \text{H}_2\text{O} \): \( c = Ax^2 + Bx + C \).

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>1.47E-6</td>
</tr>
<tr>
<td>B</td>
<td>9.23E-4</td>
</tr>
<tr>
<td>C</td>
<td>3.46E-3</td>
</tr>
</tbody>
</table>

To dampen the elastically scattered output wavepacket, the \( c \) parameter used corresponds to the initial center momentum. However, the portions of the wavepacket that make transitions to other states (via the adiabatic coupling terms), will not have the same center momentum. Rather, the kinetic energy of the fraction of the wavepacket on a different output channel should approximately equal the input channel kinetic energy plus the difference in the asymptotic potential energies of the two states. Based on this difference, the output momentum on any other state can be estimated and the damping parameters selected accordingly. In addition, since the wavepackets are typically started near the damping region, the damping operator is initially fixed to 1 (i.e., no damping) across its entire range for sufficient time (typically 250-500 fs) for the wavepacket to propagate out of that region.

5.3 Results

The results of these calculations are divided into two parts. In Section 5.3.1, we examine the static picture, i.e., the vibrational eigenstates calculated as a function of \( R \), the resulting adiabatic potential curves, and the couplings between these curves, focusing on developing predictions for the subsequent dynamics calculations. In
Section 5.3.2, we discuss the wavepacket propagation on these potential curves, determining how the dynamics proceed and how the initial vibrational state influences the subsequent dynamics. In these, we primarily focus on the results for Cl + H$_2$O, comparing with Cl + D$_2$O and Cl + HOD when appropriate.

5.3.1. Vibrational eigenfunctions, adiabats, and coupling elements

As described in Section 5.2.2, we have calculated the H$_2$O and OH/HCl vibrational eigenfunctions as a function of parametric Cl + H$_2$O distance. We first calculate the asymptotic eigenfunctions (i.e., at large Cl-H$_2$O separation), including eigenstates up to the sixth excited state, to serve as an initial basis for our subsequent parametric variation of R. The eigenenergies calculated at each step in R thus generate the adiabatic potential curves for Cl + H$_2$O shown in Fig. 5.2.

We can determine the states represented by adiabatic curves by examining the asymptotic eigenstates, which can then be used to label each of the curves. These eigenstates encompass the ground vibrational state, the lowest (v=1) stretching manifold in Cl + H$_2$O and OH + HCl, and the next excited state (corresponding to HCl(v=2) + OH(v=0) asymptotically) to ensure the availability of a higher energy output channel. These adiabatic curves by definition always follow the lowest seven eigenstates; thus, these labels may not accurately represent the nature of the wavefunction in the Cl + H$_2$O interaction region. However, asymptotically, the fourth excited state corresponds to the symmetric stretch of water, and the fifth excited state, the antisymmetric stretch; the adiabats corresponding to these states will thus serve as the input channels for the dynamics calculations.
Figure 5.2. Adiabatic potential energy curves for Cl + HOH reactive scattering, generated by calculating the H\textsubscript{2}O and OH/HCl vibrational eigenfunctions as a function of parametric R. Asymptotic eigenfunctions (at large Cl-HOH separation) serve as an initial basis for the parametric variation.
As seen in Fig. 5.2, the adiabats begin to vary in energy as R approaches 3.5 Å, indicating that they have reached the region where the couplings among various states should become quite significant. Accordingly, we re-examine the character of the vibrational eigenstates in this region. In Fig. 5.3a-d, we focus in particular on the symmetric and antisymmetric stretch eigenstates at two Cl-H₂O distances: outside the interaction region (R = 4.23 Å, Fig. 5.3a-b), where the eigenstates resemble the asymptotic eigenstates, and near the interaction region (R = 2.8 Å, Fig. 5.3c-d). As mentioned previously, the “proximal” OH bond, r₁, points toward the Cl, the “distal” bond, r₂, is on the opposite side of the molecule; thus, eigenstates at short r₁ correspond to Cl + H₂O states, and at long r₁, to HCl + OH states.

Intriguingly, the eigenfunction that corresponds asymptotically to the symmetric stretch (Cl + H₂O(s=1), the fourth excited state) becomes directed primarily along the *proximal* OH bond (r₁) with the Cl approach, i.e., it has rotated toward the Cl. Thus, the vibrational excitation is now pointed toward the reactive atom. In contrast, the antisymmetric stretch (Cl + H₂O(a=1), the fifth excited state) rotates to localize primarily along the *distal* OH bond (r₂), i.e., away from the reactive Cl atom. Thus, the approach of the Cl atom breaks the symmetry of the potential to convert *normal*-mode states into *local*-mode stretches. The localization of the symmetric stretch excitation toward the Cl might lead us to predict this state to be more reactive than the antisymmetric stretch. To further explore how the changing character of these eigenstates will affect reactivity, we next examine the adiabatic curves in more detail, looking at all three systems studied (Cl + H₂O/D₂O/HOD).
Figure 5.3. Fourth and fifth excited-state vibrational eigenfunctions for Cl + HOH outside the interaction region (R = 4.23 Å, Fig. 5.3a and b, respectively) and near the interaction region (R = 2.8 Å, Fig. 5.3c and d, respectively). The fourth excited-state eigenfunction, which corresponds asymptotically to the symmetric stretch (5.3a), becomes directed primarily along the proximal OH bond (r₁) with Cl approach (5.3c), so that the vibrational excitation points toward the reactive atom. In contrast, the fifth excited-state wavefunction, which corresponds asymptotically to the antisymmetric stretch (5.3b), rotates to localize primarily along the distal OH bond (r₂) (5.3d).
Figure 5.4a-c contains plots of the adiabats in the interaction region for these three systems, with the corresponding asymptotic states labeled (although not shown here, all curves are calculated to \( R = 7.94 \text{ Å} \) for use in the dynamics calculations). Avoided crossings are numbered, with the characteristic minimum velocity for each crossing (calculated from Eqn. 5.18) given in Table 5.3. For convenience, the classical turning points for the low (designated \( p_{lo} \), momentum = 10 au, \( v_{rel} \sim 1\times10^5 \text{ cm/s} \)) and high (\( p_{hi} = 20 \text{ au}, v_{rel} \sim 2\times10^5 \text{ cm/s} \)) momenta used in subsequent dynamics calculations are also designated. First, we focus on the general shape and trends in the curves, as well as discussing the locations of the turning points for the lowest momentum relative to the interaction region.

For Cl + H\(_2\)O (Fig. 5.4a), there are numerous avoided crossings between states; thus, it is not surprising that the character of the adiabatic wavefunctions changes dramatically. Notably, since the symmetric stretch on this surface is \( \sim 200 \text{ cm}^{-1} \) lower in energy than the antisymmetric stretch, it is correspondingly closer in energy to the HCl + OH product states in the \( v=1 \) manifold. In addition, the symmetric stretch also becomes even closer in energy to the ground state with decreasing \( R \), resulting in two narrowly avoided crossings between \( s=1 \) and \( \text{OH}(v=1) + \text{HCl}(v=0) \) in the region of \( R = 3.0 \) and 2.7 Å; this behavior is not exhibited by the antisymmetric stretch adiabat.

By examining the avoided crossings in more detail, we can predict the accessibility of each transition based on its characteristic velocity and distance from the classical turning point of the central wavepacket velocity. Nearly all of the avoided crossings for Cl + H\(_2\)O have lower characteristic crossing velocities than
Figure 5.4. Adiabatic potential energy curves for a) Cl + HOH, b) Cl + DOD, and c) Cl + HOD near the interaction region. Each number designates an avoided crossing between two curves, with the characteristic velocities (calculated from Eqn. 5.16) given in Table 5.3. The asymptotic eigenstates to which each curve corresponds are shown on the right side of the figure. For convenience, the arrows designate classical turning points for the low (designated $p_{lo}$, momentum = 10 au, $v_{rel}$ ~ $1 \times 10^5$ cm/s) and high ($p_{hi}$ = 20 au, $v_{rel}$ ~ $2 \times 10^5$ cm/s) momenta used in subsequent dynamics calculations on the fourth and fifth excited states.
Table 5.3. $v_{nm}$, curve-crossing velocities from Eqn. 5.16, in cm/s (see Fig. 5.4a-c for designation of crossing points).

<table>
<thead>
<tr>
<th>Crossing</th>
<th>Cl + HOH</th>
<th>Cl + DOD</th>
<th>Cl + HOD</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>&lt;50</td>
<td>100</td>
<td>42,000</td>
</tr>
<tr>
<td>2</td>
<td>800</td>
<td>2300</td>
<td>16,000</td>
</tr>
<tr>
<td>3</td>
<td>&gt;1E6</td>
<td>9000</td>
<td>180,000</td>
</tr>
<tr>
<td>4</td>
<td>&gt;1E6</td>
<td>18,000</td>
<td>2000</td>
</tr>
<tr>
<td>5</td>
<td>3200</td>
<td>5600</td>
<td>6000</td>
</tr>
<tr>
<td>6</td>
<td>1000</td>
<td>2500</td>
<td>22,000</td>
</tr>
<tr>
<td>7</td>
<td></td>
<td></td>
<td>15,000</td>
</tr>
</tbody>
</table>

the asymptotic value of the central velocity (see Table 5.3). However, the classical turning points for the $p = 10$ au wavepacket occur before the primary interaction region, thus only the leading fringes of the wavepacket in momentum space will reach those crossings. The strongest coupling links s=1 to OH(v=1) + HCl(v=0), with the first crossing between these states occurring just outside the reach of the central wavepacket velocity; from this, we would expect some possibility of reaction from s=1. In contrast, the only apparent reactive path for the $a=1$ state requires two transitions, first crossing near $R = 2.6$ Å into the symmetric stretch, then crossing through one (not both) of the avoided crossings between this state and OH(v=1). In light of these differences, the symmetric stretch should be the more reactive mode at low collision velocities because it ultimately places the vibrational excitation along the reaction coordinate and thus couples into product states.
For the Cl + D₂O adiabats (Fig. 5.4b), a picture emerges with subtle yet important differences. While the adiabatic potential curves have the same general shapes as those of Cl + H₂O, the curve-crossing velocities are generally 2-3 times higher (see Table 5.3). These velocities reflect the larger energy separations between neighboring states in the same stretch manifold (e.g., the asymptotic energy difference for s=1 and a=1 is 287 cm⁻¹ versus 204 cm⁻¹ for H₂O), and slightly smaller coupling terms (i.e., the wavefunctions vary more slowly with R). The major exception to this observation is the coupling to the DCl(v=2) state. The heavier mass of D versus H lowers the DCl(v=2) stretch relative to the v=1 manifold so that it approaches the antisymmetric stretch; consequently, the coupling velocities between the antisymmetric stretch and DCl(v=2) are approximately two orders of magnitude smaller than the equivalent velocities for H₂O. For this reason, we might expect to see an increase in the reactive scattering relative to inelastic scattering from Cl + D₂O over Cl + H₂O. In general, however, the velocity turning points on a=1 and s=1 in Cl + D₂O are further away from the interaction region, because 1) they occur at larger R, and 2) the crossing points among curves occur at smaller R. Consequently, the overall reactive and inelastic scattering for D₂O should be less than H₂O at the same energy.

For Cl + HOD (with the Cl approaching from the H side of the molecule), the adiabatic curves no longer resemble those of H₂O/D₂O and as such should produce substantially different dynamics. One important distinction between HOD and H₂O/D₂O is that the asymptotic product states in HOD do not correspond to localized vibration in HCl or OD and are simply designated by their total vibrational quanta.
Although they cannot be treated as uncoupled product states, this designation allows for distinguishing among elastic, inelastic, and reactive scattering. Of the two input stretches ($v_{OD}$ and $v_{OH}$), the $v_{OD}$ is lower in energy and thus closer to the product states below. However, the approaching Cl atom lowers the energy of $v_{OH}$ (relative to the ground state) because the path of the Cl lies along the OH bond. As a result, the classical turning point for $v_{OH}$ ($p_{lo}$) is much further into the interaction region than the turning points for either stretch in H$_2$O, and crossings with other states are more accessible. Correspondingly, we expect the total product in Cl + HOD to be larger than in Cl + H$_2$O for the low-momentum wavepacket.

For further comparison of Cl + HOD with Cl + H$_2$O, we examine the wavefunctions at the approach to the interaction region (see Fig. 5.5a-b). First, at the same $R = 4.23$ Å as examined for Cl + H$_2$O (i.e., corresponding to the asymptotic wavefunctions), the symmetric and antisymmetric stretches seen for Cl + H$_2$O are instead local-mode OH and OD stretches. While the symmetric stretch of H$_2$O rotates towards the Cl as it approaches, the OH stretch is localized towards the Cl axis for the entire approach of the reactive atom. However, the OH and OD stretches are not completely uncoupled. The adiabats demonstrate a very strong avoided crossing between these two states at $R = 2.8$ Å, indicating that the nature of the adiabatic wavefunctions changes rapidly with R. Accordingly, at that Cl-HOD distance, we have examined the fourth and fifth excited state wavefunctions (Fig. 5.5c-d), which correspond asymptotically to $v_{OD} = 1$ and $v_{OH} = 1$, respectively. Intriguingly, the character of the wavefunctions nearly *reverses* at this point: while both have probability in the product well, the fourth state resembles $v_{OH} = 1$ in the reactant well,
Figure 5.5. Fourth and fifth excited-state vibrational eigenfunctions for Cl + HOD outside the interaction region (R = 4.23 Å, Fig. 5.5a and b, respectively) and near a very strongly avoided crossing (R = 2.8 Å, Fig. 5.5c and d, respectively). The asymptotic eigenfunctions correspond to local-mode OH (Fig. 5.3a) and OD (Fig. 5.5b) stretches. However, at the strongly avoided crossing, the character of the wavefunctions nearly reverses: in the reactant well, the fourth state (Fig. 5.5c) resembles $v_{OH} = 1$, while the fifth state (Fig. 5.5d) resembles $v_{OD} = 1$. 
while the fifth state resembles $v_{OD} = 1$. Correspondingly, we might expect some transfer between those states, with greater transfer from $v_{OH} = 1$ to $v_{OD} = 1$ because $v_{OH}$ is higher in energy.

5.3.2. $Cl + H_2O/D_2O/HOD$ wavepacket propagation

Having calculated the vibrationally adiabatic potential energy curves and the coupling elements between those curves, we probe the dynamics by propagating wavepackets on each incoming state of interest. As detailed in Section 5.2.3, Gaussian wavepackets at relative velocities of approximately 10,000, 15,000, and 20,000 cm/s are employed to explore the dynamics and branching ratios among elastic, inelastic, and reactive scattering. This analysis focuses first on $Cl + H_2O$ dynamics, primarily at the lowest collision energy, then on additional energies and collision systems.

We first examine a sample wavepacket propagation into the $Cl + H_2O$ interaction region, monitoring transfer into other channels. Figure 5.6a follows the course of a wavepacket initiated on the $Cl + H_2O(a=1)$ state, with $t = 0$ at the bottom of the graph and each step higher indicating an additional 100-fs step. Most noticeably, the majority of the wavepacket probability remains on this curve for the duration of the interaction region, disappearing only when it is absorbed at the end of the grid by the damping operator. Thus, the dominant output channel is elastic collision between $Cl$ and the antisymmetric stretch of $H_2O$ with no effect on the vibrational eigenstate.
Figure 5.6. Sample wavepacket propagation for Cl + H₂O(a=1), monitoring the scattering into a) Cl + HOH(a=1), b) Cl + HOH(s=1), and c) HCl(v=0) + OH(v=1). The initial wavepacket is given at the bottom of the graph; each incremental step higher indicates an additional 100-fs step. For visual clarity, the wavepackets in 5.6b and c are increased in amplitude by factors of 50 and 250, respectively, relative to 5.6a. Most of the wavepacket probability remains in the elastic Cl + HOH(a=1) state; however, this sufficiently couples with other states to transfer probability into inelastic (5.6b) and reactive (5.6b) scattering.
While this vibrationally adiabatic picture describes the majority of the reaction probability for \( \text{Cl} + \text{H}_2\text{O}(a=1) \) at this low collision energy, the wavepacket experiences some coupling with other states, with a small amount of transfer to other curves. For example, Fig. 5.6b demonstrates the growth of probability on the \( \text{Cl} + \text{H}_2\text{O}(s=1) \) state, with the magnitude increased by 50 times relative to the elastically scattered wavepacket for visual clarity. This figure illustrates that as the initial wavepacket reaches the potential well, the state that asymptotically correlates to the antisymmetric stretch sufficiently couples to the asymptotic symmetric stretch state to produce a redistribution of vibrational energy. Similarly, Fig. 5.6c shows the transfer of probability to the reactive \( \text{HCl}(v=0) + \text{OH}(v=1) \) state, magnified by a factor of 250. Interestingly, at this energy, vibrational redistribution (Fig. 5.6b) is more likely to occur than chemical reaction (Fig. 5.6c). While these pictures do not provide quantitative information about the product distributions, they do provide a first glimpse into the dynamics of this system.

In order to provide quantitative determinations of probability in each exit channel, the fluxes as a function of time are monitored as described in Sect. 5.2, terminating when the remaining wavepacket probability is less than 0.01. Fig. 5.7a-b gives the accumulated fluxes versus time for the \( p = 10 \) au calculations of \( \text{Cl} + \text{H}_2\text{O}(s=1) \) and \( \text{Cl} + \text{H}_2\text{O}(a=1) \), respectively. Both figures demonstrate that these are predominantly direct reactions, i.e., without long-lived resonance states; the near-exponential rise in flux likely results from the spread in the Gaussian wavepacket. Notably, this direct behavior is similar among all input states and momenta calculated for each of the water isotopes. In addition, for both states of \( \text{Cl} + \text{H}_2\text{O} \) at this input
Figure 5.7. Accumulated fluxes versus time for the scattering from a) Cl + H₂O(s=1) and b) Cl + H₂O(a=1) for \( p = 10 \) au (510 cm\(^{-1}\) collision energy, and 101,000 cm/s relative Cl-H₂O speeds). These plots indicate that at these energies, the interactions are predominantly elastic (i.e., >90% probability of exiting on the entrance channel). Of the remaining channels, reaction dominates over inelastic scattering from H₂O(s=1) to H₂O(a=1) (Fig. 5.7a); in contrast, inelastic scattering from H₂O(a=1) to H₂O(s=1) dominates over reaction (Fig. 5.7b).
momentum, the elastic channel dominates, with a total probability near 0.95 of exiting on the input channel. Among those channels which alter Cl + H₂O state, reactive channels dominate over inelastic scattering from H₂O(s=1) to H₂O(a=1) (Fig. 5.7a); in contrast, inelastic scattering from H₂O(a=1) to H₂O(s=1) dominates over reactive scattering (Fig. 5.7b). Thus, as predicted from the adiabatic potentials, the symmetric stretch is more reactive than the antisymmetric stretch of H₂O.

Monitoring the accumulated flux out of each channel in this fashion allows a comparison of the products of the Cl + H₂O reaction with the other collision systems studied, namely, Cl + D₂O and Cl + HOD (each calculated for p ~ 10 au). The flux out of each channel is summed over reactive and inelastic product states and plotted in Fig. 5.8. Overall, these data support the predictions made from the adiabatic curves, as discussed in Section 5.3.2. First, as predicted from the rotation of the symmetric stretch wavefunction toward the Cl atom, the symmetric stretches of both H₂O and D₂O are more reactive than the antisymmetric stretches. In addition, the overall amount of inelastic and reactive scattering from H₂O is larger than from D₂O, consistent with the larger coupling velocities between states of D₂O and the greater distance of the classical turning points from the interaction region. Finally, the OH vibrational excitation of HOD is the most reactive of all states of H₂O/D₂O/HOD and, indeed, is more reactive than ν₀D by nearly an order of magnitude, consistent with a local-mode picture of this reaction.

However, two more subtle comparisons of reactive and inelastic flux warrant additional investigation. First, despite the apparent similarity in adiabatic potential curves between H₂O and D₂O, the antisymmetric stretch states of these two molecules
Figure 5.8. Accumulated flux for $p \sim 10$ au wavepackets into non-elastic channels for Cl + HOH, Cl + DOD, and Cl + HOD, summed separately over inelastic and reactive channels. The symmetric stretches of both H$_2$O and D$_2$O are more reactive than the antisymmetric stretches, with overall amount non-elastic scattering from H$_2$O greater than from D$_2$O, while the OH vibrational excitation of HOD is the most reactive state.
produce opposite relative amounts of inelastic and reactive products. Second, despite
the excitation of the “wrong” bond in HOD, reactive scattering from $v_{OD} = 1$ is
significantly larger than inelastic scattering. This is somewhat surprising, in part
because the curve-crossing velocity with $\text{Cl} + \text{HOD}(v_{OH}=1)$ given in Table 5.3 is
smaller than the velocity for coupling with the highest mixed $v=1$ wavefunction, thus
one might expect that inelastic channel to dominate.

Fortunately, time-dependent wavepacket propagation allows for monitoring
of probability in each channel as a function of time, i.e., for directly observing
transfers between states. Accordingly, we examine the probability in each channel as
a function of time for several initial states, plotted in Fig. 5.9a-b and 5.10a-b.
Importantly, the diminution of the total probability at the end of the reactive
encounter results from application of the damping operator near the end of the grid.

For $\text{Cl} + \text{H}_2\text{O}(s=1)$ and (a=1), comparisons of the dynamics can be made
between Fig. 5.9a-b. For the input channel $\text{Cl} + \text{H}_2\text{O}(s=1)$ (Fig. 5.9a), three major
pathways (i.e., $\text{HCl}(v=0) + \text{OH}(v=1)$, $\text{HCl}(v=1) + \text{OH}(v=0)$, and $\text{Cl} + \text{H}_2\text{O}(a=1)$)remove probability nearly simultaneously from that state, indicating that probability
transfers directly to each of the dominant product states. In comparison, for the initial
state $\text{Cl} + \text{H}_2\text{O}(a=1)$ (Fig. 5.9a), probability first transfers from a=1 to s=1, as
evidenced by the growth of probability in s=1. This transfer must occur as the tail of
the wavepacket reaches the avoided crossing between these two states (designated as
avoided crossing 5 on the adiabatic potential curves in Fig. 5.3a). As the probability
in s=1 subsequently drops near 500 fs, the probability in $\text{HCl}(v=0)$ grows, indicating
**Figure 5.9.** Wavepacket probability in each channel as a function of time for a) Cl + HOH(s=1) and b) Cl + HOH(a=1) at \( p \sim 10 \) au. At the end of the timescale, the probability in each channel approaches zero due to damping of the wavefunction outside the interaction region. For Cl + HOH(s=1) (Fig. 5.9a), probability transfers directly into the asymmetric stretch and two HCl/OH product states, while for Cl + H\(_2\)O(a=1) (Fig. 5.9b) probability first transfers into the symmetric stretch, then to HCl(v=0).
that the path from the input antisymmetric stretch state to reaction must pass through
the symmetric stretch.

As predicted in Sect. 5.3.2, the dynamics of Cl + D₂O(a=1) are altered from
those of Cl + H₂O(a=1) by the presence of a low-lying state from the v=2 manifold.
Fig. 5.10a demonstrates that as with H₂O(a=1), some probability transfers from a=1
to s=1 and subsequently into the DCl + OD v=1 product states. However, more
probability flows directly from D₂O(a=1) into DCl(v=2) via avoided crossings 3 and
4 shown on Fig. 5.3b. This behavior indicates that the lowering of the v=2 manifold
relative to v=1 by isotopic substitution effectively opens an additional product
channel unavailable to H₂O.

For Cl + HOD, the probabilities as a function of time from the v_{OD} input
channel are given in Fig. 5.10b. This probability plot shows amplitude oscillating out
of v_{OH}=1 as the wavepacket passes through the couplings at crossings 1 and 2 (Fig.
5.3c). Since the probability for the v=1 reactive product grows in between those two
peaks, it must result from the coupling at crossing 3. This result is intriguing, since
that coupling velocity is quite larger than most of the other coupling velocities yet
clearly contributes to the formation of the product channels.

The last part of this analysis is to examine how a greater collision momentum
affects the probability distribution in each product channel, focusing on Cl + H₂O.
Figure 5.11a-b plots the output fluxes from Cl + H₂O(s=1) and Cl + H₂O(a=1),
respectively, as a function of increasing momentum. Three major points can be
gleaned from a comparison of these two figures. First of all, not surprisingly, the
total amount of inelastic/reactive scattering increases with increasing momentum in
**Figure 5.10.** Wavepacket probability in each channel as a function of time for a) Cl + DOD(a=1) and b) Cl + HOD(v_{OD}=1), damped to zero after leaving the interaction region. For D₂O (5.10a), as with H₂O(a=1), some probability transfers from a=1 to s=1 to products; however, more probability flows directly from D₂O(a=1) into DCl(v=2) due the lowering of the v=2 manifold relative to v=1 by isotopic substitution. For Cl + HOD (5.10b), amplitude leaves v_{OH}=1 and transfers to the v=1 reactive product as the wavepacket passes through the avoided crossings 1 and 2.
Figure 5.11. Momentum dependence of output fluxes in each channel from a) Cl + H₂O(s=1) and b) Cl + H₂O(a=1). In both cases, total inelastic and reactive scattering increase with increasing momentum; for H₂O(s=1), inelastic scattering grows larger than reactive, while for Cl + H₂O(a=1), reactive grows larger than inelastic. As a result, at high collision momenta, excitation of the antisymmetric stretch forms more HCl + OH product than does the symmetric stretch.
both cases. This increase reflects the greater number of avoided crossings accessed by wavepackets at the higher momentum, as evidenced by the location of the classical turning points further into the interaction region (denoted $p_{hi}$ in Fig. 5.4a).

Second, the relative amounts of inelastic and reactive scattering reverse between low and high momentum: for scattering from $s=1$, inelastic grows larger than reactive, while for scattering from $a=1$, reactive grows larger than inelastic. The adiabatic curves for this system (Fig. 5.4a) provide an explanation for this phenomenon. As mentioned previously, as $R$ decreases, the $s=1$ adiabatic state begins to resemble a local-mode OH stretch directed toward the Cl atom, while the $a=1$ adiabat becomes a local-mode stretch away from the Cl. Correspondingly, the transition between these two adiabats represents a transition between local-mode stretches. For high-momentum scattering from $s=1$ and $a=1$, the classical turning point lies directly on the avoided crossing between these two states (avoided crossing 5); accordingly, a larger amount of wavepacket probability transfers than at low momentum. For input on Cl + H$_2$O($s=1$) (Fig. 5.11a), this diabatic transfer to the local-mode stretch away from the Cl leaves probability “stuck” in the $a=1$ exit channel, which has no subsequent crossings into reactive states as the wavepacket exits the interaction region. For input on Cl + H$_2$O($a=1$) (Fig. 5.11b), the opposite occurs: more probability transfers into the local-mode stretch toward the Cl and can subsequently transfer into the HCl($v=0$) + OH($v=1$) product state. The higher momentum also produces an increased probability of this transfer to the reactive channel such that probability in the product channel grows.
Third, as a result of these high-momentum inversions in inelastic versus reactive channels for both input states, the relative amounts of reaction product from the two input channels also inverts: excitation of the antisymmetric stretch now forms more HCl + OH product than does excitation of the symmetric stretch. In other words, the antisymmetric stretch becomes more reactive than the symmetric stretch with increased collision velocity. The implications of this result are discussed in the next section.

5.4 Discussion

The preceding section outlines the key results of the Cl + H₂O/D₂O/HOD reactive scattering calculations, exploring in detail how the adiabatic curves generated for this prototypical set of reaction systems can be used to predict the subsequent dynamics. Our final step is to reexamine the specifics of this model system to determine what insights can be formed that are independent from the details of the potential surface and the collinear water geometry.

Perhaps the most intriguing outcome of these calculations is the rotation of the symmetric-stretch eigenstate of H₂O towards the approaching Cl atom and the corresponding rotation of the antisymmetric stretch away from the Cl. This result indicates that, adiabatically, the antisymmetric stretch correlates with vibrational excitation in the non-reacting bond. This concept is not new; indeed, Schatz postulated that this correlation should generally exist in systems with symmetric and antisymmetric stretches for the following reason. The local-mode, reactive bond stretch is lowered in energy relative to the unreactive bond by the approaching
reactant; it thus adiabatically couples to the lower-energy symmetric stretch, thereby increasing the reactivity of the symmetric stretch relative to the antisymmetric stretch.

This principle was demonstrated by Schatz with classical trajectory calculations for O + CS₂: vibrational adiabaticity in this reaction yields more OS + CS product from the CS₂ symmetric stretch than the antisymmetric stretch.³⁵ This result is consistent with our results for Cl + linear H₂O: at the lowest translational energy calculated, the symmetric stretch of H₂O is more reactive. It is intriguing that this effect appears in both O + CS₂, in which O-S-C is a light-heavy-light atom combination, and in Cl + H₂O, with a Cl-H-O as a light-heavy-light combination, in calculations at comparable collision energies. Since the vibrational energies of the symmetric and antisymmetric stretch in CS₂ are much more widely separated than in H₂O, the adiabaticity in that system should persist to higher collision velocities. In contrast, the adiabaticity of our model H₂O breaks down at a collision velocity only three times higher than the average thermal velocity, indicative of a transition to diabatic behavior. Notably, the spacing between the experimental symmetric and antisymmetric stretch energies in water is approximately half that spacing in our model.³⁶ Correspondingly, we anticipate that the vibrational adiabaticity of water should break down at even lower, i.e., near-thermal, collision velocities.

A related result, observed in all three collision systems, is that the local-mode stretch in the reactive bond is lowered in energy with respect to the ground state as the reactive atom approaches. In H₂O and D₂O, this lowers the energy of the proximal OH stretch (which corresponds asymptotically to the symmetric stretch) toward the reactive channels. In Cl + HOD, however, this lowers the higher-energy
OH stretch toward the OD stretch, producing a strong mixing between $v_{OH}$ and $v_{OD}$ character in the HOD well region. While the magnitude of this mixing will vary for different systems, the trend should be the same for any high-frequency vibration approached by a reactive atom.

Finally, the lowering of the next excited vibrational manifold ($v=2$) in D$_2$O relative to D$_2$O($v=1$) opens up a higher-energy product channel for the antisymmetric stretch of D$_2$O, one which is unavailable to H$_2$O. This emphasizes that isotopic substitution affects not only the vibrations within a single manifold, but also the positioning of those vibrational manifolds with respect to one another.

5.5 Conclusions

The role of intramolecular vibrational redistribution (IVR) on the timescale of a reactive encounter is explored via time-dependent quantum reactive scattering on a linear model system with isotopic variations. In these studies, the vibrational eigenstates of Cl + H$_2$O → HCl + OH are calculated as a function of Cl-H$_2$O center-of-mass separation using a Chebychev expansion of the time-dependent propagation operator in imaginary time. This calculation generates adiabatic potential energy curves, as well as the coupling matrix elements for transitions between these curves, for use in time-dependent dynamics calculations. For the vibrational eigenfunctions, the near-resonance of the H$_2$O symmetric and antisymmetric stretch causes these states to couple strongly as the Cl atom approaches. These couplings rotate the symmetric stretch of H$_2$O into a local-mode excitation pointing towards the Cl, and the antisymmetric stretch away from the Cl. Scattering calculations from the
symmetric and antisymmetric stretch thus indicate greater probability for product formation from the symmetric stretch than the antisymmetric stretch at low collision velocities. This vibrational adiabaticity breaks down at higher velocities, so that the antisymmetric stretch becomes more reactive than the symmetric stretch. For the similar Cl + D₂O simulation, the reduced stretching vibrational frequencies provide less energy towards reaction, hence the reaction probability decreases for both modes, while the lowering of the DCl(v=2) product state relative to the antisymmetric stretch states increases reactive scattering over inelastic scattering from the symmetric stretch. For Cl + HOD, vibrational excitation in OH enhances HCl + OD reaction probability by an order of magnitude more than excitation in OD.
References for Chapter 5


V. Aquilanti, private communication


NAG Fortran Library (Oxford University: Oxford, 1997).


Rothman, L. S., HITRAN database (ONTAR, 1996)


J. Tennyson, private communication


