

Synchronization and phase lock of two mode-locked femtosecond lasers

Robert K. Shelton, Long-Sheng Ma,* Henry C. Kapteyn, Margaret M. Murnane, John L. Hall, and Jun Ye†

*JILA, National Institute of Standards and Technology and University of Colorado,
and Department of Physics, University of Colorado, Boulder, CO 80309-0440*

Two independent mode-locked femtosecond lasers are synchronized to an unprecedented precision. The rms timing jitter between the lasers is 4.3 fs observed within a 160 Hz bandwidth over tens of seconds, or 26 fs within a 50 kHz bandwidth. Novel multi-stage phase locked loops help to preserve this ultrahigh timing resolution throughout the entire delay range between pulses (10 ns). We also demonstrate that the same level of synchronization can be achieved with two lasers at different repetition frequencies. Under such synchronization, phase lock between the carrier frequencies of the two fs lasers has been achieved.

The ability to synchronize a passively mode-locked laser to an external reference, or to a second laser, has many applications in science and technology. Previous work in synchronizing two mode-locked Ti:Sapphire lasers has demonstrated timing jitter of at best a few hundred femtoseconds (fs)^{1,2}. Since it is now routine to generate pulses with duration <20 fs, improved techniques would make it possible to take full advantage of this time resolution for applications such as high power sum- and difference-frequency mixing, novel pulse generation and shaping, and for novel laser/accelerator based light sources³. Indeed, accurate timing of high intensity fields is essential for several important schemes in quantum coherent control and extreme nonlinear optics such as efficient X-ray generation⁴. Perfect synchronization between two ultrafast lasers would enable precision control of femtosecond lasers at the same level of technological maturity as for the cw lasers, leading to unprecedented flexibility and bandwidth for pulse synthesis and optical comb generation.

A Kerr-lens mode-locked (KLM) femtosecond laser generates a regularly spaced comb of optical frequencies. Stabilization of this wide-bandwidth optical frequency comb has many useful applications^{5,6}. Precision phase control of the fs comb has already revolutionized the field of optical frequency metrology^{7,8}, providing the capability of a direct phase-coherent link between optical and microwave frequencies. Frequency-domain control of fs combs not only provides an effective means to transfer the stability of a cw optical oscillator to the entire comb⁹, but also has a strong impact on the time domain evolution of carrier-envelope phase¹⁰. The frequency spacing of the comb interval, which represents one of the two degrees of freedom of the comb, has been controlled effectively either through a microwave clock^{7,8} or via a stable laser⁹. Since the frequency mode spacing of the fs-comb is equal to the inverse of the cavity round trip time of the laser, reducing phase noise of the repetition rate spectrum directly improves the control of timing jitter.

In this paper, we demonstrate robust synchronization of pulse trains from two separate fs lasers, with a timing jitter of < 5 fs, at a bandwidth of 160 Hz, observed over an interval of one minute. The two independent mode-locked Ti:Sapphire lasers¹¹ operate at 780 nm and 820 nm respectively, with ~ 100 MHz repetition rates. One laser is pumped by a Spectra Physics Millennia and the other by a Coherent Verdi. The bandwidth of both lasers corresponds to a transform limit of <20 fs mode-locked pulses. Our synchronization scheme shown in Fig. 1 employs two high-speed photo-diodes to detect the two pulse trains. These signals are then input to three phase locked loops (PLL) working at different timing resolutions. We synchronize the repetition rate of laser #1 to a stable RF source, while laser #2 is synchronized to laser #1 using the PLL. The first PLL compares and locks the fundamental frequencies of the two lasers to 100 MHz. The phase shift between the two 100 MHz signals can be used to control the timing offset between two pulse trains. The second PLL compares the phase of the 80th harmonic of the two repetition frequencies; i.e., at 8 GHz. The second loop is activated and replaces the first one when the two pulse trains are nearly overlapped. This represents an electronic realization of a “differential micrometer”, – the 100 MHz loop provides the full dynamic range of timing offset between two pulse trains, while the 8 GHz loop produces enhanced phase stability of the repetition frequency. To further minimize jitter, the intensity of the sum frequency signal from the two pulse trains overlapped in space and time is directly used as a control error signal for a third loop. This third loop can be usefully activated only when the 8 GHz PLL is working effectively and most timing jitter noise has already been eliminated. All three loops actuate fast piezo-transducers (PZT) mounted to the laser end-mirrors. We use a combination of a fast, small, PZT and a slow, long, PZT to achieve a high servo bandwidth (> 50 kHz) and a large tuning range.

The motivation for using a high harmonic for phase locking the repetition rate is to obtain an enhanced signal-to-noise ratio (S/N). In Fig. 2 the solid curve represents the detected phase noise power spectrum of the laser repetition

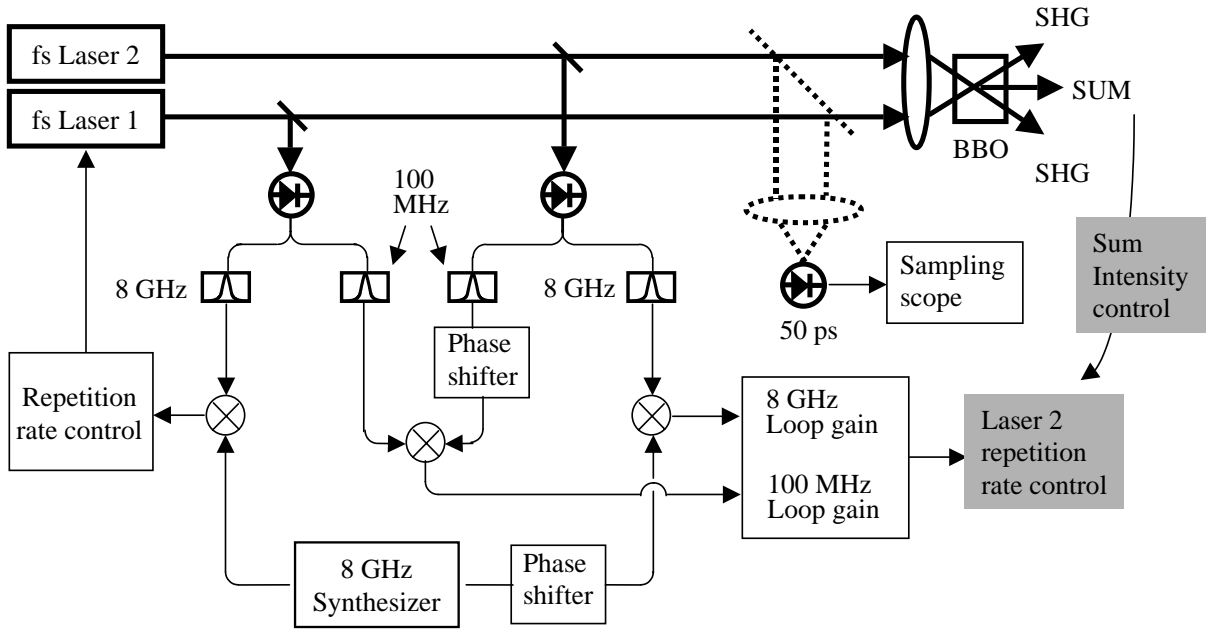


FIG. 1: Experimental setup for timing synchronization of two fs lasers. The three phase locked loops for synchronization are shown, along with the signal analysis scheme.

signal, while the dotted curve indicates the microwave reference to which the repetition signal is locked. Experimental data show that the laser repetition signal has less fast phase noise than the rf reference beyond the frequency B (around 10 kHz) indicated in Fig. 2. Therefore the servo loop bandwidth should be limited to below B , provided that the noise floor of the repetition detection is a few dB below the dashed line. If the detection S/N is not sufficiently high, then the servo bandwidth will be further limited. Detection at a high harmonic can help to avoid this problem. The high-speed photo diodes used in this experiment suffer a loss of S/N of only 3 dB when the repetition signal is detected at the 80th harmonic, compared with the S/N at the fundamental. When analyzed at the fundamental while stabilized at the 80th harmonic, the repetition signal thus enjoys an effective increase in S/N of 16 dB.

Figure 3 shows the effective use of the two PLLs for the control of the timing offset between two pulse trains. The second pulse train is scanned relative to the first via phase shift inside the 100 MHz loop, showing the full range scanning capability in Fig. 3 (a) and (b). Once the two pulses are within 200 ps of each other, we gradually reduce the gain of the 100 MHz PLL and increase the gain of the 8 GHz loop, leading to a smooth transition between the two loops and a small jump of the timing offset by at most 62.5 ps (1/2 of one 8 GHz cycle). Tuning of the timing offset can then be continued with the 8 GHz loop, as shown in Fig. 3 (c) and (d) with expanded time axis. The two pulses are maximally overlapped in Fig. 3 (e).

To further characterize our system, we focus the two pulse trains so that they cross in a 500 μm -thick, room temperature, BBO crystal for nonlinear frequency generation (Type-I). Figure 4 (a) shows the generated second harmonic light from the two pulse trains after the crystal. When the two pulses are overlapped in space and time, sum frequency generation is enabled, as shown with the bright spot in the center of Fig. 4 (b). We can thus use the intensity of the sum frequency generation as a diagnostic tool to study our system performance. Figure 4 (c) shows a cross-correlation measurement between the two pulses, carried out by a simple electronic sweep of the relative phase inside the 8 GHz PLL. The Gaussian FWHM of the cross-correlation peak is 164 fs. This compares well with a theoretical estimate of 160 fs, based on the measured pulse widths of 82 fs and 138 fs for the individual lasers. (Because no extra-cavity dispersion compensation is used, the 20 fs laser pulses are broadened due to dispersion.) Since the PLL system compares the phase of the two 8 GHz signals with a double-balanced mixer, the phase scan can be accomplished by either tuning a phase shifter in the second signal path before the mixer or by injecting a precision voltage waveform into the output port of the mixer. Compared to a mechanical scanning system, this electronic tuning method offers a vastly superior performance in terms of the repeatability, reliability, and speed for setting the time offset, with no noticeable hysteresis when we switch back and forth between two pre-selected phase values.

The intensity fluctuations in the generated sum-frequency light are proportional to the timing jitter, particularly when the two pulses are offset in time by $\sim 1/2$ the pulse width. At short time scales, the intensity fluctuation of the sum frequency light can be studied by simply recording the pulse-to-pulse variation. Using a ns-speed photodiode and ns sampling rates, we have directly digitized the sum frequency pulse train over a period of 10 μs . (The length of data

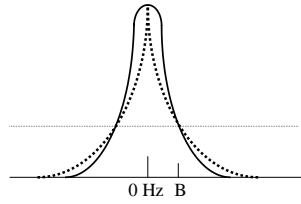


FIG. 2: Phase noise spectrum of the microwave reference signal (dotted curve) compared with the phase noise of the detected laser repetition signal (solid curve). At frequencies higher than B, the laser has an intrinsically lower noise than the reference.

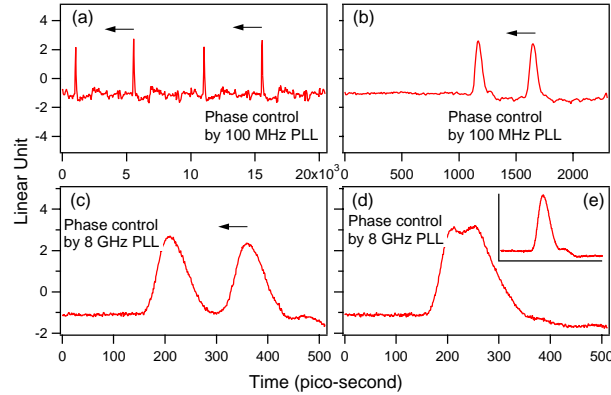


FIG. 3: Control of the relative timing offset between the two independent pulse trains using the combined phase locked loops. Relative to laser #1, the pulse train from laser #2 is scanned via the rf phase shifter in the PLL. (a) Two independent pulse trains incident on a same photodiode, with repetition period of 10 ns. (b) Expanded time axis, 100 MHz PLL control. (c) Time scale further expanded, 8 GHz PLL control. (d) Two pulses nearly overlapped via adjustment of the 8 GHz phase shifter. (e) Two pulses maximally overlapped, permitting study of relative timing jitter.

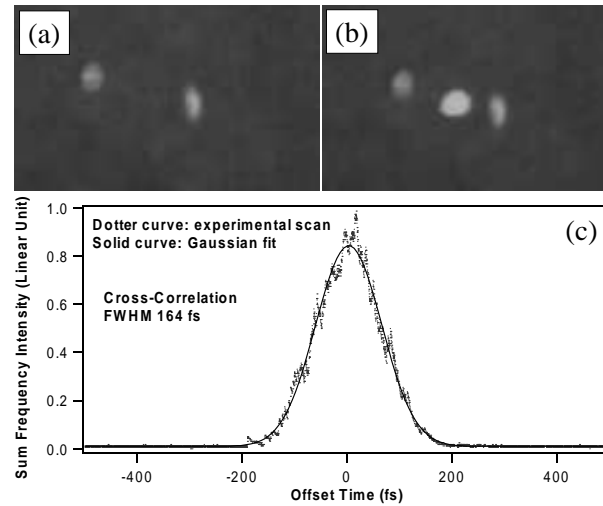


FIG. 4: (a) Second harmonic generation from two spatially crossed pulse trains in a BBO crystal. (b) Sum generation is enabled when the two pulses are synchronized and overlapped. (c) Cross-correlation measurement via the electronic scan of relative phase.

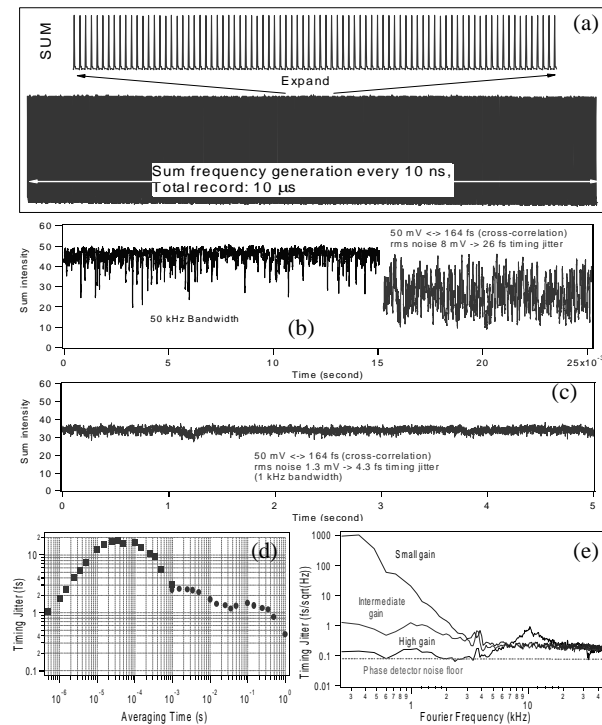


FIG. 5: Timing jitter noise analysis. (a) A $10\ \mu\text{s}$ direct digitization record of the sum frequency generation. Also shown is the time-expanded trace. The pulse-to-pulse intensity fluctuation is below 0.4%, similar to the original laser intensity fluctuation. (b) Sum frequency generation observed with a 50 kHz bandwidth. The left trace shows two pulses optimally overlapped and the right trace shows two pulses offset by a half width. (c) Sum signal observed under a 160 Hz bandwidth, showing an rms timing jitter noise of 4.3 fs. (d) Allan variation of the timing stability, showing the maximum jitter occurs around 10 - 100 μs . (e) Fourier frequency spectrum of the error signal from the 8 GHz phase locked loop.

is limited by the digitizer memory.) The recorded data is shown in Fig. 5 (a), along with the expanded trace, when the relative timing offset between the two original pulse trains is near zero. The pulse-to-pulse variation of the sum frequency signal is basically the same as that of the original pulses from the two lasers, – below a level of 0.4%. Since the bandwidth of our servo loop does not quite reach the $10\ \mu\text{s}$ time scale, this superior timing stability is attributed entirely to the free-running lasers due to the lack of environmental disturbance on such short time scales. At longer time scales, the intensity fluctuation in the sum frequency signal can be explored with an appropriate low-pass filter to avoid sampling noise. A 50 kHz low-pass filter is sufficient to suppress the discrete nature of the pulse train and permit the study of intensity fluctuations on a cw basis. In Fig. 5 (b), the left trace shows the sum frequency intensity fluctuation when the two pulse trains are maximally overlapped, while the right trace is recorded when the two pulses are offset in time by $\sim 1/2$ the pulse width. For the right trace, the sum frequency signal is monitored near the middle point of the cross-correlation peak shown in Fig. 4 (c). Therefore the intensity fluctuations can be translated linearly into timing jitter noise using the calibrated slope of the correlation peak. For a maximum intensity of the sum frequency light at 50 units, and the FWHM of the cross-correlation peak at 164 fs, we can conservatively estimate the conversion scale of the slope at 3.3 fs/unit. The rms timing noise from the right trace is thus determined to be ~ 26 fs at a 50 kHz bandwidth. At higher bandwidths, the jitter does not increase. If we use a bandwidth of 160 Hz (equivalent to 1 ms averaging time) the resultant intensity fluctuations of the summing light shown in Fig. 5 (c) indicates rms timing jitter noise of 4.3 fs. We have recorded such stable performance over periods extending to nearly a minute. The advantage of the high harmonic PLL over the 100 MHz loop is particularly clear from the recorded sum frequency intensity, exhibiting fluctuations more than 20 times bigger when under the 100 MHz control. The synchronization lock can be maintained for durations of several hours, limited by the dynamic range of the servo PZT and by thermal expansion. A simple integrator stage is implemented to control the temperature of the laser base-plate to extend the lock time even further.

It is interesting to explore further the issue of the timing jitter noise vs its characteristic time scales (or equivalently its frequency spectrum). Allan variance analysis¹² is a powerful technique developed for the study of frequency noise of stable oscillators in the time domain. The approach compares adjacent measurements segmented within certain time windows. In this first-difference calculation one is able to separate and isolate processes based on their time

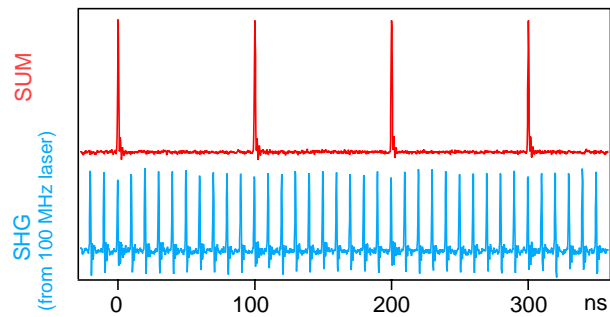


FIG. 6: Sum frequency generation from two synchronized fs-lasers that have different repetition rates, one at 90 MHz and the other at 100 MHz. The second harmonic signal from the 100 MHz laser is also shown. Notice the slight decrease in the second harmonic signal when sum frequency generation occurs with two pulses overlapped.

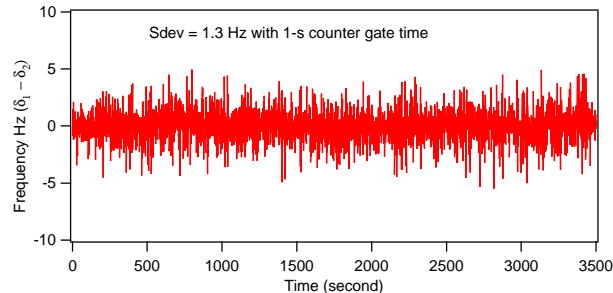


FIG. 7: Record of the carrier beat signal between the two fs lasers when they are synchronized and phase locked. The beat frequency under the locked condition shows a standard deviation of 1.3 Hz at 1-s averaging time.

scales. This is useful to identify time scales at which fluctuations are the largest. From the time record of the timing jitter noise shown in Fig. 4 (b) and (c), we calculate the Allan variance of the timing jitter. The result is shown in Fig. 5 (d). The data points in “square” correspond to the fast time record [the right trace in Fig. 5 (b)] while the data points in “circle” correspond to the longer record [shown in Fig. 5 (c)]. It is clear from this analysis that the dominant timing jitter noise occurs within 10 - 100 μ s, a region where the gain of the PLL loop is rolling off from the low frequency end while the external perturbations to the laser are increasing from the high frequency end. However, it is satisfying to find that the timing jitter noise never exceeds 20 fs at any timescale.

These results can be confirmed through the equivalent analysis of the error signal within the PLL servo loop¹³. Figure 5 (e) shows the Fourier spectrum analysis of the error signal at different gain settings. When the loop is operated stably with a high gain, within a frequency range from DC to 5 kHz the error signal is very close to the limit ($\leq 0.1fs/\sqrt{Hz}$) set by the intrinsic noise floor of the 8 GHz mixer, i.e., the phase comparator used in the PLL. (We have removed the last two data points below 250 Hz that were affected by the DC offsets of the Fourier-transform spectrum analyzer.) A small servo bump appears near 10 kHz and rolls off to a flat noise floor near $0.14fs/\sqrt{Hz}$. Integrating the noise density over the interested spectral range (from DC to 50 kHz) would yield an rms timing jitter noise of ~ 30 fs, slightly larger than that indicated by the direct time domain data.

The flexibility of this synchronization system is demonstrated by locking two independent lasers working at different repetition frequencies. The 81st harmonic of the repetition rate of laser #1, still operating at 100 MHz, is compared to the 90th harmonic of laser #2, now running at 90 MHz. The two pulse trains will then collide in the time domain every 100 ns, leading to a sum-frequency pulse train at a 10 MHz repetition-rate. The result is shown in Fig. 6, where the top trace reflects the summing frequency generation and the bottom trace is the second harmonic generation of the 100 MHz laser. Notice the slight decrease in the second harmonic intensity when sum frequency generation occurs with two pulses overlapped. This approach can be generalized to produce sum- and difference- frequency generations with arbitrary repetition rates, yet perfectly synchronized to the master frequency.

When the two lasers are well synchronized, heterodyne beat between the two corresponding sets of combs can be recovered with impressive S/N . The beat detection effectively measures the difference in the carrier-envelope offset frequency between the two fs combs. Therefore by stabilizing the beat frequency to a prefixed value, for example, of a mean value of zero Hertz, the carrier-envelope phase evolution dynamics of one laser will be closely followed by the second laser. Locking of this beat frequency to zero Hz can be conveniently implemented using an acousto-optic modulator (AOM). One laser beam passes through the AOM, picking up the AOM’s frequency offset. The beat is

then phase locked to the AOM's drive frequency, effectively removing the AOM frequency from the beat. Figure 7 shows the recorded beat frequency signal under phase locked condition. With an averaging time of 1-s, the standard deviation of the beat signal is 1.3 Hz. When the phase lock loop is not active, the standard deviation goes up to a few MHz.

In summary, we have synchronized two independent mode-locked femtosecond lasers to an unprecedented precision. The remaining rms timing jitter between the lasers is 4.3 fs observed within a 160 Hz bandwidth over tens of seconds, or 26 fs within a 50 kHz bandwidth. This ultrahigh timing resolution is available through the entire dynamic range of pulse repetition period (10 ns). We have also demonstrated that such synchronization can be achieved with two lasers at different repetition frequencies. Such a degree of synchronization is necessary for realization of an optical carrier phase locked loop between independent femtosecond lasers¹⁴. The techniques developed should prove to be invaluable in many research areas of ultrafast science and extreme nonlinear optics.

ACKNOWLEDGMENTS

We are indebted to D. Anderson for the loan of a pump laser. We also thank S. T. Cundiff and T. H. Yoon for useful discussions. The work at JILA is supported by NIST, NASA, and NSF.

REFERENCES

- * Permanent address: East China Normal University, Shanghai, China
- † corresponding author, ye@jila.colorado.edu
- ¹ D. E. Spence *et al.*, *Opt. Lett.* **19**, 481 (1994).
- ² S. A. Crooker *et al.*, *Rev. Sci. Instru.* **67**, 2068 (1996).
- ³ R. W. Schoenlein, *et al.*, *Science* **274**, 236 (1996).
- ⁴ K. Kobayashi *et al.*, *Nucl. Instrum. and Methods A* **455**, 239 (2000).
- ⁵ R. Teets, J. Eckstein, and T. W. Hänsch, *Phys. Rev. Lett.* **38**, 760 (1977).
- ⁶ Y. V. Baklanov and V. P. Chebotayev, *Appl. Phys.* **12**, 97 (1977).
- ⁷ Th. Udem *et al.*, *Phys. Rev. Lett.* **82**, 3568 (1999); Th. Udem *et al.*, *Opt. Lett.* **24**, 881 (1999).
- ⁸ S. A. Diddams *et al.*, *Phys. Rev. Lett.* **84**, 5102 (2000);
- ⁹ J. Ye, J. L. Hall, and S. A. Diddams, *Opt. Lett.* **25**, 1675 (2000).
- ¹⁰ D. J. Jones *et al.*, *Science* **288**, 635 (2000).
- ¹¹ M. T. Asaki *et al.*, *Opt. Lett.* **18**, 977 (1993).
- ¹² D. W. Allan, *Proc. IEEE* **54**, 221 (1966).
- ¹³ H. Tsuchida, *Opt. Lett.* **24**, 1641 (1999).
- ¹⁴ R. K. Shelton, L.-S. Ma, H. C. Kapteyn, M. M. Murnane, J. L. Hall, and J. Ye (to be published, 2000).