

Status of the Solar neutrino problem ~2000

Several different experiments found neutrino fluxes smaller than the theoretical prediction:

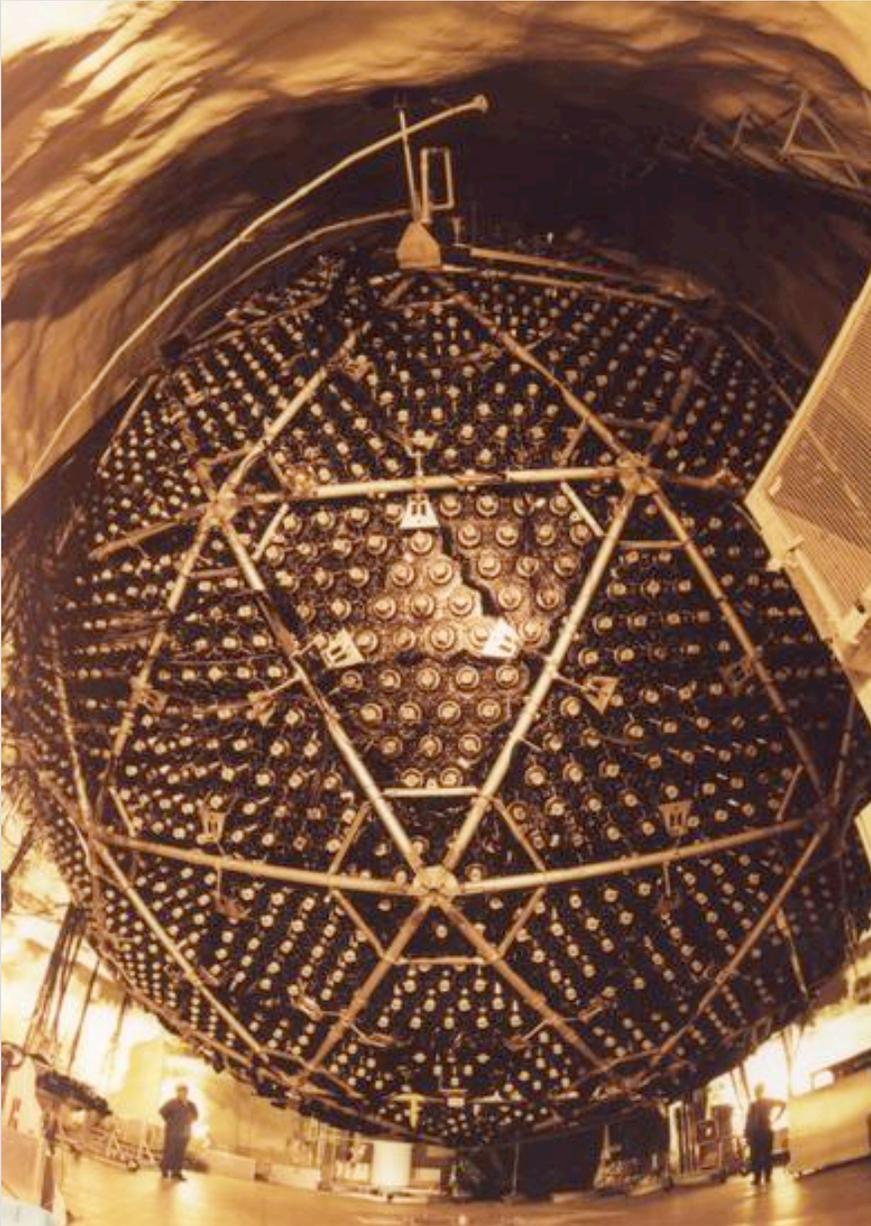
- **Chlorine** ($E > 0.8$ MeV) - 34%
- **Gallium** ($E > 0.2$ MeV) - 55%
- **Ordinary water** ($E > 5$ MeV) - 48%

Two possible explanations:

Sun is producing fewer neutrinos than expected. Gallium results meant that a fairly serious error in Solar structure would have been implied by this...

Electron neutrinos are being produced in the Sun at the 'right' rate, but are being 'lost' on their way to Earth.

Sudbury Neutrino observatory



Water cherenkov radiation detector, but uses heavy water D_2O rather than H_2O .

~1000 tons of D_2O , situated at 7000 foot depth in a mine.

Use of D₂O allows three separate classes of neutrino interaction to be detected:

Charged current $\bar{\nu}_e + d \rightarrow p + p + e^-$

Like the Cl \rightarrow Ar reaction (requires changing a neutron into a proton). **Only** works for electron neutrinos.

Elastic scattering $\bar{\nu}_x + e^- \rightarrow \bar{\nu}_x + e^-$

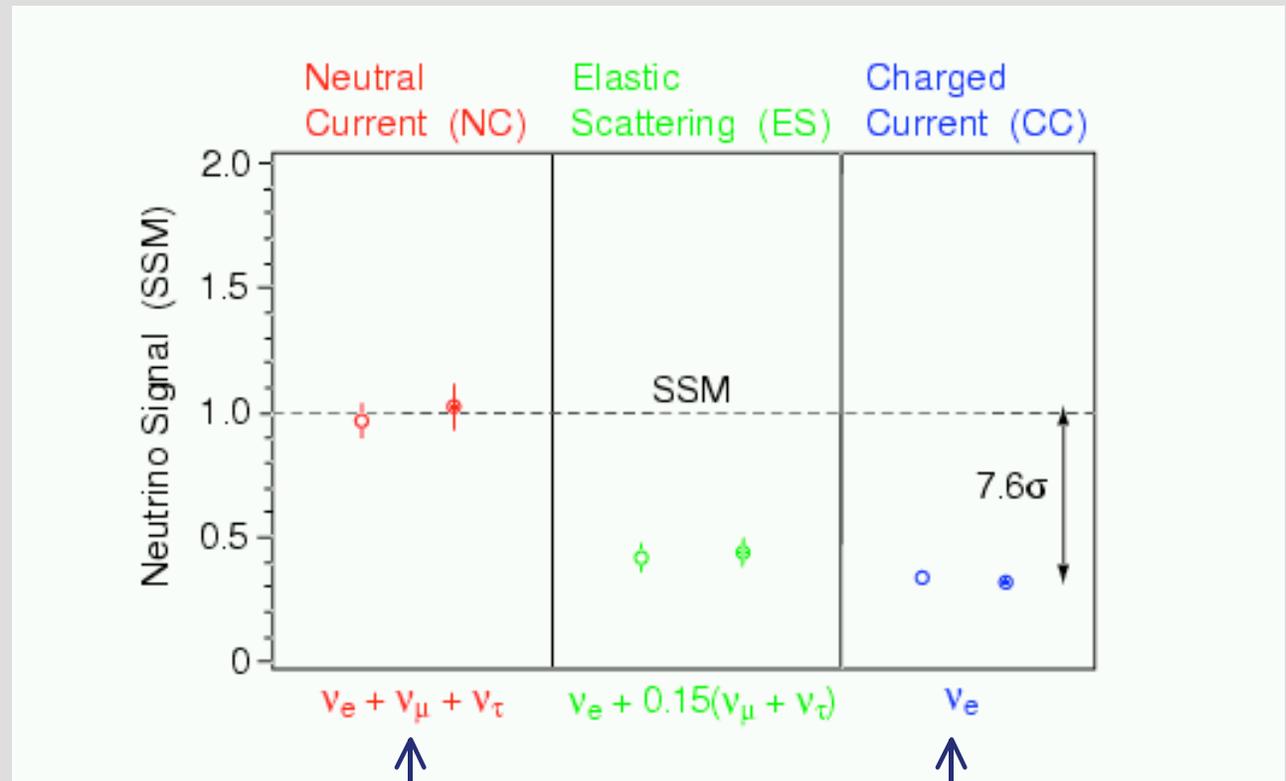
Same reaction as in Super-Kamiokande. Works for all neutrinos, but **much smaller** cross-section (15%) for muon or tau neutrinos as compared to electron neutrinos.

Neutral current $\bar{\nu}_x + d \rightarrow \bar{\nu}_x + n + p$

New reaction - neutrino breaks up a deuteron. Works equally for all neutrino flavours.

Results from Sudbury neutrino observatory

fraction of expected number of events (based on a Solar model prediction) that are observed



Total number of neutrinos agrees well with the theoretical expectation

Number of ν_e is about one third of number produced in the Sun

Most straightforward interpretation of these results:

1) Solar models correctly predict the number of electron neutrinos formed in the core of the Sun

Evidence: *total* flux of neutrinos at Earth (all three types) measured by SNO is in good agreement with this number.

Probably do understand the astrophysics of the Solar interior pretty well...

2) Electron neutrinos are converted into a mix of all three flavours en route to Earth

SNO and all other detectors measure a flux of *electron* neutrinos that is much smaller than the predicted Solar flux.

Neutrino oscillations

Basic idea: particles that are created / observed via nuclear interactions (the ν_e , ν_μ , and ν_τ) are linear combinations of 'different' particles which propagate through space.

e.g. for only two neutrino flavours can write this as:

particle states that are created or observed via weak interactions \longrightarrow

$$\begin{aligned}\nu_e &= \nu_1 \cos\theta + \nu_2 \sin\theta \\ \nu_\mu &= \nu_1 \sin\theta + \nu_2 \cos\theta\end{aligned}$$

particle states that propagate through space (the 'mass eigenstates')

Use factors of $\cos\theta$ and $\sin\theta$ for mathematical convenience, these are just constants. Call θ the 'mixing angle', measures how different the flavour states are from the mass states.

If the neutrinos (strictly now ν_1 and ν_2) have zero mass, this description does not describe any new physics.

However, if at least one of the masses is non-zero, then the mass eigenstates propagate at *different* speeds. After traveling some distance L , this causes the flavour of the neutrino to oscillate between the two possibilities.

Result is:

Probability that an initially electron neutrino will be subsequently detected as an electron neutrino

$$P_{ee} = 1 - \sin^2 2\theta \sin^2 \left[k \frac{m^2 L}{4E} \right]$$

- $k = \text{constant}$ ($k=1.27$)
- m^2 is the square of the mass difference
- L is distance between source and detector
- E is the energy

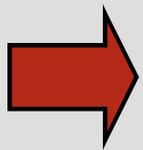
Actually, things are (even) more complicated because:

- there are 3 types of neutrino, not 2
- if the neutrinos travel through matter, not a vacuum, the oscillations can be altered

Important point though, is that using a combination of:

- Different Solar neutrino experiments
- Observations of μ created in the Earth's atmosphere

...can measure (most) of the unknown parameters in the theory.



Δm^2 - the mass difference (squared) between neutrino states

θ - the mixing angle(s)

Neutrino oscillations for different energies

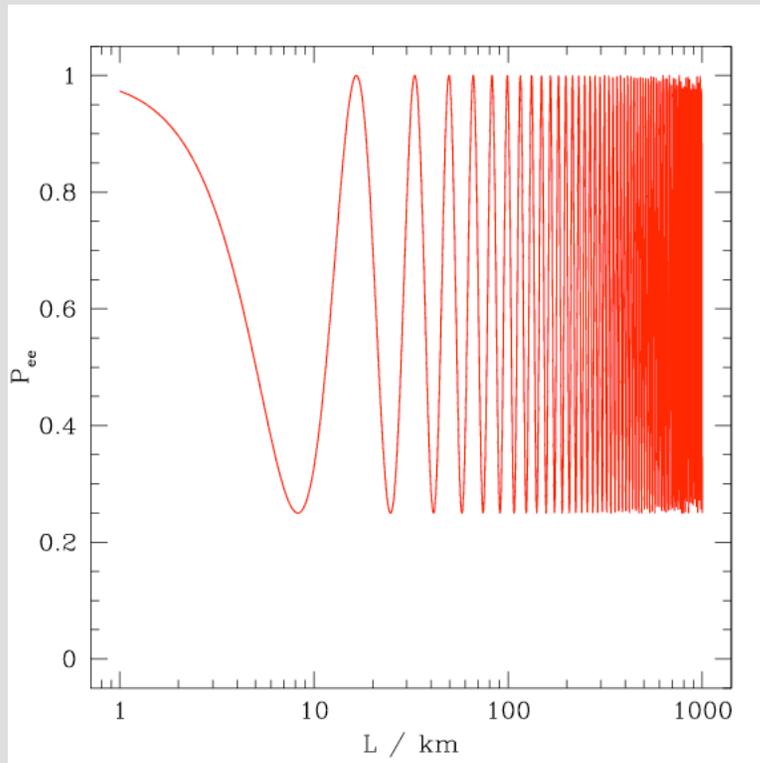
$$P_{ee} = 1 - \sin^2 2\theta \sin^2 \left[\frac{\Delta m^2 L}{4E} \right]$$

$$\theta \approx 45^\circ / 6$$

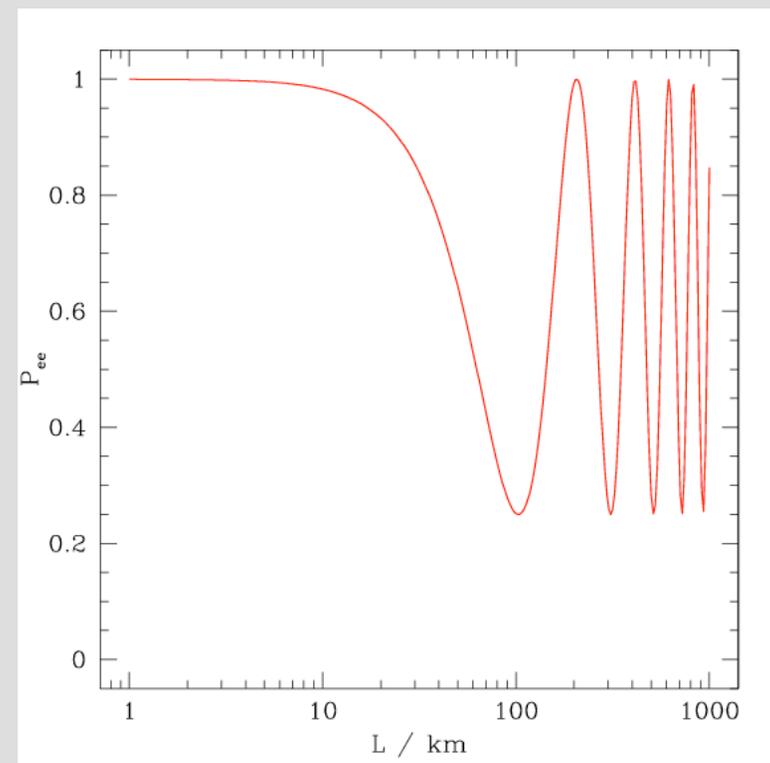
$$\Delta m^2 \approx 6 \times 10^5 \text{ eV}^2$$

Best-fit parameters to explain Solar neutrino and other experimental data

0.4 MeV



5 MeV

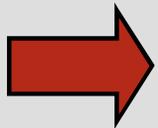


Derived oscillation parameters are accessible to lab experiments. For MeV neutrinos, need to measure the flux as a function of distance over $d \sim 100$ km. Possible neutrino sources:

- Nuclear reactor (very large power but isotropic emission)
- Particle accelerator (smaller power but narrow beam)

e.g. for a reactor with 1 GW power, each fission releases ~ 200 MeV. Rate of fissions is $\sim 3 \times 10^{19} \text{ s}^{-1}$. Say one neutrino each, then flux is:

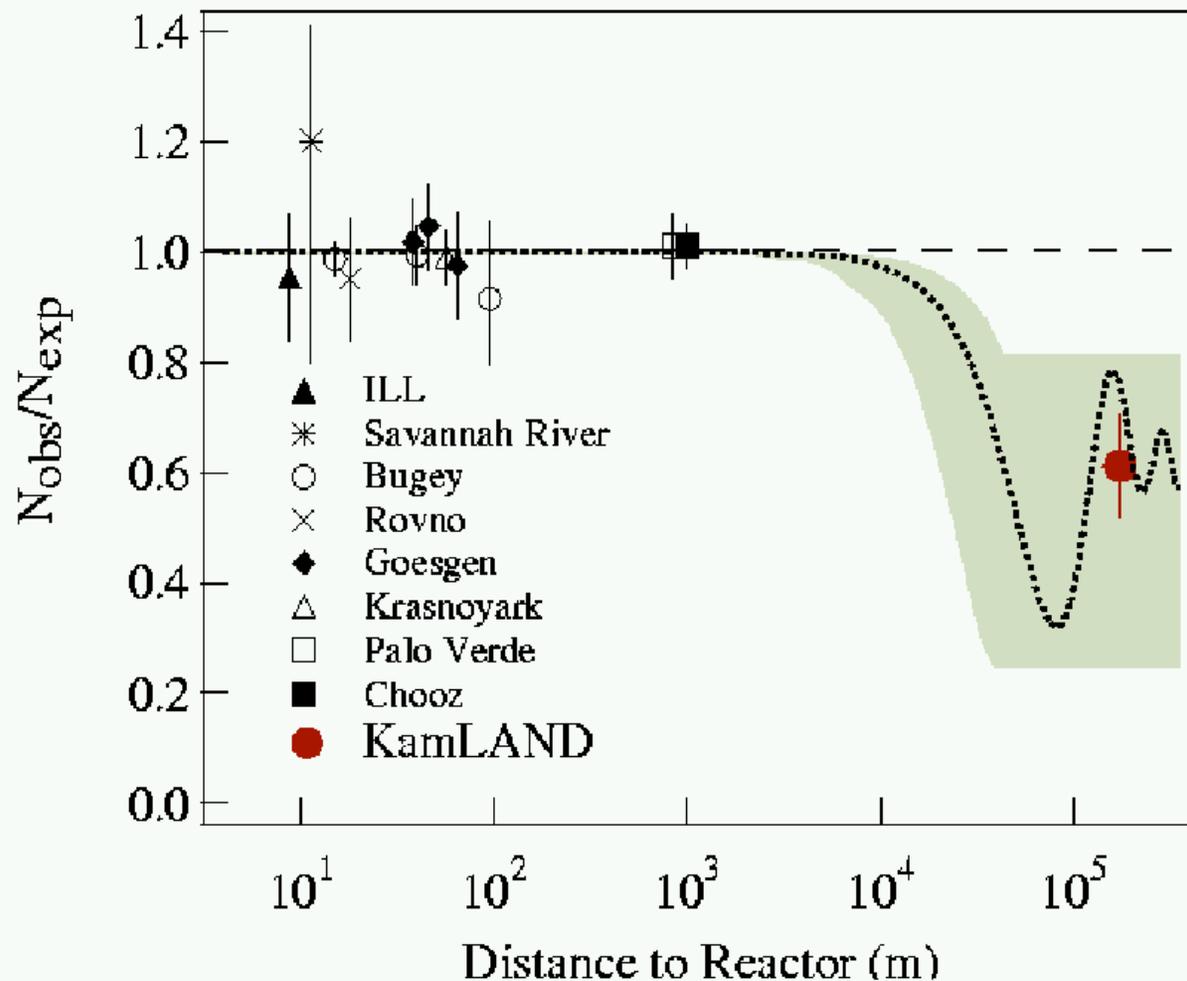
- $\text{few} \times 10^{10} \text{ cm}^{-2} \text{ s}^{-1}$ at $d = 100$ m
- $\text{few} \times 10^4 \text{ cm}^{-2} \text{ s}^{-1}$ at $d = 100$ km



Comparable difficulty to the Solar neutrino experiments for distances of ~ 100 km

KamLAND experiment

Experiment measured the flux of neutrinos at $d = 160$ km from a Japanese power station. Found to be $\sim 60\%$ of expected flux.



Very strong evidence for reality of neutrino oscillations.

Implications

Neutrinos have mass:

- So far constrained the mass **difference** between two neutrinos to be $\sim 6 \times 10^{-5} \text{ eV}^2$
- Might be 'reasonable' to assume the masses are comparable to the mass difference i.e $\sim 10^{-2} \text{ eV}$
- But... this is just a guess, don't know for sure.
- Other limits indicate that the masses are $< 1 \text{ eV}$.

Learned more about neutrino physics than about the Sun - all existing data is *consistent* with theoretical models of fusion in the Sun, but enough free parameters in oscillation theory that haven't yet tested the details via neutrinos...